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**Per Zone Variable BPI for Improving Storage Device Capacity and Yield**

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**Field of the Invention**

The present invention relates generally to the storage of information ~~storage on a fixed storage media, and more particularly to improving storage of information on rotating magnetic media, such as a disks in a disk drive.~~

**Background of the Invention**

Data storage devices such as disk drives are used in many data processing systems for data storage. Typically a disk drive includes a magnetic data disk having ~~disk recording~~ surfaces with concentric data tracks, and a transducer head paired with each ~~disk recording~~ surface, for reading data from and writing data to, and reading data from, the data tracks. ~~Each paired magnetic head and media surface couples to provide a unique data recording capability which depends on the fly height of the head from the recording surface, the quality/distribution of magnetic media on the recording surface, and the magnetic properties of the magnetic head.~~

Disk drive storage capacity increases by increasing the data density (or areal density) of the data stored on the disk surfaces. Data density is the linear bit density on the tracks multiplied by the track density across the disk surface. Data density is measured in bits per square inch (BPSI), linear bit density is measured in bits per inch (BPI) and track density is measured in tracks per inch

1 (TPI). As data density increases, the head performance distribution also  
2 increases which diminishes disk drive storage capacity and yield.

3  
4 CConventional disk drives fail to account for methods of recording data  
5 using the paired head and recording surface are inefficient because they do not  
6 take into consideration the differences in data recording capabilities of between  
7 the one pair of head and disk recording surface pairs, and another head and  
8 surface pair. Conventionally, each disk surface is formatted to store the same  
9 amount of data as every other disk surface. However, each head and disk  
10 surface pair has unique data recording capability, such as sensitivity and  
11 accuracy, which depends on the fly height of the head over the disk surface, the  
12 magnetic properties of the head and the quality/distribution of the magnetic  
13 media for the disk surface. Thus, in conventional disk drives a head and disk  
14 surface pair that has a low error rate is formatted to the same BPI and TPI as a  
15 head and disk surface pair that has a high error rate.

16  
17 ~~\_\_\_\_\_ Though the heads are designed to perform identically in read/write~~  
18 ~~operations, in practice different heads in a disk drive can have different read/write~~  
19 ~~performance capabilities. Lower performing heads cannot read/write data as that~~  
20 ~~of other heads in the disk drive. Typically, a single error rate level and a single~~  
21 ~~storage capacity level are used to record data for all the pair heads and surfaces.~~  
22 ~~This results in inefficient data storage for those pairs of heads and surfaces that~~  
23 ~~can store more data. It also lowers the qualification yields of the disk drives~~  
24 ~~because one or more pairs of heads and surfaces do not record data at the~~  
25 ~~qualifying error rate and capacity levels.~~

26  
27 ~~\_\_\_\_\_ Further, in high data rate design of disk drives, as the recording density~~  
28 ~~(i.e. bits per inch and/or tracks per inch) is increased, maintaining transducer~~  
29 ~~head tolerances has become a challenge. Variance in the relative head~~  
30 ~~performance distribution increases with increasing data density. In conventional~~

1 ~~disk drives, the drive yield and capacity suffers as a result of head performance~~  
2 ~~variations in disk drives.~~

3  
4 ~~One method of increasing the data storage capacity of a disk drive~~  
5 ~~includes increasing the areal density of the data stored on the media surfaces~~  
6 ~~(bits/sq. in. BPSI). Areal density is the track density which is the number of~~  
7 ~~tracks per radial inch (TPI) that can be packed onto the media/recording surface,~~  
8 ~~multiplied by the linear density (BPI) which is the number of bits of data that can~~  
9 ~~be stored per linear inch.~~

10  
11 ~~Conventional disk drive manufacturing processes applies a single error~~  
12 ~~rate and a single data storage level for the head and disk surface pairs, and for~~  
13 ~~qualifying disk drives scraps a disk drives that include a low performing head and~~  
14 ~~disk surface pair that fails to meet when the qualifying requirements measured~~  
15 ~~disk capacity of the disk drive is less than a target disk capacity. This lowers~~  
16 ~~storage capacity due to inefficient use of high performing head and disk surface~~  
17 ~~pairs that can store more data, and lowers yield due to disk drives being~~  
18 ~~scrapped if they include a low performing head and disk surface pair even if they~~  
19 ~~also include a high performing head and disk surface pair. Conventionally, each~~  
20 ~~recording surface is formatted to store the same amount of data as every other~~  
21 ~~recording surface. Thus, a recording surface that has a low error rate is~~  
22 ~~formatted to the same TPI and BPI levels, as a recording surface having a high~~  
23 ~~error rate, even though it can store more data. However, by adopting a single~~  
24 ~~TPI and BPI level for every recording surface, conventional processed fail to~~  
25 ~~account for the differences in sensitivity and accuracy of the paired head and~~  
26 ~~recording surface, which results in less data storage and more waste of space on~~  
27 ~~each recording surface. This also results in lower overall yields of disk drives~~  
28 ~~because if even a few of the recording surfaces do not meet their targeted~~  
29 ~~capacity, the sum of the surface capacities of all the media surfaces will be less~~  
30 ~~than the target capacity, causing the entire disk drive to fail.~~

1 U.S. Patent Nos. 6,091,559 and 5,596,458 provide for recording at  
2 different BPI on different disk recording surfaces, however these approaches,  
3 ~~such methods~~ do not take into consideration multiple constraints, including head  
4 performance across the stroke per disk surface ~~affecting disk drive capacity,~~ disk  
5 drive performance requirements such as (e.g., throughput) and manufacturing  
6 requirements such as (e.g., test time). Instead, disk surface zZone frequencies  
7 are selected based on ~~measurement of a single metric for~~ one head.

8  
9 There is, therefore, a need for ~~a method of storing data in a disk drive~~  
10 which improves disk drive storage capacity and yield and while accounts for  
11 ~~meeting the desired target drive capacity or increasing the drive capacity while~~  
12 ~~meeting a desired drive yield by taking advantage of the head performance~~  
13 variation.

#### 14 15 Summary of the Invention

16 The present invention satisfies these needs.

17  
18 In an embodiment, a variable BPI storage format is a function of storage  
19 zones in data storage devices, such as disk drives, based on head performance  
20 variation between different heads in a set of data storage devices.

21  
22 In another embodiment, - According to one embodiment of the present  
23 ~~invention,~~ a population of disk drives is selected, and head performance  
24 measurements are taken for ~~each selected disk media~~ surface locations at  
25 different frequencies. Head pPerformance distributions are obtained from the  
26 head performance measurements data, provide storage formats and a format  
27 optimizer uses the distributions to for the disks by determining obtain a design of  
28 different read/write frequencies for across the disk media surface zones, and  
29 ~~determine head allocation. Once the different frequencies for the zones have~~  
30 ~~been determined, then in each disk drive, the heads in each disk drive are~~  
31 assigned to the ~~predetermined frequencies optimized for.~~ As such, the present

1 ~~invention allows maintaining consistent performance (both sequential and~~  
2 ~~random throughput) across a population of disk drives, and reduced test time.~~

3  
4 ~~\_\_\_\_\_ T—This is accomplished by determining head performance and design of~~  
5 ~~format at development/design time, and assignment of heads to different~~  
6 ~~frequencies at manufacturing time. Therefore, predetermined design of formats~~  
7 ~~is performed off-line, and then marries to a manufacturing test process for~~  
8 ~~assignment of heads to different frequencies.~~

9  
10 ~~\_\_\_\_\_ In one example, the density/format for each recording surface zone and~~  
11 ~~the number of heads allocated to each density, are preselected at design time,~~  
12 ~~and at manufacturing time heads are assigned to higher/lower density formats.~~  
13 ~~Unlike conventional methods, he head allocations and assignments areis per~~  
14 ~~head per zone, taking into consideration head performance variation across the~~  
15 ~~zones. For instanceAs such, if a first head that performs well at the inner~~  
16 ~~diameter (ID) of the disk but poorly at the outer diameter (OD) of the disk, and a~~  
17 ~~second head has reverse performance, then that performance is traded off~~  
18 ~~wherein the first head is assigned a to high BPIdensity at the ID and at low~~  
19 ~~BPIdensity at the OD, and the second head is assigned in the opposite fashion.~~  
20 ~~TIn the per zone variable BPI storage format for improving storage capacity by~~  
21 ~~taking according to the present invention, several manufacturing and customer~~  
22 ~~constraints are taken into consideration. Performance of each head across the~~  
23 ~~stroke of the disk surface, as well as performance variation from one head to~~  
24 ~~another, is determines utilized in designing the storagedensity format and~~  
25 ~~assignments of the head assignmentsss to the density formats.~~

26  
27 In another embodiment, the head performance and the storage format are  
28 determined off-line at development/design time, and then the heads are assigned  
29 to the different frequencies at manufacturing time. For ~~one~~ example, the  
30 storage format for each disk surface zone and the number of heads allocated to

1 each data density are preselected at design time, and then the heads are  
2 assigned to high/low data density storage formats at manufacturing time.  
3

4 ~~\_\_\_\_\_ The present invention provides a variable BPI storage format as a function~~  
5 ~~of storage zones in storage devices, such as disk drives, based on transducer~~  
6 ~~head performance variations between different heads in a set of disk drives.~~

7 ~~\_\_\_\_\_ In another embodiment, a~~The present invention provides a method of  
8 ~~defining the~~such a storage format in multiple data storage devices, with -each  
9 data storage device having a multipleplurality of storage media and a plurality of  
10 corresponding data transducer heads, each transducer head for recording on  
11 and playback of information from a corresponding storage mediamedium in  
12 multiple zones, and wherein each zone includinging a plurality of concentric  
13 tracks for recording on and playback of information. ~~The method includes the~~  
14 ~~steps of: (1) selecting a plurality of a sample of the~~said data storage devices,; (2)  
15 for each selected data storage device, measuring a record/playback performance  
16 ~~capability~~of each head at one or more read/write frequencies per zone,; (3)  
17 ~~based on said performance capability measurements, generating head~~  
18 ~~performancestorage~~density distributions corresponding to at least a number of  
19 ~~the heads in said selected data storage devices~~based on the head performance  
20 measurements,; (4) selecting a group of read/write frequencies for thesaid  
21 ~~multiple~~ data storage devices, two or more frequencies for each zone, based on  
22 thesaid head performancestorage density distributions,; and thereafter, during  
23 manufacturing, (5) assigning one of thesaid read/write frequencies to each head  
24 based on the performance capability of that head ~~per storage device~~.  
25

26 Advantageously, the present invention provides consistent performance  
27 (both sequential and random throughput) across a population of disk drives,  
28 improves storage capacity and yield and reduces test time.  
29  
30

31 **Brief Description of the Drawings**

1        These and other features, aspects and advantages of the present  
2        invention will become understood with reference to the following description,  
3        appended claims and accompanying figures where:

4        FIG. 1A shows ~~an example partial schematic diagram of a disk drive with~~  
5        ~~an example data storage format according to the present invention;~~

6        FIG. 1B shows ~~another example schematic of drive the disk drive of FIG.~~  
7        ~~1A illustrating disk drive electronics for the disk drive;~~

8        FIG. 1C shows ~~a servo tracks and data tracks on a disk n example surface~~  
9        ~~format for data storage according to the present invention;~~

10       FIG. 1D shows ~~an example diagram representing the general zone~~  
11       ~~format layout in of the a disk drive with N disks, and 2N heads, and depicting~~  
12       ~~different heads in a section of a zone on different disk surfaces;~~

13       FIG. 1E shows another example of capacity-zone format layout on a disk  
14       ~~surface a disk;~~

15       FIG. 1F shows ~~example of a series of radial zones on a disk surface that,~~  
16       ~~wherein each zone includes multiple virtual cylinders;~~

17       FIG. 1G shows an example representative data track format layout for the  
18       ~~each of several virtual cylinders in a zone on different disk surfaces with~~  
19       ~~corresponding heads;~~

20       FIG. 1H shows a ~~rather~~ example servo track and data track format layout  
21       for a zone on different disk surfaces with corresponding heads in which, ~~wherein~~  
22       the number of servo tracks and data tracks in different virtual cylinders of a zone  
23       on different disk surfaces are the same;

24       FIG. 1I shows another example layout wherein the servo and data track  
25       format layout that varies from zone to zone on a disk surface;

26       FIG. 2A shows an example function and flow/functional diagram for  
27       ~~embodiment of steps of generating the format layout of FIG. 1I-1A according to~~  
28       ~~the present invention;~~

29       FIG. 2B shows a graph of playback error measurement for a head at a  
30       zone at different recording frequencies;

31       ~~FIG. 2C shows an example joint BPI distribution plot;~~

FIG. 2C shows an example histogram of the frequency capabilities of the heads in a set of disk drives at a zone at a fixed target error rate;

FIG. 2D shows a joint BPI distribution;

FIG. 3 shows an example flowchart of an embodiment of steps of vertical variable zoning data collection process in FIG. 2A;

FIG. 4 shows an example flowchart of an embodiment of steps of vertical zoning post-measurement processing and per zone joint BPI distribution extraction process in FIG. 2A;

FIG. 5 shows an example flowchart of head an embodiment of steps of vertical zone assignments in process of FIG. 2A; and

FIG. 6 shows an example flowchart of an embodiment of steps of format generation and optimization interaction process of in FIG. 2A.

### **Detailed Description of the Invention**

Data storage devices used to store data for computer systems include, for example, hard disk drives, floppy disk drives, tape drives, optical and magneto-optical drives, and compact disk drives. Although the present invention is illustrated by way of an exemplary magnetic hard disk drive 100, the present invention can be used in other data storage devices and other storage media and drives, including non-magnetic storage media, is as apparent to those of ordinary skill in the art and without deviating from the scope of the present invention.

Referring to FIGs. 1A-1C show, an exemplary hard disk drive 100 is diagrammatically depicted for storing user data and/or operating instructions for a host computer system 54. The hard disk drive 100 includes comprises an electro-mechanical head-disk assembly 10 that shown in FIG. 1A as including one or more rotating data storage disks 12 mounted in a stacked, spaced-apart relationship upon a rotating spindle 13. The spindle 13 is rotated by a spindle motor 14 at a predetermined angular velocity.



Each disk 12 ~~includes~~defines at least one diskmedia surface 23, and usually two diskmedia surfaces 23 on opposing sides ~~of each disk 12~~. Each diskmedia surface 23 ~~has associated~~ ~~is coated~~ ~~is coated with~~ magnetic or other media for recording data. The spindle drive-motor 14 ~~rotates~~turns the spindle 13 ~~in order to~~ move the disks 12 past ~~the~~ magnetic transducer heads 16 suspended by ~~the~~ suspension arms 17 over each diskmedia surface 23. Generally, each magnetic-head 16 is attached to ~~the~~ suspension arm 17 by a head gimbal assembly (not shown) that enables ~~the~~ magnetic-head 16 to swivel to conform to ~~the~~ diskmedia surface ~~23s on the disks 12~~. The suspension arms 17 extend radially from a rotary voice coil ~~motor 20~~actuator (not shown). ~~The voice coil An~~ ~~actuator-motor 20~~54 rotates the suspension ~~actuator and head-arms 17~~ and thereby positions the magnetic-heads 16 over the appropriate areas of the diskmedia surfaces 23 in order to ~~locate and read from~~ or write data ~~from or to~~ the diskstorage surfaces 23. - Because the disks 12 rotate at relatively high speed, the magnetic-heads 16 ride over the diskmedia surfaces 23 on a cushion of air (air bearing).

-Each magnetic-head 16 ~~include~~comprises a read element (not shown) for reading magnetic-data ~~from on a disk~~ magnetic storage media surfaces 23 and a write element (not shown) for writing data ~~to a disk~~on the media surfaces 23. Most preferably, ~~the read element is a magneto-resistive or giant magneto-resistive sensor and~~ ~~although not necessarily,~~ the write element is inductive and has an ~~electrical~~ writing width which is wider than an ~~electrical~~ reading width of the read element, ~~which is preferably of magnetoresistive or giant magnetoresistive material.~~

~~E~~Referring to FIG. 1C, each diskmedia surface 23 is divided into a plurality of concentric circular data tracks 30 that each have individually addressable data sector portions 35, ~~such as sectors,~~ in which user data is stored in the form of magnetic bits. The data sectors 35 are separated by narrow embedded ~~narrow-servo sectors or spokes-25~~ arranged in radially extending

1 servo spokes. The servo sectors 25 ~~which~~ include a series of phase-coherent  
 2 digital fields followed by a series of constant frequency servo bursts. The servo  
 3 bursts are radially offset and circumferentially sequential, and are provided in  
 4 sufficient numbers ~~such that~~ fractional amplitude read signals generated ~~picked~~  
 5 ~~up by the head 16~~ read element from portions of at least two servo bursts passing  
 6 under the head 16 ~~read element~~ enable the controller 57 to determine and  
 7 maintain proper ~~head position of the head 16~~ relative to a data track 30. ~~A~~ One  
 8 ~~example of a servo burst pattern for use with a head that includes an inductive~~  
 9 ~~write element a~~ /magneto-resistive read element and an inductive write element  
 10 ~~head 16 is~~ described ~~provided~~ by commonly assigned U.S. Patent No. 5,587,850,  
 11 entitled: "Data Track Pattern Including Embedded Servo Sectors for Magneto-  
 12 Resistive Read/Inductive Write Head Structure for a Disk Drive"; which is  
 13 incorporated herein by reference.

14  
 15 The drive-controller 57 controls ~~operation of the pairs of magnetic heads~~  
 16 ~~16 and media surfaces 23~~ to read from and write data ~~onto the each disk media~~  
 17 surfaces 23. The drive-controller 57 preferably ~~is~~ comprises an application  
 18 specific integrated circuits chip (ASIC) ~~chip~~ which is connected by a printed  
 19 circuit board 50 to ~~with other ASIC chips~~, such as a read/write channel ~~chip 51~~, a  
 20 motors driver ~~chip 53~~, and a cache buffer ~~chip 55~~, ~~into an electronic circuit as~~  
 21 ~~shown in FIG. 1B~~. The controller 57 preferably includes an interface 59 which  
 22 connects to the host computer 54 via a known bus ~~structure 52~~, such as an ATA  
 23 or SCSI bus.

24  
 25 The controller 57 executes embedded or system software  
 26 include ~~comprising~~ programming code that monitors and operates the disk drive  
 27 100 ~~controller system and driver 100~~. During a read or written data retrieval  
 28 operation, the host computer system 54 ~~determines~~ the "address" where the  
 29 data is located ~~in the disk drive 100~~. The address specifies the, i.e., magnetic  
 30 head 16 number, the data track 30, and the data sector ~~relevant portion(s) 35 of~~  
 31 ~~the track 30~~. This data is transferred to the drive-controller 57 which maps the

1 address to the physical location in the disk drive 100, and in response to reading  
 2 the servo information in the servo sectors 25, operates the voice coil actuator  
 3 motor 2054 and ~~suspension arm 17~~ to position ~~thea~~ magnetic head 16 over the  
 4 corresponding data track 30. As the diskmedia surface 23 rotates, the magnetic  
 5 head 16 reads the servo information embedded in each servo sectorspoke 25  
 6 and also reads an address of each data sectorportion 35 in the data track 30.

7  
 8 During a read operation, ~~When the identified data sectorportion 35~~  
 9 appears under the magnetic head 16, the entire contents of the data  
 10 sectorportion 35 containing the desired data ~~is~~are read. In reading data from the  
 11 diskmedia surface 23, the head 16~~read element (not shown)~~ senses a variation  
 12 in an electrical current flowing through a ~~magnetoresistive sensor of the read~~  
 13 ~~element (not shown)~~ when it passes over an area of flux reversals on the disk  
 14 ~~surface 23 of the media~~. The flux reversals are transformed into recovered data  
 15 by the read/write channel ~~chip 51~~ in accordance with a channel algorithm such as  
 16 partial response, maximum likelihood (PRML). The recovered data is then read  
 17 into the cache buffermemory chip 55 ~~of the disk drive 100 from whence~~ it is  
 18 transferred to the host computer system 54. The read/write channel 51 most  
 19 preferably includes a quality monitor ~~function which enables measurement of~~  
 20 the quality of recovered data and ~~thereby provides an indication of the data error~~  
 21 rate. One channel implementation which employs channel error metrics is  
 22 described in commonly assigned U.S. Patent No., 5,521,945 to Knudson,  
 23 entitled: "Reduced Complexity EPR4 Post-Processor for Sampled Data  
 24 Detection" which is, incorporated herein by reference. The present inventioni  
 25 uses the indication of recovered data error to ~~is used in order to select linear~~  
 26 bitdata density, track density and/or error correction code levels, ~~in accordance~~  
 27 ~~with principles of the present invention, as more fully explained hereinbelow.~~

28  
 29 ~~Writing or storing data on the media surface 23 is the reverse of the~~  
 30 ~~process for reading data.~~ During a write operation, the host computer system 54  
 31 remembers the addresses for each file on the diskmedia surface 23 and which

1 ~~data sector~~portions 35 are available for new data. The drive-controller 57  
2 operates the voice coil actuator-motor 2054 in response to the servo information  
3 read back from the ~~embedded-servo sectors 25~~ in order to position the head 16a  
4 ~~magnetic-head~~1, settles the head 16 into a writing position, and waits for the  
5 appropriate data sectorportions 35 to rotate under the head 16 to perform the  
6 ~~actual-writing theef~~ data. To write data on the diskmedia surface 23, an  
7 electrical current is passed through a write coil in the inductive write element (~~not~~  
8 ~~shown~~) of the head 16 to create a magnetic field across a magnetic gap in a pair  
9 of write poles that magnetizes the ~~magnetic-storage-media-coating-the~~ diskmedia  
10 surface 23 under the head 16. When the data track 30 is full, the drive-controller  
11 57 moves the ~~magnetic-head~~ 16 to the next available data track 30 with sufficient  
12 contiguous space for writing of data. If still more track capacity is required,  
13 another head 16 is used to write data to a data sectorportion 35 of another data  
14 track 30 on another diskmedia surface 23.

15  
16 ~~In one aspect,~~ the present invention increases the data-storage capacity  
17 and yield of data storage devices, such as the disk drive 100, -having a plurality  
18 of magnetic media surfaces, such as the disk surfaces 23, ~~such as hard-disk~~  
19 ~~drive 100 including disks 12 covered with magnetic media.~~

#### 20 21 ~~V~~Overview of general method-vertical Zzoning

22 In every disk drive, there is a distribution associated with the head and  
23 disk surface /media-pair performance ~~in that disk drive~~. -The present invention  
24 takes advantage of that distribution to determine different linear bit density (BPI)  
25 recording frequency assignments for the heads, and optionally track allocation.

26  
27 ~~A~~ According to one embodiment of the present invention, a set of disk  
28 drives is selected, and head performance measurements are taken for each  
29 selected diskmedia surface location in the disk drives at different frequencies.

——— Empirical frequency capability histograms are extracted at a given known target performance metric from the measurement data. Head performance distributions ~~Probability cumulative distribution functions~~ (such as joint BPI probability distributions) are estimated from the histograms and fed into a format optimizer to obtain and design (vertically zoned) frequency format profiles (~~i.e., across the stroke and the disk media surface zones~~) as well as the optimal number of head allocations to the frequencies. Once the frequency format profiles and the optimal number of head allocations are designed and pre-determined, during a test process, every head at every zone is assigned to one of the ~~multiple pre-determined frequencies~~ based on the head's performance capability.

——— ~~As such, the present invention allows maintaining consistent performance (sequential/random throughput) across several of disk drives, without introducing significant additional test time. This is accomplished by determining head performance and design of format at development/design time, and assignment of heads to different frequencies at manufacturing time. Therefore, the predetermined design of frequency format profiles and (optimal) number of head allocations are performed off-line while the assignment of heads to different frequencies is performed during the test process such as during manufacturing.~~

——— ~~Unlike conventional methods, in the present invention head allocation and assignment is per head per zone, taking into consideration head performance variation across zones (i.e. across the stroke). As such, during head frequency assignment, if a first head performs well at ID but poorly at OD, and a second head has the opposite performance, the performance variation between the heads is traded off such that the first head is assigned to high density (frequency) at ID and at low density at OD, and the second head is assigned to low density at ID and high density at OD. In a method of per zone variable bits per inch (BPI or linear density) for improving capacity according to the present invention, several manufacturing and customer constraints are taken into consideration. And,~~

performance of each head across the stroke, as well performance variation from one head to another, is utilized in designing the density format and assignments of heads to the density formats.

Referring back to FIG. 1A shows, a storage format for the disk drive 100. Each disk surface 23 includes zones 60 that extend from one radius of the disk 12 to another radius of the disk 12, and the format of the zones 60 on each disk surface 23 is the same. Then example of density layout according to an embodiment of the present invention is shown. In one aspect, the present invention provides a variable BPI storage format is layout as a function of the zones 60 on each disk surface 23 based on e.g. two data recording formats -- (i.e., low high data density and high low data density --) that utilize: (1) head performance variation from one head 16 to the next head 16 in the disk drive 100, and (2) the performance (variation) of a given head 16 across the stroke of a disk surface 23. Further, the present invention provides a method of generating said layout.

In this example, each zone comprises a group of tracks laid out in zones 60 between one radius and another radius on the disk surface 23, wherein the zone layout for the multiple disk surfaces in each disk drive 100 are the same.

The disk drive 100 includes the N-disks 12 depicted as (d)Disks 1 to N, the heads 16 depicted as heads 1 to 2N, and the disk surfaces 23 depicted as disk surfaces 1 to 2N. E), each disk 12 includes having two opposing disk surfaces 23, and each head 16 is associated with one of the disk surfaces 23a Surface1 and opposing Surface. For instance, head 1 is associated with disk surface 1 of disk 1, head 2 is associated with disk surface 2 of disk 1, head 3 is associated with disk surface 3 of disk 2, and head 2N is associated with disk surface 2N of disk N.

~~E2, wherein each disk surface 23 includes the zones 60 depicted as has~~  
~~M-zones (zZones\_1 through ZoneM) across its the actuator stroke, with, and~~  
~~one head per disk surface. For each disk surface, zZone\_1 is at the in-ID and z,~~  
~~Zone\_M is at the in-OD. T, wherein the radial boundaries onf zZone\_1 of disk~~  
~~sSurface\_1 of dDisk\_1 are the same as the radial boundaries of zZone\_1 onf disk~~  
~~sSurface\_2 of dDisk\_1, and so on. Similarly, the radial boundaries of zZone\_M on~~  
~~disk sSurface\_1 of dDisk\_1 are the same as the radial boundaries of zZone\_M on~~  
~~disk sSurface\_2 of dDisk 1, and so on. However, different zones 60 across the~~  
~~stroke on each disk surface 23 need not necessarily have the same number of~~  
~~data tracks 30 or TPI (e.g., Zone1 and ZoneM on the same surface do not~~  
~~necessarily have the same number of tracks). For example, zZone\_1 on disk~~  
~~sSurface\_1 of dDisk\_1 (i.e., Head1) has the same number of data tracks 30 and~~  
~~the same radialphysical-zone boundaries as zZone\_1 on disk sSurface\_1 of dDisk~~  
~~N-(Head 2xN), etc. aAnd, zZone\_M on disk sSurface\_1 of dDisk\_1 -(Head1) has~~  
~~the same number of data tracks 30 and the same radialphysical-zone~~  
~~boundariesy as zZone\_M on disk sSurface\_1 of dDisk\_N-(Head2N). However, the~~  
~~number of data tracks 30 in zZones\_1 and ZoneM can be different.~~

~~Each disk surface 23 also includes virtual cylinders 39 depicted as virtual~~  
~~cylinders 1 to n. Each zone 60 includes multiple virtual cylinders 39, and each~~  
~~virtual cylinder 39 includes multiple data tracks 30 on each disk surface 23. The~~  
~~physical-zone boundaries vertically align on the disks in each disk drive, forming~~  
~~virtual cylinders 39 (VC). In this example, there are n virtual cylinders 39, VC1~~  
~~through VCn. Further, wWithin a virtual cylinder 39, different heads 16 may read~~  
~~and /write at different frequencies (e.g., variable BPI) to provide, hence the~~  
~~concept of vertical zoning.~~

~~The level of track density (TPI) can be one of fixed number of preselected~~  
~~levels or can be derived from an algorithm that is based on the location of a~~  
~~portion 35 of the media surface 23. Embedded servo sectors 25 are initially~~  
~~written on a media surface 23 during a factory servo-writing process at a servo~~

track density that can be higher than the data track density, as illustrated in FIG. 1C. Servo bursts within each servo sector 25 are provided in such number and placement to enable accurate positioning of the magnetic head 16 in a full range of positions across the media surface 23, given the particular effective width and characteristics of the read element of a particular head (the read element width typically being narrower than the writer carry out the head positioning method, information in the embedded servo sector 25 is read by the magnetic head 16 and passed to the drive controller 57 which directs the actuator motor 20 to readjust the position the suspension arm 16. In the example shown in FIG. 1C shows, the data tracks 30 and the servo tracks 37 on the disk surface 23. The data tracks 30 include the data sectors 35, and the servo tracks 37 include the servo sectors 25. the servo track density is about 150% of the maximum possible data track density. In FIG. 1c five servo tracks 37 depicted as servo tracks (e.g., Sa, Sb, Sc, Sd and Se) are shown in relation to three data tracks 30 depicted as data tracks Tk1, Tk2 and Tk3.

The servo tracks 37 are written on the disk surface 23 during manufacturing at a servo track density that is about 150% of the maximum data track density. -The sServo track density is determined by determining the maximum- read width and the minimum- write width of a population of themagnetic heads 16. After writing the servo tracks 37wedges 25 at the servo track pitch, the actual data tracks 30 can be written at any disk-radial position between the servo tracks 37. The data track density (TPI) can be selected from predetermined levels or can be based on the location of a data sector 35. Additional tests, can be performed to determine the optimum data track density of the diskmedia surface 23. Each servo track 37 comprises radially similarly situated servo information in servo sectorwedges 25 in the servo spokes. For example, (e.g., the set of servo trackinformation Se contains servo sectors 25 at essentially the same radial distance from the disk-center of the disk 12, the servo track Sd contains servo sectors 25 at essentially the same radial distance from the center of the disk 12, form a servo track circumferentially, set of servo



1 ~~information. See at essentially same radial distance from the disk center form~~  
2 ~~another servo track circumferentially, etc.)~~

3  
4 FIGs. 1D to 1I show vertical zone formats in which different heads 16 on  
5 different disk surfaces 23 may read/write at different linear frequencies (variable  
6 BPI) on the data tracks 30 within a virtual cylinder 39.

7  
8 ~~FIG. 1D shows an example diagram representing the general zone 60~~  
9 ~~format layout of the a-disk drive 100, with N disks 12, and 2N heads 16, and~~  
10 ~~depicting different heads 16 in a section zZone 1 on different disks 12.~~ FIG. 1E  
11 ~~shows another example of capacity-zone 60 format layout on the disk surface 23a~~  
12 ~~surface a disk.~~ FIG. 1F shows each example of a series of radial zones 60 on  
13 the disk surface 23, Zone1 through ZoneM, on a disk surface, wherein each  
14 zone includes multiple virtual cylinders 39. Zone 1 includes virtual cylinders 1 to  
15 i, and zone M includes virtual cylinders 1 to i. The radial boundaries of the zones  
16 60 are shown as dark circles, and the radial boundaries of the virtual cylinders 39  
17 are shown as light circles. FIG. 1G shows ~~an example representative data track~~  
18 30 format layout for the each of several virtual cylinders 39 in a zone 60 (e.g.,  
19 Zone1), on different disk surfaces 23 with corresponding heads 16. FIG. 1H  
20 ~~shows a data track 30 and another example servo track 37 format and data track~~  
21 ~~35 layout for a zone 60 on different disk surfaces 23 with corresponding heads~~  
22 16 in which, wherein the number of data tracks 30 and servo tracks 37 and data  
23 tracks in different virtual cylinders 39 of a zone 60 (e.g., Zone1) on different disk  
24 surfaces 23 is are the same. And, FIG. 1I shows a data track 30 and servo track  
25 37 format for zones 60 on the disk surface 23 with a corresponding head 16 in  
26 which another example layout wherein the servo and the data track 30 and servo  
27 track 37 format layout varies from zone zone 1 to zone M60 on a disk surface 23.  
28 ~~In all of the above examples of vertical zoning layout according to the present~~  
29 ~~invention, within a virtual cylinder 39, different heads on different surfaces may~~  
30 ~~read/write at different linear frequencies on the data tracks (e.g., variable BPI).~~

## Overview of Format Optimization

~~The In one embodiment, a vertical zoning method according to the present invention includes designing, optimizing and (selecting) for two or more recording frequency profiles (i.e., per zone) for a sample number of disk drives (e.g., performed off-line during the disk drive development/design phase). Then, for a population of disk drives, in each disk drive, each head is assigned to one of the predetermined frequencies for a given zone (e.g., during the disk drive manufacturing phase). A~~ The assignment step includes assigning a predetermined read/write frequency (BPI) is assigned to each head based on a known number of head allocations and the head's performance capability. A head assigned to a higher frequency/density (HD) records more bits on a track, and a head assigned to a lower frequency/density (LD) records less bits on a track.

Performance testing of the head and disk surface pairs occurs after full read/write and servo calibration and optimization of the disk drive. Referring to the example in FIG. 1A, if the tested performance of hHead\_1 at zZone\_1 on disk sSurface\_1 of dDisk\_1 at a given frequency (after full drive read/write and servo calibration/optimization) is better than a desired target performance metric, then that (strong) head, hHead\_1, is considered strong since it is capable of to have some margin for storing more information than it was originally accounted for. Thus, the designed recording frequency can be increased at zZone\_1 on disk sSurface\_1 of dDisk\_1 for hHead\_1 yet so as to ensure the its performance does not fall below the desired target performance metric. If the tested performance of hHead\_2 at zZone\_1 on disk sSurface\_2 of dDisk\_1 at the same frequency (after full drive read/write and servo calibration/optimization), is worse than a desired target performance metric, then that (weak) head, Hhead\_2 is considered weak, but can be compensated for by relaxing the frequency at which hHead\_2 operates, so as to ensure the target performance metric is met. Performing the above trade-off between the heads for all the zones, without loss of overall capacity, provides resulting frequency profiles (i.e., across the stroke) that are

1 ~~comprising~~ vertically zoned frequency format profiles without loss of overall  
2 storage capacity.

3  
4 ~~Advantageously, As the above example shows,~~ by compensating for  
5 ~~hweak~~ Head\_2, rather than failing the disk drive due to the weak H~~head~~\_2, the  
6 vertical zoning improves the disk drive yield. ~~Without application of vertical~~  
7 ~~zoning such a disk drive would not have passed the test limits, and hence would~~  
8 ~~have failed.~~ Furthermore, the format optimizer uses the head estimates of  
9 performance (i.e., read/write frequency capability) ~~cumulative distributions~~  
10 ~~function~~ at every zone and a target performance metric, to design a group of  
11 read/write frequency format profiles for strong and weak ~~and strong~~ heads within  
12 a given disk drive. The format optimizer also determines the optimal number of,  
13 ~~for example,~~ strong versus weak versus strong heads.

14  
15 The format optimizer does not determine which specific head is ~~actually~~ at  
16 the high or lower ~~or higher~~ frequency, but does only provides a breakdown of the  
17 number of heads at the high~~lower~~ frequency and the number of heads at the  
18 low~~higher~~ frequency. ~~The~~at breakdown is fixed, performed off-line, and ~~is~~ used  
19 during the head assignment ~~process~~. Then, in the head assignment ~~process~~  
20 ~~(e.g., during a manufacturing test process)~~, out of  $2 \times N$  heads in a disk drive with  
21  $N$  disks, the number of heads ~~that have to be~~ assigned to each predetermined  
22 frequency/~~format~~ is also predetermined ~~(e.g., number heads to assign to low~~  
23 ~~frequency and number of heads to assign to high frequency)~~.

24  
25 ~~As such,~~ the heads within a set of disk drives are allocated to the  
26 predetermined group of read/write frequencies as part of the optimization  
27 process to meet the storage capacity and yield requirements for the disk drives.  
28 The allocation process allocates a number of the heads in a disk drive to ~~one of~~  
29 the predetermined/~~designed~~ frequencies, however the specific assignment of a  
30 particular head to a particular frequency is performed later during ~~as part of the~~  
31 assignment process thereafter. ~~For~~ In one example, in a two2 read/write

frequency design (high frequency density and low frequency density) for a set of disk drives- each with eight8 heads, in each disk drive for zZone\_1 on all the disk surfaces, any five3 heads of the eight8 heads are allocated to the highlower frequency and any three5 heads of the eight8 heads are allocated to the lowhigher frequency in the allocation process based on the performance measurements of all the heads in the set- of the disk drives. Thereafter, the specific assignment of each particular head to a particular predetermined frequency is performed as part of the assignment process. For example,- in a first disk drive heads 1, 3, 4 are assigned to the low frequency, and heads 2, 5, 6, 7, 8 are assigned to the high frequency and heads 1, 3, 4 are assigned to the low frequency, whereas in a second disk drive heads 2, 3, 8 are assigned to the low frequency, and heads 1, 4, 5, 6, 7 are assigned to the high frequency and heads 2, 3, 8 are assigned to the low frequency. T, and so on, wherein the specific head assignments depend on the specific capability of the heads in each disk drive.

The optimal number of heads per frequency (i.e., head allocation) is determined at the same time that the group of read/write frequencies are designed/selected by the format optimizer, by solving a joint constrained optimization problem. For example, in a the 8 head disk drive with eight8 heads and with above, for the case of two frequencies a (high frequency (freq1)) and a low frequency (freq2)) that are each a different ratio of a reference frequency at a ratio to a frequency freq, in each vertical zone, allocating two2 heads to the high frequency1 and six6 heads to the low frequency2, provides a specific first storage disk drive capacity. Changing the said frequency ratio of the frequencies and the number of heads allocated to each frequency, provides a different storage capacity for that disk drive. Thus, As such, the disk drive storage capacity is a function of the number of heads multiplied by the frequency allocated to each head per zone. —For example, if a nominal disk surface data storage level capacity is 1 unit, and if the high frequency 1 =  $4/3 \times$  the reference frequency and the low frequency 2 =  $2/3 \times$  the reference frequency, then one

1 head can be at the high frequency<sup>4</sup> for every one head at the low frequency<sup>2</sup>, to  
2 maintain ~~whereby~~ the average disk surface data storage capacity ~~at~~<sup>is</sup> 1 unit.

3  
4 The head performance distributions represent percentages of the heads in  
5 the disk drives than can operate at different frequencies. For example, the head  
6 performance distribution is a BPI distribution that represents the head frequency  
7 capability at a target performance metric. –Using the head performance  
8 distributions (~~i.e., the~~ head read/write frequency capability distributions at the  
9 target performance metric for every zone), the number of heads, the format of the  
10 virtual cylinders, and ~~thea~~ desired storage capacity, the format optimizer  
11 determines the frequency for each virtual cylinder in each zone ~~in each virtual~~  
12 ~~cylinder~~ and the number of heads in each disk drive allocated to each frequency;  
13 ~~in order to achieve thea~~ desired storage capacity. Thereafter, in the assignment  
14 process (~~e.g., as part of a testing of each disk drive~~), each ~~specific~~ head in a  
15 population of disk drives is assigned to one of the predetermined frequencies  
16 based on the allocation criteria and the specific head performance. For an  
17 example, in a 4-head disk drive with four<sup>4</sup> heads, the format optimizer considers  
18 three<sup>3</sup> heads at the high frequency<sup>4</sup> and one<sup>1</sup> head at the low frequency<sup>2</sup>, then  
19 two<sup>2</sup> heads at the high frequency<sup>4</sup> and two<sup>2</sup> heads at the low frequency<sup>2</sup>, and  
20 then one<sup>1</sup> head at the high frequency<sup>4</sup> and three<sup>3</sup> heads at the low frequency<sup>2</sup>.  
21 Thus, And in each case, the format optimizer ~~usings~~ the ~~estimated~~ head  
22 ~~performance cumulative-distribution-functions to~~ determines the disk drive yield.  
23 ~~The head performance distributions (e.g., BPI distributions) represent~~  
24 ~~percentages of the heads in the disk drives than can operate at different~~  
25 ~~frequency densities. This allows the format optimizer to determine the storage~~  
26 capacity and yield and capacity. ~~In the description of the example embodiment~~  
27 ~~herein, head performance distribution, such as a BPI distribution, represents~~  
28 ~~head frequency capability (probability) cumulative distribution at a target~~  
29 ~~performance metric.~~

In one version of the optimization process, ~~the disk drive yield~~ is maximized while meeting a constraint on storage capacity. In another version, the storage capacity is maximized while meeting a constraint on ~~disk drive yield~~. In the former case, the format optimizer uses a format where the maximum number of disk drives qualify and the fewest number of disk drives fail to reach the required storage capacity ~~higher frequency is freq1 and the lower frequency is freq2. For In the example, in a 4-head disk drive with four4 heads and a nominal disk surface data storage capacity of 1 unit, allocating two2 heads to the high frequency4 and two2 heads to the low frequency2, provides a nominal data surface capacity of 1 unit, and storage capacity of 4 units for the disk drive. In the later case, the format optimizer uses a format where the maximum number of disk drives reach the required storage capacity and the fewest number of disk drives fail to qualify. For example, in a disk drive with four4 heads and a nominal disk surface data storage capacity of 1 unit, allocating three3 heads are allocated to the high higher frequency4 and one1 head to the low the lower frequency frequency2 provides, a higher data storage capacity of (i.e. 4.66 and 2/3) units is achieved for the disk drive. In that case, the format optimizer lowers the zone recording frequencies to meet that constraint of capacity of 1 unit per surface. As such, for 2 heads at freq1 and 2 heads at freq2, the format optimizer manipulates the difference of those frequencies such that surface capacity always reaches 1 unit, but maximizes yield whereby a maximum number of disk drives qualify and fewest number of disk drives fail to reach required capacity.~~

Thus, ~~As such, according to one embodiment of the present invention, a the vertical zoning approach for variable BPI design includes use of an off-line predetermined per zone format design of formats based on disk drive data collection and head performance (joint) BPI distribution extraction methods. In one version, a fixed predetermined zone boundary format layout is used to design multiple frequency BPI formats based on representative or actual joint BPI distributions at one or more desired target performance metrics (such as off-track~~

1 symbol error rate) and, wherein the joint BPI distributions are extracted from a  
2 finite pre-selected set of disk drives.

3  
4 The collected data is used to extract ~~thesaid~~ joint BPI distributions for the  
5 heads at every {pre-selected} zone, and the per zone design of low/high and low  
6 data density formats for the heads is performed off-line. The format optimizer  
7 solves a constrained joint optimization-~~process~~ off-line to obtain ~~thesaid~~ format  
8 designs, using well-known constrained optimization routines. Using joint BPI  
9 distributions allows consideration of potential correlation of BPI capability of the  
10 heads across the stroke as well as the individual contribution of each head to the  
11 storage overall drive capacity (or areal density) and yield.

12  
13 The off-line format design ~~of formats~~ allows the format optimizer to  
14 ~~consideration of other potential constraints that may arise, as additional~~  
15 ~~constraints within the optimizer, and hence solved by the optimizer.~~ For  
16 example, as more information is obtained in quantifying the thermal stability  
17 constraints of the disks recording media (which in turn places an upper bound  
18 on linear bit density for the heads) the off-line format design does provides the  
19 ability of not exceeding theese constrainlimits. Likewise, if there are data rate  
20 constraintlimitations in either the write process capability or the ASICs  
21 component capability, such constraints may be cast within the joint constrained  
22 format optimizer to ensure thesaid constrainlimits are not exceeded.

#### 23 24 Data Overview of Measurement Process

25 ~~A~~In one implementation of the method of the present invention, a  
26 measurement procedure is used to collect data, from which ~~such that after~~  
27 ~~processing of the collected data,~~ one-dimensional (1-D), two-dimensional (2-D)  
28 and as well as three-dimensional (3-D) joint BPI (probability) distributions at a  
29 desired read/write target error rate (or any other ~~choice of metric~~) can be  
30 extracted. -Data is collected based on head capability measurements taken at  
31 different radial positions on the disk. ~~The collected data is used to extract 1-D,~~

~~2-D and 3-D empirical distributions at a target choice of performance metric. The dimensions are dimensions of the distributions, and the distributions represent the capability of each head at different radial positions. For example, several disk drives which collectively include 1000 heads are selected for measurement, and, in a measurement process, record/playback error rate measurements of the 1000 heads from zZone\_1 to zZone\_24 of the disk surfaces at different frequencies are obtained. Thereafter, in post-measurement data processing: (a) the BPI capability of eachvery head at a fixed target performance metric at e.g. zZone\_1 is determined in order to obtain a 1-D BPI distribution, (b) the BPI capability of eachthe head at a fixed target performance metric at e.g. zZones\_1 and zZone\_5 is determined in order to obtain a 2-D BPI joint distribution, and (c) the BPI capability of eachthe head at a fixed target performance metric at e.g. zZones\_1, zZone\_5 and zZone\_20 is determined in order to obtain a 3-D BPI joint distribution.~~

The BPI distributions are then ~~passed~~used as input to the format optimizer to solve three constrained optimization problems to provide head frequency per zone allocations. The three constrained optimization problems, wherein: (1) one ~~problem-maximizes the disk drive yield while preserving the same storage drive capacity,~~ (2) ~~another-maximizes the storage disk drive capacity while preserving the same drive yield and,~~ and (3) ~~another-maximizes the disk drive yield while ensuring a desired target storage drive capacity is met at a fixed target track-per-inch (TPI).~~ Additionally, customer related or application specific integrated circuit (ASIC) data rate (limitation) constraints are also considerutilized. -The format optimizer ~~can~~ is capable of solving any one of these above-mentioned three problems, and ~~wherein~~ one problem can take priority over another depending on the process phase. For example, at an earlier development phase of a program where the disk drive components are not matured yet, meeting the storage drive capacity may be a challenge. In that phasecase, the format optimizer can be used to design the variable BPI format profiles by solving the second problem above. Then, aAs the disk drive components mature, and



1 ~~such that~~ meeting the storage drive capacity becomes easier and meeting the  
 2 ~~drive-yield~~ becomes more important, the first problem may be solved ~~considered~~  
 3 ~~instead.~~ Thereafter, as part of a test process, an assignment algorithm ~~is used to~~  
 4 ensures the appropriate head assignments to the predetermined high and low  
 5 data density (~~pre-specified~~) formats per head and per zone or across the head  
 6 strokes, based on the head allocation breakdown of the format optimizer.

7  
 8       The yDisk drive-yield is improved while meeting the desired-target storage  
 9 drive-capacity by allowing a frequency format layout with (~~e.g.,~~ high and low  
 10 frequencies and y) ~~with~~ a predetermined number of high and low performing  
 11 head allocations. Utilizing realistic constraints such as ASIC data rate  
 12 limitations, the same fixed target TPI is maintained by increasing the average  
 13 target BPI across the ~~head-stroke on a disk surface~~ to achieve the target ~~desired~~  
 14 ~~disk-drive data-storage~~ capacity. As such, head performance variation from one  
 15 head to the next head in the disk drive (~~and for across the head stroke across the~~  
 16 stroke of the disk surface) is utilized to ~~allow-increasing~~ the storage capacity  
 17 ~~areal density of the stored information while preserving the same overall disk~~  
 18 drive-yield. ~~For In one example, the~~ a vertical zoning format layout use method  
 19 ~~according to the present invention~~ utilizes several design constraints to improve  
 20 the drive-yield using a variable high and low/high BPI design with a fixed  
 21 predetermined number of head allocations as a function of the zones while  
 22 meeting the target storage capacity at a fixed target TPI. The hHead  
 23 performance variation or correlation across the stroke is also utilized.

24  
 25       Further, ~~the method of present invention takes into consideration the~~  
 26 difference in data storage ~~storage capacity~~ of two or more zones on a disk  
 27 surface is considered, as it affects storage ~~overall disk-drive~~ capacity. The  
 28 storage ~~disk-drive~~ capacity is defined as a weighted combination of the zone  
 29 capacities across the stroke on each disk surface in the disk drive. A correlation  
 30 in the head performance statistics is extracted from one head to another head,

1 and for every given head considered in a set of disks drives across the head  
2 stroke on each disk surface.

3  
4 The joint constrained optimization process determines a per zone target  
5 high and low low/high data density format/layout. The optimization process takes  
6 into account constraints including customer related requirements such as the  
7 ~~requirement of a minimum logical block count (LBA)~~, monotonic data rate, and  
8 maximum data rate requirements at the outer zone areas which can be  
9 formulated into (additional) constraints. ~~Head allocation and assignment~~  
10 ~~according to the present invention improves manufacturing yield and provides a~~  
11 ~~disk drive with minimal performance degradation (i.e., sequential or random~~  
12 ~~throughput as well as test process time).~~

#### 13 14 Example Implementation

15 FIG. 2A shows an example function and flow diagram of an example  
16 ~~implementation of the above described method according to the present~~  
17 ~~invention for generating the optimal data density format/layout shown by example~~  
18 ~~in FIG. 1A. -The function and flow diagram example method in FIG. 2A includes:~~  
19 ~~a data collection/measurement process (block) 62, a post-measurement data~~  
20 ~~post-measurement processor (block) 64, a format optimizer process (block) 66~~  
21 ~~and a format generator process and head assignment process (block) 68;~~  
22 ~~example embodiments of which are described below.~~

#### 23 24 Data Collection/Measurement process

25 The data measurer 62 takes data measurements for every zone at a finite  
26 number of frequency samples.

27  
28 ~~In one embodiment, the data measurement block 62 implements a~~  
29 ~~measurement procedure that includes the steps of:~~

30 (1). ~~\_\_\_ Creating several different predetermined linear bit density format~~  
31 ~~profiles include comprising a profile of different frequencies per zone across the~~

1 ~~actuator~~ stroke, such as ~~e.g.~~ a first profile including high frequency ~~freq1~~1 for  
2 zZone\_1, high frequency ~~freq1~~2 for ~~zto~~ Zone 2, . . . , high frequency 4M for  
3 zZone\_M; and a second profile including low frequency2\_1 for zZone\_1, low  
4 frequency2\_2 for zZone 2, . . . , low frequency2\_M for zZone\_M, ~~etc.~~, to be loaded  
5 on a representative number of disk drives selected for the measurement process  
6 (or if possible on all of the available disk ~~built~~ drives for that build);

7 (2) ~~\_\_\_~~ Loading a frequency format profile;

8 (3) ~~\_\_\_~~ Performing read/write and servo optimization and calibration;

9 (4) ~~\_\_\_~~ Taking head performance measurements including ~~e.g.~~ (off-track)  
10 mean square error (~~MSE~~) or quality metric (~~QM~~) and/or symbol error rate (~~SER~~)  
11 ~~measurements~~ at pre-selected frequencies for preferably all available zones, and  
12 ~~saving~~ the data; and

13 (5) ~~\_\_\_~~ Repeating steps 2-4 above for all the remaining frequency format  
14 profiles.

15  
16 The above steps are performed for the selected disk drives in the  
17 measurement process.

18  
19 Thus, in the disk drive 100, As such density is selected and the data is  
20 recorded on a data sector 35 ~~portion of the diskmedia surface 23 at the selected~~  
21 data density by positioning the ~~a magnetic head 16 abutting the data sector~~  
22 ~~portion 35 of the diskmedia surface 23, and sending the appropriate write signals~~  
23 ~~to the write element (not shown) of the magnetic head 16. Typically, a sample of~~  
24 data is recorded on the disk surface 23 ~~such that a significant number of errors~~  
25 are detected (such as e.g., ten 10 errors per error rate measurement), is  
26 ~~recorded on the diskmedia surface 23 to obtain a statistically representative~~  
27 sampling of the error rate for the data sector portion 35 of the diskmedia surface  
28 23. Thereafter, the recorded data is read by the read element (not shown) of the  
29 ~~magnetic head 16, and the data read is stored by the host computer system 54~~  
30 for evaluation. An error rate of the recorded data is measured or compiled by  
31 comparing the actual-written data with the read data, element-by-element. The

~~Suitable methods of determining the error rate can be determined using a include~~  
~~actual-bit error measurement in which a bit of data read from the diskmedia~~  
~~surface 23 is compared with the correct bit, or bit stream measurement in which~~  
~~a bit stream of data read from the disk surface 23 a correct bit stream in is~~  
~~compared with a correct bit stream, or a measured bit stream.~~ An alternative  
~~method uses the mean square error metric measurement method in which a~~  
~~waveform read from the diskmedia surface 23 is compared with an ideal~~  
~~waveform to provide an error signal that is squared and summed to form the~~  
~~error metric.~~

In this description, a component distribution is defined ~~as to be a~~ (random)  
variation (i.e., tolerance) of a pre-specified (target) nominal component  
parameter such as a head write/read width, and ~~a the term~~ distribution is defined  
as ~~at the~~ probability distribution function (PDF). During ~~the~~ early product  
development process, when the head performance distributions are wide and  
unreliable, data from a matured set of disk drives is used for extracting reference  
(joint) BPI distributions at a target performance metric such as on-track symbol  
error rate, off-track symbol error rate, on-track mean square error (e.g., off/on  
track error rate or off-track mean square error). Later in the process, when the  
~~amount of~~ head performance variations from one phase to the next in the  
distribution is expected to be minimal, new sets of measurement data are  
collected using a selected plurality/population of disk drives at their more  
matured stages.

Thus, a number of BPI formats including the nominal target format are  
selected. Then, on-track or off- or on-track symbol error rate or mean square  
error MSE-measurements are taken at different pre-selected locations of the disk  
surfaces, such as the e.g., outer, middle and inner zones. The performance  
measurements can be limited to ~~are taken (in one example scenario described~~  
~~further below, the choice is limited to thesesaid three zones, to reduce the~~  
measurement time for performing measurement). However, preferably the

performance measurements over multiple zones ~~can be performed~~ and other measurements such as off-track measurements ~~(e.g., 747 measurements)~~ can ~~be performed~~ also be taken. The nominal formats are generated from the data.

Two or more different linear bit density format profiles can be loaded at a time. In one example, two variable BPI format per zone design (~~low/high and low~~ data density format profiles) can be created for ~~the purpose of measurement data~~ collection during every build. In this way, more statistical data can be collected from more disk drives, however, there will be only two frequency samples per zone available for ~~data~~ post-measurement data processing.

#### Raw Data post-Mmeasurement Data P-processor

~~In the above steps, measurements (e.g. either MSE or SER) for every zone are taken at a finite number of frequency samples. In post-measurement data processor processing (post-processing) block 64, using the available performance metric, measurements are used to calculate each head's frequency performance, for instance as (e.g., kilo flux per inch (kFCI) or kilo bits per inch (kBPI),) at a given target performance metric. The performance of every head at every zone is determined as a function of the said read/write frequency profiles used for the measurements.~~

For example, if six different frequency profiles are used, then for every head per zone, the data measurement process 62 provides measured data as a function of six frequency samples at a target performance metric. In the post-measurement data processor 64, all the measured data is sorted and the performance of every head at every zone at the six different frequency samples is extracted to generate frequency capability histograms at a target performance metric ~~(e.g. error rate).~~

~~Referring to FIG. 2B~~ shows a graph of playback error measurement for a head at a zone at different recording frequencies. The curve shows head

performance as a function of frequency (BPI). ~~T, the samples can be depicted in a two dimensional graph wherein the x-axis (horizontal) is the read/write frequency in (e.g., frequencies 1 through 6, kBPI at the outer diameter-OD), and the y-axis (vertical) is the on-track symbol error rate measurement in a log scale for Head1 at zone 1 for each of the said 6 frequencies.  $E(\log \text{SER})$  (in FIG. 2B, each frequency sample data sample 70 is depicted as a "+", each curve fit point 72 is depicted as "o" and each projected frequency 74 is depicted as "◇").~~

In the illustration, head 1 at zone 1 in disk drive 3 is measured at six frequency samples. The curve is generated using a least square polynomial fit to the six frequency samples. The projected frequency (BPI) for a target on-track symbol error rate is extracted from the curve by interpolation or extrapolation. For example, if the target on-track symbol error rate is  $10^{-8}$  then the projected frequency is determined by interpolation, whereas if the target on-track symbol error rate is  $10^{-6}$  then the projected frequency is determined by extrapolation. The on-track symbol error rate varies measurement can vary e.g. from  $1e^{-4}$  (i.e.,  $1 \times 10^{-4}$ ) to  $1e^{-7}$  (i.e.,  $1 \times 10^{-7}$ ) as a function of the 6 frequencies, and wherein the error rate increases as the read/write frequency (density) increases.

The nominal kBPI (before vertical zoning) and the kBPI gain relative to the nominal kBPI are also shown. Head 1 can be classified as a strong head because there is reasonably significant margin before its on-track symbol error rate of  $-9.1$  (log) at a nominal frequency/kBPI of  $\sim 188$  can be changed to a projected on-track symbol error rate of  $-6.22$  at a frequency/kBPI of  $\sim 217$ . Hence, there is a total kBPI gain of  $\sim 29$ , allowing the nominal frequency to increase by 15% while meeting the target on-track symbol error rate performance metric of  $6 \times 10^{-7}$ . Thus, head 1 of disk drive 3 has a frequency capability of about 217 at the target on-track symbol error rate of  $6 \times 10^{-7}$ , which provides a sample for the generation of a histogram.

FIG. 2C shows a histogram of the frequency capabilities of the heads in a set of disk drives at a zone at a target performance metric. The histogram 76 is constructed using the projected frequencies determined in FIG. 2B for the heads in the selected disk drives reading from zone 1 at the target on-track symbol error rate of  $6 \times 10^{-7}$ . The x-axis is the projected frequency capability at the outer diameter, and the y-axis is the number of heads. The histogram is extracted and empirical, has a normal distribution fit and has a width that corresponds to the head performance variation.

Additional histograms — To determine frequency capability of e.g. Head1 at Zone1 at a target error rate of  $1e^{-6}$  (i.e.,  $1 \times 10^{-6}$ ), a curve is fit (e.g., using known curve fitting techniques such as least squares polynomial fit) to the 6 samples, to determine by interpolation the frequency value that gives rise to that target error rate (in FIG. 2B, each curve fit point 72 is depicted by a "o"). If the target error rate is at  $1e^{-8}$  (i.e.,  $1 \times 10^{-8}$ ) then the frequency value that gives rise to that target error rate is determined by extrapolation (in FIG. 2b, the projected or extrapolated frequency value 74 is shown as a diamond shape). The process for that target error rate is performed for Zone1 for all the heads in the selected disk drives used in the measurement process 62, to create a histogram (FIG. 2D) of the frequency capabilities of all the heads in the disk drives at Zone1 at that fixed target error rate. are constructed The process is the same for all the remaining zones based on the frequency capabilities determined from the graphs based on the performance measurements taken at the remaining zones so that - As such, using every available head considered in the disk drives under measurement has, BPI histograms can be extracted at a given target performance metric per zone.

— FIG. 2B shows an example curve of error rate of performance (SER) as a function of BPI (e.g., SER at 6 different BPI/frequency samples) for a head located at the outer diameter (OD) of the disk. Also shown is extracted BPI/frequency capability value of that head at a zone (e.g., OD) for the specified

~~target error rate, using interpolation/extrapolation (i.e., if the specified desired target error rate is outside the performance range, extrapolation or interpolation, such as polynomial fit, is used as necessary). The amount of BPI gain, or margin relative to the nominal BPI setting, is also specified and marked.~~

~~Thus, The performance measurements are provided for each head at each zone in the selected disk drives, the graphs are generated for each head at each zone, the frequency capabilities for each head at each zone are determined for a target performance metric, and the histograms are constructed for each head at each zone for the target performance metric. Likewise, above process is performed for all the heads considered in the measurement procedure, and a BPI/frequency capability of all heads at a given target error rate for every zone is generated. Thus, in this manner, BPI/frequency capability histograms for every zone at a specified target error rate are constructed. If a the histogram of head BPI capability at a target performance metric error rate of a every zone (such as an intermediate zone) is not available, then the histogram for that zone can be constructed by interpolation or /extrapolation is preformed to construct histograms for the intermediate zones. The histograms can be used to estimate a BPI distribution.~~

FIG. 2D shows a joint BPI distribution calculated from the histograms of the heads in the measured disk drives at a~~The constructed histograms are used to calculate cumulative performance distribution functions (CDF) of the head frequency (e.g., BPI) capability at a given target performance metric. The joint BPI distribution is a 2D distribution based on the histograms in FIG. 2C error rate performance metric) as input to the format optimizer at the target on-track symbol error rate of  $6 \times 10^{-7}$ . The x-axis is the BPI capability of the heads at the middle diameter (MD) of the disks, the y-axis is the BPI capability of the heads at the outer diameter (OD) of the disks, and the z-axis is the calculated number of heads divided by the total number of heads. The joint BPI distribution provides~~



an estimate of the probability that the heads meet the target performance metric at the MD and the OD.

The joint BPI distribution may predict, for example, that 10% of the heads in the measured disk drives can operate at a high frequency of 1.5 x the reference frequency, 50% of the heads can operate at a high frequency of 1.25 x the reference frequency, 90% of the heads can operate at the reference frequency, and 99.9% of the heads can operate at a low frequency of 0.75 x the reference frequency.

~~Such performance distribution functions are designated as marginal, individual or per zone distributions. In one example the distribution functions include one dimensional (1-D), two dimensional (2-D) and three dimensional (3-D) joint BPI/frequency capability CDF, calculated at the same specified target error rate. Marginal or one dimensional distribution functions from the joint distribution functions can also be calculated.~~

~~A version of estimating performance (e.g., frequency capability) cumulative distribution functions at a given desired target performance metric and zone is described. A number of frequency format profiles can be generated and tested on a set of disk drives to ensure proper operation. The frequency formats are generated and used to exploit every head's linear density or frequency/BPI sensitivity at every zone. Thus, for example, the linear bit density sensitivity of every head at a zZone\_K (where K ranges from 1 to M-zones) at the six frequency samples is determined. To do so, the performance of every head is measured (after full drive read/write and servo calibration/optimization) at each frequency at ZoneK. If frequency 1 Freq1\_K, frequency Freq2\_K . . . , . . . , fFrequency 6\_K are the frequency samples selected frequencies at zZone\_K, in the measurement process, every head is positioned on a track (e.g., the same track) in at zZone\_K and the record/playback performance of each head is~~

measured at every frequency sample using a target performance metric of choice (e.g., off-track symbol error rate (SER)).

The BPI distributions can be calculated at the target performance metric as ID, 2D or 3D distributions that are marginal, individual or per zone distributions, respectively. The format optimizer uses the estimated frequency capability BPI distributions for every zone at the target performance metric to determine the storage capacity and yield.

—— For example, FIG. 2B shows the on-track SER performance of a selected head e.g. Head1, at Zone1, and the best least square polynomial fit curve. For a desired on-track target SER of  $6e-7$ , the BPI capability of the (randomly) selected Head1 at that target performance metric can be projected by extrapolating the data (interpolation is performed if the desired on-track target SER is in the performance range, and extrapolation is performed otherwise). FIG. 2B shows the projected BPI capability of that head at an on-track SER of  $6e-7$  (i.e.,  $6 \times 10^{-7}$ ). The original nominal kBPI (i.e., before the application of vertical zoning) is also shown. The head can be classified as a strong head because there is a reasonably significant amount of margin before the on-track SER performance of this head can be changed from its nominal frequency/kBPI of  $\sim 188$  with an on-track (log of) SER of  $-9.1$  to a projected on-track (log of) SER of  $-6.22$  operating at a frequency/kBPI of  $\sim 217$ . Hence, there is a total kBPI gain of  $\sim 29$ , allowing increase in the nominal frequency by 15 % while meeting the desired target on-track SER performance metric of  $6e-7$  (i.e.,  $6 \times 10^{-7}$ ). Thus, for example, Head1 of disk drive3 has a frequency capability equal to 217 at an on-track SER of  $6e-7$  (i.e.,  $6 \times 10^{-7}$ ), which is noted for Head1 as one sample for generation and extraction of empirical histograms.

—— Performing the above steps for all the heads of all the disk drives considered in the measurement process, allows extraction of the empirical histograms of frequency capability at on-track SER of  $6e-7$  (i.e.,  $6 \times 10^{-7}$ ) for such heads, as shown by example in FIG. 2D. The y-axis shows the number of heads

that meet the interpolated/extrapolated (i.e., projected) frequency capability that is shown on the x-axis. The extracted (empirical) histogram can be used to estimate the probability cumulative distribution function. The width of each histogram 76 corresponds to a variance of the head performance histogram, wherein an objective of the present invention is to improve the disk drive yield and capacity, and as a result reduce that variance.

FIG. 2C shows an example joint BPI distribution plot. Such BPI distributions may predict that, for example, 10% of the heads in the disk drives for which measurement was performed, can operate at a frequency density of  $1.5 \times \text{freq}$  (wherein freq is a reference frequency), and 50% can operate at density of  $1.25 \times \text{freq}$ , and 90% can operate at density of  $1.0 \times \text{freq}$ , and 99.9% can operate at density of  $0.75 \times \text{freq}$ , etc. Using the estimated frequency capability cumulative distribution functions at the target performance metric and every zone, the format optimizer determines the disk drive yield and capacity.

FIG. 2C is an example of a 2-D joint (i.e. outer diameter (OD) and middle diameter (MD)) BPI cumulative distribution function (CDF) at a target performance metric (e.g. on-track symbol error rate of  $6e-7$ ). The x-axis shows the BPI capability of all heads (i.e. from all the disk storage devices considered in the measurement phase) at MD AND y-axis is the BPI capability of all heads at OD. The z-axis shows the (calculated) number of heads divided by the total number/population of heads i.e., an estimate of probability that those heads have a joint BPI capability at OD AND MD of less than or equal to any given desired values. BPI capability for e.g. at OD in the above description it is meant that while operating at (or below, i.e., if considering CDF) a given BPI, after full Read/Write and servo calibration and optimization, meeting a desired given target performance metric of choice at OD. Thus, the aforementioned description of BPI capability can similarly be extended to joint BPI capability.

Format Optimizer-process

1  
 2 The format optimizer ~~process block 66 provide~~comprises a variable BPI  
 3 optimization. ~~The format optimizer 66 solves process for solving multiple (e.g.,~~  
 4 ~~three) constrained optimization problems in response to various inputs. given the~~  
 5 ~~inputs: number of frequency formats (i.e., desired number of different read/write~~  
 6 ~~frequencies), number of heads in each disk drive, and thesaid BPI distributions.~~  
 7 The first problem maximizes the drive-yield while preserving the storage same  
 8 drive-capacity, the second problem maximizes the storage drive-capacity while  
 9 preserving the same drive-yield, and the third problem maximizes the drive-yield  
 10 while reducing the track density and meeting the storage capacityallowing  
 11 reduced/relaxed TPI such that the desired target drive capacity can be met. The  
 12 inputs include the number of different read/write frequencies (frequency profiles  
 13 or formats), the number of heads in each disk drive, the BPI distributions, and the  
 14 nominal storage capacity. The BPI distributions indicate the frequency capability  
 15 distribution of the heads at a target performance metric.

## 16 17 I

18  
 19 ———The format optimizer 66 inputs ~~thesaid BPI distributions, a desired disk~~  
 20 ~~drive capacity, the total number H of heads per disk drive and the number N of~~  
 21 ~~frequency profiles or vertical zones (i.e., frequency per zone across a diskmedia~~  
 22 ~~surface stroke). Given the frequency capability distribution of heads at a target~~  
 23 ~~performance metric, the total number of vertical frequency formats (F), the total~~  
 24 ~~number of heads per drive (H) and the nominal drive capacity, the format~~  
 25 optimizer 66 simultaneously searches through all possible continuous range of  
 26 all possible frequency capabilities to maximize the drive-yield such that the  
 27 desired-nominal storage drive-capacity is met. The format optimizer 66 can also  
 28 performsolve the same operation with the problem, but the drive-storage capacity  
 29 and the drive-yield interchanged interchanged.

~~The As such, in one example, the format optimizer 66 can optimizes high~~  
~~and /low data density as a function of the zones, to improve the drive yield and~~  
~~meet a fixed target capacity. The format optimizer also optimizes capacity while~~  
~~achieving a fixed nominal drive yield, wherein the nominal yield is before the~~  
~~application of vertical zoning according to the present invention. ForIn the said~~  
~~example, in a disk drive with eightof F=2 formats (high density and low density)~~  
~~and H=8 heads 16 in a disk drive 100, the possibilities are oneinclude 1 head at~~  
~~high data density and seven7 heads at low data density, two2 heads at high data~~  
~~density and six6 heads at low data density, three3 heads at high data density~~  
~~and five5 heads at low data density, four4 heads at high data density and four4~~  
~~heads at low data density, one1 head at low data density and seven7 heads at~~  
~~high data density, two2 heads at low data density and six6 heads at high data~~  
~~density, and three3 heads at low data density and five5 heads at high data~~  
~~density, etc. Hence, the format optimizer 66 considers all the combinatorial~~  
~~possibilities, and in each case solves a constrained optimization problem and~~  
~~finally chooses the best optimal solution amongst all the possibilities.~~  
 Alternatively, the format optimizer 66 can be designed to reach the best optimal  
 solution more directly by solving a (non-linear) mixed-integer programming.

Therefore, once the 1-D, 2-D and 3-D joint-BPI distribution/frequency  
~~capability CDFs (discussed above) at a given target performance metric are~~  
~~calculated and passed as input to the format optimizer 66, the format optimizer~~  
~~66 solves the above two problems, namely: (1) maximizing or improving the drive~~  
~~yield (i.e., due to the target pre-selected performance metric, e.g., off-track SER)~~  
~~while meeting the a desired nominal storage drive capacity, and (2) maximizing~~  
~~the storage disk drive capacity while meeting thea desired nominal drive yield.~~

The format optimizer 66 then mathematically casts these two problems  
~~stated above as constrained optimization problems and solves them using well-~~  
~~known optimization techniques such as a e.g. line search algorithm. The~~  
 constrained optimization problems can also be cast as (non-linear) mixed-integer

programming and solved using existing ~~methods in optimization~~ methodstheory.  
 Example constraints to be considered, and cast mathematically within the format  
 optimizer 66, include not exceeding a certain frequency at the outer diameter OD  
 due to ASIC data rate limitations or at the inner diameter ID due to  
 head/diskmedia limitations. Furthermore, closed form equations are derived and  
 used in the format optimizer 66 to estimate the storage capacity and actual drive  
yield and drive capacity. The format generator 66 also considers A-Format  
Generator process, described below, is utilized to calculate the actual drive  
capacity after including all possible overheads, such as adding and including  
redundant bits due to error correction coding or gray coding.

The format optimizer 66 also uses the information from the format  
 generator 68, such as the calculated format efficiency per zone (i.e., defined in  
 percentages as the amount of user data e.g. in blocks that can fit in all tracks in a  
 zone), or the number of tracks per zone, to achieve a very close estimate of the  
storage disk drive capacity calculation as determined by the format generator 68.  
 Then, the format optimizer 66 calculates optimal linear bit density format profiles  
 as well as the optimal number of heads allocated to each vertically zoned format  
profile.

For As an example, histograms are extracted and the corresponding BPI  
distributions are estimated for different zones at the desired target on-track  
symbol error rates (e.g., for Zone1 at a target error rate of  $1e^{-6}$ , Zone2 at a target  
error rate of  $1e^{-6}$ , Zone3 at a target error rate of  $1e^{-6}$ , etc.) as described above of  
 $6 \times 10^{-7}$ . A format design is provided for a disk drive with four4-heads disk drives  
(Hand two frequencies to optimize yield =4), and 2 vertical frequency  
format/profiles (F=2), wherein the disk drive yield is optimized while meeting a  
minimum storage capacity requirement.

~~Without the method of the present invention (vertical zoning),~~  
 conventionally when the same frequency is used per head per zone, if one of the

~~4 heads is a weak performing head having an error rate measurement e.g.  $1e^{-5}$~~   
~~at Zone1 (higher than the target error rate), that disk drive is failed. With the~~  
~~application of the present invention in that case, the format optimizer allocates~~  
~~the 3 other heads to higher frequencies, and allocates the weak head to a lower~~  
~~frequency at Zone1. The recording/playback performance of the weak head is~~  
~~compensated for, such that the minimum capacity requirement is met. As such,~~  
~~the format optimizer 66 utilizes the performance distributions to determine two or~~  
~~more optimal frequencies per zone, and the optimal number of head allocations~~  
~~to those frequencies per zone such that constraints such as required disk drive~~  
~~yield and/or capacity are met.~~

For example, the format optimizer 66 uses the estimated 1D, 2D and 3D  
 joint frequency/BPI capability distributions at the a desired target performance  
 metric to jointly optimize for vertically zoned frequency format profiles and the  
 corresponding number of head allocations three zones at a time. An advantage  
 of considering three zones instead of one zone, ~~as compared to only one (and~~  
~~thus considering a joint optimization instead of versus individualized~~  
~~optimization,~~ is that the joint optimization allows the optimization of format  
~~profiles (e.g., frequency profiles to be optimized)~~ across the stroke on each disk  
 surface. Therefore, joint optimization in this way we exploits the potential  
 correlation in performance from one zone to another zone as well as their  
 individual and weighted contribution to the storage overall surface capacity. A  
joint optimization approach is preferable for a high/low/high data density format  
~~layout across the stroke for either improving the drive yield while keeping the~~  
~~same storage drive capacity, or improving the storage drive capacity while~~  
~~preserving the same drive yield.~~

The format optimizer 66 generates results from the format optimizer  
~~include:~~ the target high/low BPI formats per zone, the (optimal) number of head  
~~allocations per format, layout and an estimate of the storage capacity and drive~~  
~~yield and capacity.~~ -The accuracy of the estimates can be sensitive to the

1 underlying ~~extracted (joint)~~ BPI distributions at the target performance metric  
 2 ~~given (on or off track) error rate~~. Further, the target high/low BPI formats can be  
 3 sensitive to the variance of the ~~(extracted)~~ BPI distributions. And, the variance of  
 4 the BPI distributions can be sensitive to the absolute value of the target  
 5 performance metric and the type of target performance metric~~(on or off track)~~  
 6 ~~target error rate and the choice of metric (e.g. error rate vs. MSE)~~. In addition,  
 7 ~~because the design of target high/low BPI formats are~~ designed ~~performed~~ three  
 8 zones at a time and the yield improvement (while preserving the storage ~~same~~  
 9 ~~overall drive capacity~~) is based on the profile of the target nominal formats. ;  
 10 The format optimizer 66 also ~~allows for a smoothing operation in order to smooth~~  
 11 ~~the target variable BPI format designs if so desired~~. The format generator 68  
 12 determines the number of tracks per zone, the number of blocks per track, the  
 13 radius at each zone, as well as block and track format efficiency. This  
 14 information is saved in ~~e.g.~~ output files for use with the format optimizer 66. The  
 15 format optimizer 66 then saves the ~~design of target high/low BPI formats per~~  
 16 zone that it generates, in two separate files that can be ~~read and loaded as input~~  
 17 ~~files into the format generator 68~~.

18  
 19 Once the target format profiles are calculated, if they are non-smooth  
 20 across the stroke, optionally a smoothing process is applied. The format profiles  
 21 are then loaded into the format generator 68 ~~described below~~, to create vertically  
 22 zoned formats and configuration pages. The formats and configuration pages  
 23 are used by the disk drive firmware to create binary files to be loaded into the  
 24 reserve image of the disk drives as part of the file system. ~~FIG. 2A shows the~~  
 25 ~~communication between the format optimizer 66 and the format generator 68~~. In  
 26 this fashion, the design and implementation of the format profiles, as well as the  
 27 number of optimal head allocations are performed off-line and are predetermined  
 28 for every disk drive configuration.

29  
 30 For An example, in a disk drive with four heads and four disk surfaces on  
 31 two disks, the format optimizer 66 designs ~~of format optimization for designing~~



vertically zoned high and low and high-frequency profiles for disk drives with 4  
heads (i.e., Head1 through Head4 corresponding to Surface1 through Surface 4  
of Disk1 and Disk2) is described. In this example, every disk surface is  
(uniformly) partitioned into three zones across the stroke, at a track density with a  
fixed number of tracks (TPI) per zone, vertically aligned from one disk surface to  
another. The nominal disk surface data storage capacity (before the application  
of vertical zoning) can be approximated by the sum over all the zones of the  
products of nominal tracks per zone multiplied by the nominal BPI frequency per  
trackzone multiplied and by the format efficiency per zone. -Format efficiency per  
zone is the percentage of all the user data that is effectively stored per zone.  
Then the nominal storage disk drive capacity is equal to the nominal disk  
surface data storage capacity multiplied by the total number of disk surfaces (or  
heads). The nominal number of tracks per zone and the format efficiency per  
zone can be generated by and obtained from the format generator 68 (described  
further below).

Performing vertical zoning to e.g. improve the drive yield without losing  
storage by nominal (disk drive) capacity, finds the best frequency per zone and  
per head such that the disk drive meets performance and storage capacity  
requirements. As such, if a disk drive with four 4 heads fails test process  
performance limits due to the e.g. performance of hHead\_1 at zZone\_1, but the  
performance of another head/zone pair, such as hHead\_1 at zZone\_2 (or another  
head such as hHead\_3 at zZone\_1,) performance is significantly better, (i.e.,  
passing the test limits with reasonable margins), then a higher than nominal  
frequency than nominal at zZone\_12 or zZone\_24 is designed for the strong  
heads that are stronger (i.e. high density heads), and instead the frequency at  
zZone\_1 for the weak heads that are weaker (i.e. low density heads) is lowered.  
This trade-off is performed obtains a vertically zoned design of variable  
frequencies per zone such that the storage overall disk drive capacity is  
preserved, to obtain a vertically zoned design of variable frequencies per zone.  
 In addition, the number of heads (e.g. per zone) allocated to high or low data

density is determined. Thus, the storage disk drive capacity can be approximated by the sum (over all the zones) of ~~the products of the~~ number of strong low density heads per zone multiplied by the high low frequency data storage per zone multiplied by the format efficiency per zone plus the (sum over all the zones of the) products of the number of weak high density heads per zone multiplied by the low number of high frequency data storage heads per zone multiplied by the format efficiency per zone.

For example, ~~in one version,~~ the format optimizer solves for the above problem as follows. The format optimizer 66 is provided with joint the BPI (joint) frequency capability cumulative distribution functions (extracted and estimated from all heads considered in the measurement process above) at the a desired target performance metric (i.e., ~~the same targets used in the test process~~). Then, for every combinatorial possibility of head allocation (e.g. to high or low frequency,) the format optimizer 66 searches through a continuous range of possible frequencies, by considering every zone independently (i.e. using the marginal distributions) and by the combination of zones (i.e. using the joint BPI distributions), to maximize the disk drive yield calculated using a closed form equation, such that the storage disk drive capacity after the application of vertical zoning is applied is essentially the same as the nominal storage disk drive capacity. Further, the (optimal) high and low and high frequency profiles for every combination of head allocations is compared and the one that results in the highest value of (calculated) disk drive yield is chosen and passed to the format generator 68 for the generation of vertically zoned configuration pages to be used by the disk drive firmware.

The disk surfaces of disks can be partitioned into more than ~~the example~~ three zones above. ~~The above steps of determining the optimal variable frequencies per zones are useful to consider more than three zones.~~ To reduce computational complexity and time, if the selected/designed number of zones per disk surface in a disk drive is more than three, the format optimizer 66 can be

1 ~~used to generate~~ high and low and high-frequency profiles three zones at a time  
 2 ~~and, suitable smoothing operations are used to smooth the profile after post-~~  
 3 processing. Another approach includes embedding the smoothing operator in  
 4 the design and extending the joint optimization to all the zones ~~so as to consider~~  
 5 the effect-and-impact of smoothing to drive-yield (calculation) as part of the  
 6 design rather than the later stages.

7  
 8 In the disk drive with four ~~above 4-heads disk drive example, the disk drive~~  
 9 yield is maximized while preserving the ~~same nominal~~ storage ~~disk drive~~  
 10 capacity. To determine the number of head allocations, the format optimizer 66  
 11 begins with one weak ~~one low density head and three strong high density heads~~  
 12 ~~(e.g., per zone)~~. The format optimizer 66 searches through a continuous range  
 13 of possible frequency capabilities per zone, as well as two and three zones at a  
 14 time, by considering ~~and using the 1D (i.e., marginal), (joint)-2D and 3D BPI~~  
 15 distributions that result in the best calculated ~~value of the drive yield~~ such that a  
 16 minimum nominal storage drive capacity can be obtained. Next, the format  
 17 optimizer 66 uses two weak heads and two strong ~~low and high density heads~~  
 18 and repeats solving the ~~same~~ constrained optimization problem. This process is  
 19 continued until all the combinatorial possibilities are considered. Finally, the  
 20 format optimizer 66 chooses the solution that results in the best calculated ~~value~~  
 21 ~~of the drive yield~~ and provides the target high and low and high (optimal) data  
 22 density format profiles and the associated number of high and low head  
 23 allocations to the format generator 68. The format generator 68 then generates  
 24 vertically zoned format files and configuration pages to be used by the disk drive  
 25 firmware.

## 26 27 Format Generator

28 ~~— In one embodiment, the format generator process block 68 is used for~~  
 29 ~~embedded servoing (i.e., servo position is generated by reading back written~~  
 30 ~~information from the disks, such as servo wedges in which position information is~~

1 ~~embedded on the disks, and that information is used to position the head on the~~  
2 ~~disk surfaces).~~

3  
4 ~~For example, the format generator 68 described herein generally~~  
5 ~~performs three functions. First, the format generator 68 uses including utilizing~~  
6 ~~target formats/frequencies (or linear densities/BPI) for each zone as an input,~~  
7 ~~and performing an exact calculation of the data storage capacity of each zone~~  
8 ~~and thus the storage capacity of the disk drive itself. Second~~ Further, the format  
9 generator 68 calculates the format efficiency (the percent of the disk surface area  
10 that is occupied by user customer data) for each zone. ~~Third, The third, and~~  
11 ~~primary purpose of the format generator 68 is to generate configuration pages~~  
12 ~~data. The configuration pages contain per-drive, per-zone, and per-head-per-~~  
13 ~~zone parameters that are programmed into the disk drive electronics such as~~  
14 ~~components. Such components include the preamplifier 21, the disk controller,~~  
15 ~~the read/write channel 51, and the controller 57~~ preamplifier. The parameters are  
16 ordered such that the disk drive firmware selects the correct set of parameters to  
17 be programmed into each of the components for the particular head and zone  
18 that is being written to or read from at the time.

19  
20 The format generator 68 calculates the exact frequency and the data  
21 storage exact capacity of each zone taking into consideration limitations in the  
22 programmability and of the components and limitations of the capabilities of the  
23 disk drive components. For example, Some examples of component limitations  
24 include: the heads 16 have varying down-track separation between the read and  
25 write elements, the preamplifier 21 has a minimum and maximum delay in turning  
26 on the write current, the read/write channel 51 synthesizer frequencies are  
27 limited to a discrete collection of frequencies, the motor driver 53 can keep the  
28 spindle motor 14 within a finite precision of the nominal rotational speed;  
29 ~~preamplifier (not shown) has a minimum and a maximum delay in turning on its~~  
30 ~~write current; the down track separation between the head read and write~~  
31 ~~elements (not shown) varies from component to component; the reference~~

1 ~~crystal (not shown) has finite accuracy and stability over temperature; the~~  
2 ~~spindle motor driver can keep the spindle motor speed within a finite precision of~~  
3 ~~the nominal rotational speed; the controller 57 has specific latencies in~~  
4 ~~generating commands to the preamplifier 21 and the read/write channel 51 and~~  
5 ~~preamplifier, often with a finite uncertainty as to the exact timing of these~~  
6 ~~commands, and a reference crystal (not shown) has finite accuracy and stability~~  
7 ~~over temperature, etc.~~

8  
9 The format generator 68 can be fully automated, or can be directed by a  
10 human operators specialist. In the absence of input from the format optimizer 66,  
11 the target per-zone BPI/frequency profiles, in particular, must be generated  
12 by from a human operator input. In general, the human operators specialist  
13 modifies the target frequency profiles until the desired storage capacity is  
14 reached.

15  
16 ~~In one embodiment,~~ the format generator 68 includes a format efficiency  
17 process that uses the format optimizer 66's target high/low/high variable BPI  
18 format designs as well as the optimal predetermined number of high/low/high  
19 performing head allocations, to modify and generate the appropriate  
20 configuration pages (i.e., as part of the file system). For each zone, the format  
21 generator 68 selects the nearest frequency to the target frequency for that zone,  
22 given the component limitations ~~and programmability~~ mentioned above. The  
23 nearest frequency provide comprises the target formats.

24  
25 The optimal predetermined number of ~~low/high/low~~ performing head  
26 allocations comprises the number of heads allocated to each of the multiple  
27 frequencies in each zone. The format optimizer 66 determines the head  
28 allocation, which is input to the format generator 68. The capacity of a zone  
29 depends ~~both~~ on the target frequencies and the number of heads allocated to  
30 each frequency.

The format optimizer 66 uses the nominal average BPI or frequency (nominal BPI format target designs) (e.g., one read/write frequency) in each zone as ~~input~~ from the format generator 68 to estimate the ~~disk drive~~ yield before applying the variable BPI designs. For a design with multiple frequencies per zone, this is the weighted average (by the number of allocated heads) of the multiple frequencies. The nominal format is created by ~~e.g.~~ a human operator working with the format generator 68 in an the interactive manner described ~~above~~.

The format generator 68 ~~performs calculations~~ the number of tracks per zone, number of blocks per track, radius at each zone as well as block and track format efficiency to calculate the ~~drive-zone~~ data storage capacity. The format optimizer 66 estimates the zone data storage capacity using the tracks per zone, radii, and format efficiency. Thus, the format optimizer 66 and the format generator 68 interact as shown in FIG. 2A6. For example, in a disk drive with four ~~for 4-heads disk drives~~, and two~~2~~ data density format frequency profiles (i.e., high and low frequency profiles) with three~~3~~ zones across the disk surface, after the measurement and optimization processes, the format generator 68 is provided with two~~2~~ optimal frequency profiles and the optimal allocation of the heads. The format generator 68 then calculates the storage capacity, and if the disk drive capacity meets the minimum required storage~~required~~ capacity, ~~then~~ the format generator 68 generates the configuration files/pages for the disk drive firmware. The configuration pages are used by the disk drive firmware to command the head to write at an assigned frequency to a zone. If the calculated storage drive capacity does not meet the minimum required storage capacity, the format optimization is performed again with new format efficiency values, and the process is repeated.

#### Head format Assignments and selection criterion

Allocating ~~The process for allo~~the cation of numbers of heads to each of the predetermined multiple frequencies in a zone, and assigning ~~the process of~~

1 ~~assignment of~~ a particular head in a particular disk drive to a particular  
2 frequency, are distinct. ~~First the allocation process is performed by the format~~  
3 ~~optimizer 66, and applies to the disk drives of a particular design (product).~~  
4 Then, the head assignments ~~are process is then performed during manufacturing~~  
5 as part of a test process undergone by each disk drive to be produced. ~~This~~  
6 ~~section describes the assignment process task.~~

7  
8 Once the configuration pages are generated and converted to binary files  
9 as part of the file system, they can be loaded and saved into a reserved image of  
10 the disk drive for use after power cycling. Then, for every disk drive, the  
11 ~~following example assignments are process is performed per head and per zone,~~  
12 to ~~determine assignment of a certain predetermined number of heads to high BPI~~  
13 formats and the remaining heads to low BPI formats in a two frequency design,  
14 to satisfy the allocation of heads to the said formats by the format optimizer 66.

15  
16 The head assignments ~~process~~ for the two ~~example 2~~ frequency format  
17 where high and low frequencies are used, includes the steps of:

18 (1). Load default parameters from the configuration pages, and  
19 calibrate selected parameters on a per head, per zone basis (e.g., load high BPI  
20 format profile for all the zones across the stroke);

21 (2). Take measurements from the all heads at ~~all the~~ disk surfaces at  
22 pre-selected zones with respect to a target performance metric, e.g., mean  
23 ~~square error, on/off track error rate, etc.;~~

24 (3). For each head in every measured zone, sort/rank the heads by the  
25 target performance metric from best to worst; select a pre-specified (by the  
26 allocation process in the format optimizer 66) number of heads with the best  
27 performance, and assign those heads to the higher frequency for a particular  
28 zone;

29 (4). Optionally interpolate between the measurements obtained from  
30 the pre-selected number of zones to find the results for the other zones, and do  
31 the same for the interpolated zones. The interpolation ~~operation in a version of~~

1 ~~the present invention~~ reduces the test process time. Head performances are  
2 measured, sorted and assigned to a frequency for a subset of the total number of  
3 zones. For the remaining zones, the heads are assigned by interpolating ~~on~~ the  
4 head assignments ~~made from~~ the measurements;

5 (5) For every zone, save the worst pre-specified number of weak bad  
6 ~~(i.e. low performing)~~ heads with respect to the target performance selected  
7 metric; and

8 (6) For every zone, load and calibrate ~~all the~~ weak bad heads with the  
9 lower BPI format.

10  
11 The above process can ~~be used to improve~~ storage yield, improve  
12 capacity, improve yield and trade-off between ~~yield and storage capacity and~~  
13 yield. In a test, the heads can ~~be passed or failed~~ with respect to a target  
14 performance metric ~~(e.g., off track error rate)~~ to determine if the test target limits  
15 are met.

16  
17 The disk drives ~~serve~~ firmware is extended to load more than one format  
18 profile. A head can be assigned a different read/write frequency per zone across  
19 a disk surface, and radially similarly situated zones on different disk surfaces can  
20 have different read/write frequencies assigned to the corresponding heads  
21 whereby one head is assigned a different frequency/format profile than another  
22 head.

23  
24 The head example ~~assignments~~ ~~process described herein~~ applies to a  
25 format design with two recording frequencies per zone, but. ~~However, the~~  
26 ~~process~~ can be easily extended to more than two frequencies per zone and,  
27 ~~wherein the process can be iterated upon~~ to assign heads to more than two  
28 frequencies per zone, ~~as described by an example below~~. For example, in a  
29 design with H heads and F frequencies per zone, ~~above~~ steps 1 and 2 are  
30 completed for the high frequency. The first selection of heads in step 3 assigns  
31 the highest h1 heads, where h1 is the pre-specified number of heads allocated to



the highest frequency for that zone. The remaining ( $H - h_1$ ) heads are then loaded and calibrated with the second highest frequency (step 1 again), measurements are taken (step 2 again), ~~and the heads are ordered~~ relative to the metric and the best  $h_2$  heads are assigned to the second highest frequency (step 3 again). Here  $h_2$  is the pre-specified number of heads allocated to the second highest frequency in the zone. Steps 1-3 ~~of the process~~ are then iterated for the ( $H - h_1 - h_2$ ) heads, followed by the ( $H - h_1 - h_2 - h_3$ ) heads, and so on, until  $h_F$  heads remain to be assigned to the lowest frequency. -The set of  $\{h_1, \dots, h_F\}$  heads receive ~~comprise~~ the head allocation made by the format optimizer 66.

Table 1 ~~below illustrates the result of an example of the vertical zoning head assignments process~~ on a disk drive with six6 heads and five5 zones across the stroke on each disk surface. Each head is assigned to either a high or low data density format based on record/playback performance of that head, ~~and wherein as discussed above,~~ the number of heads assigned to high data low density and the number of heads assigned to low data high-density is according to the head allocation ~~results~~ determined by the format optimizer 66.

| HEAD # | <u>FORMAT</u> <u>ZONE</u><br>ZONE 1 | ZONE 2 | ZONE 3 | ZONE 4 | ZONE 5 |
|--------|-------------------------------------|--------|--------|--------|--------|
| 0      | Low                                 | High   | Low    | High   | Low    |
| 1      | High                                | Low    | High   | High   | Low    |
| 2      | High                                | Low    | High   | Low    | High   |
| 3      | High                                | High   | Low    | High   | High   |
| 4      | Low                                 | High   | High   | High   | High   |
| 5      | High                                | High   | High   | Low    | High   |

Table 1 – EAn example ~~for the~~ format assignment of a disk drive after test ~~process,~~ using vertical zoning with variable BPI across ~~the~~ zones.

1 ~~FIGs. 3-6 show example steps of an embodiment of the above processes.~~  
 2 Referring to FIG. 3 shows, a flowchart of an example vertical zoning data  
 3 collection ~~that process~~ includes the steps of:

4 (1) Select a number of disk drives for data measurement/collection  
 5 ~~process~~-(step 300);

6 (2) Create a nominal linear bit density profile KFCI (~~i.e., nominal~~  
 7 ~~\_KFCI~~):

8  $\overline{kFCI}(R)$ , where  $R$  is the disk radius (step 302);

9

10 (3) Create more linear bit density profiles by multiplying the nominal  
 11 ~~\_KFCI~~ by the scaling factor  $x_i$ , (step 304):

$$(1 \pm x_i) * \overline{kFCI}(R)$$

12

13 (4) Create a binary file system for every generated profile (step 306),  
 14 ~~i.e. for~~

15

$$i \in \{1, \dots, N\}$$

16

17 where  $N$  is the total number of frequency format profiles, ~~f~~ For  
 18 example, for  $N=2$ , having  $X_1$ , and  $X_2$ , if  $X_1=0.05$  and  $X_2=0.1$ , then including  
 19 the nominal frequency format ~~itself~~, there are five5 different frequency profiles in  
 20 step 304, as follows: (a) nominal\_KFCI, (b)  $1.05 \times$  nominal\_KFCI, (c)  $0.95 \times$   
 21 nominal\_KFCI, (d)  $1.1 \times$  nominal\_KFCI, and (e)  $0.90 \times$  nominal\_KFCI (~~wherein~~  
 22 ~~"\*" is the multiplication operator~~);

23 (5) Select the first head by setting  $i$  to 1 (step 308);

24 (6) Load the file system  $i$  into the reserved image of the disk drives  
 25 (step 310);

26 (7) Take the head performance measurements (~~e.g., (on/off) track MSE~~  
 27 ~~and SER measurements~~) (step 312);

28 (8) Unload and save the results in the dData bBase (step 314);

- 1 (9) Increment  $i$  by one ( ~~$i=i+1$~~ ) (step 316);
- 2 (10) Determine if  $i = N$ ? (step 318);
- 3 (11)                      If not, go to step 310; and
- 4 (12) Otherwise, else stop (step 320) done.

5

6 The above process collects performance data for all the heads at all the

7 zones.

8

9 Referring to FIG. 4 shows, a flowchart of an example vertical zoning post-

10 measurement processing and per zone BPI distribution extraction that process

11 includes the steps of:

- 12 (1) Organize the head performance data (e.g., MSE and SER)
- 13 ~~obtained above~~, for every head  $i \in \{1, \dots, M_1\}$  and every zone  $j \in \{1, \dots, M_2\}$  as
- 14 a function of the linear bit density samples, wherein in this example  $M_1$  is the total
- 15 number of heads in the disk drives selected for the measurement process (e.g.,
- 16 ~~40 disk drives each including 4 heads, results in total of  $M_1=160$  heads~~), and  $M_2$
- 17 is the total number of zones, to generate head performance histograms (step
- 18 400);

- 19 (2) Choose a target performance metric (e.g., MSE or SER) (step 402);

- 20 (3) Set  $j = 1$  and  $i = 1$  (step 404);

- 21 (4) Interpolate/eExtrapolate BPI at the ~~specified~~ target performance
- 22 metric (e.g., MSE or SER) for head  $i$  at zone  $j$  (step 406);

23

- 24 (5) Select the next head by incrementing  $i$  by one ( ~~$i=i+1$~~ ) (step 408);

25

- 26 (6) Determine if  $i = M_1$ ? (i.e., have all the heads have been
- 27 processed?) by determining if  $i = M_1$ . (Step 410);

28

(7) If not, got to step 406 to process the next head, ~~otherwise~~ else generate a frequency capability histogram at ~~that given~~ zone  $j$  for all the heads (step 412);

(8) Determine if ~~is  $j = M_2$ ?~~ (i.e., have all the zones have been processed?) by determining if  $j = M_2$ . (Step 414);

~~(9) If yes, stop;~~

~~(9) If not, Otherwise,~~ move to the next zone and start with the first head again, set whereby  $j = j + 1$  and,  $i = 1$  (step 416), and go to step 406; and

(10) Otherwise, stop (step 418) to repeat.

The above process generates {1D} frequency capability histograms at a target performance metric ~~and~~ for every zone by considering all the heads from the sample disk drives selected for in the measurement process. Using the {1D} frequency capability histograms at a ~~given~~ target performance metric, techniques in probability theory known to those skilled in the art can be adopted to estimate the {1D} frequency capability distributions. Further, the above process ~~above~~ is extended (i.e., by using 2D and 3D interpolation/extrapolation routines), to extract and estimate the 2D and 3D joint frequency capability histograms and their associated distributions.

Referring to FIG. 5 shows, a flowchart of head assignments for N heads with an example head assignment process for a two frequency format (N=2, high/low data density) that design, includes the steps of:

(1) Assign all ~~n~~ the heads in a disk drive to the ~~first selected~~ format (e.g., high data -density format) (step 500);

(2) Calibrate all ~~n~~ the heads at the high data -density format for selected zones (step 502);

(3) Measure the head performance metric at the selected zones for all the heads (step 504);

(4) For each selected zone, rank the heads by the head performance metric (step 506);

(5) For each selected zone, assign the highest K heads to the high data -density format, and assign the other N-K heads to the low data density format (step 508);

(6) Optionally interpolate the head assignments for the remaining zones (step 510); and

(7) Complete the calibration of all the heads and all the zones at the assigned formats (step 512).

The above process completes the assignment of each head in each disk drive to a predetermined frequency.

~~As shown in FIG. 2A, information is passed between the format~~  
~~generator 68 and the format optimizer 66, wherein initially, the format generator~~  
~~68 passes the information including e.g. track format layout to the format~~  
~~optimizer 66 to have a more accurate way of calculating the storage capacity~~  
~~(nominal format). Such information and constraints are provided to the format~~  
~~optimizer 66 to solve the said joint optimization problems. The format optimizer~~  
~~66 performs a coarse calculation of the storage capacity, whereas the format~~  
~~generator 68 performs an exact calculation of the storage capacity. The format~~  
~~generator 68 performs functions of providing format information (such as e.g.,~~  
~~number of tracks per zone, and the zone format layout) to the format optimizer 66,~~  
~~and calculating the exact storage format capacity. Such information is passed~~  
~~once from the format generator 68 to the format optimizer 66 for a head design~~  
~~(e.g., 4 head design) with a given number of heads. -The format generator 68~~  
~~initially provides nominal information- to the format optimizer 66, and wherein the~~  
~~format optimizer 66 performs its calculation of target densities (zone frequencies~~  
~~and number of heads allocated to each frequency) and provides that information~~

to the fFormat-gGenerator 68. The format generator 68 then determines if required storage capacity has been reached. Adjusting the target densities to meet storage capacity and/or yield and/or capacity requirements includes adjusting the selected zone density or zone frequencies.

Referring to FIG. 6 shows, a flowchart of format generation and optimization in which an in-example Format Generator/Format Optimizer iterative process for a minimum storage capacity requirement (C), and a user specified storage allowed overcapacity-Delta, ( $\Delta$ ) includes the steps of:

(1) Determine the disk geometry, track density (TPI) and servo spokewedge details, and provide the output inner diameter (ID) and outer diameter (OD) radii, the track density (TPI), the number of servo spokewedges, and the servo spokewedge length (step 600);

(2) The fformat generator 68 generates the initial format at the storage capacity using the values-ID and -OD radii, the TPI, the number of servo spokewedges and the servo spoke wedge-length, and provide outputs the radius of each zone per disk surface, the number of tracks per zone, the number of blocks per track, and the format efficiency by zone (step 602);

(3) The fformat optimizer 66 generates optimal target densities at all the zones using the radius of each zone per disk surface, the number of tracks per zone, the number of blocks per track, and the format efficiency by zones as described above, and provides the high and low BPI outputs frequency-density targets (e.g., low/high BPI) by zone, and the number of high and low BPI frequency density (e.g., low/high BPI) head allocations by zone (step 604);

(4) The fformat generator 68 generates new formats with a storage cCapacity (the i.e., number of logical blocks per disk drive) (step 606);

(5) Determine if the storage cCapacity > C and the storage cCapacity < (C +  $\Delta$ Delta) (step 608);

(6) If not, then stop;

(6) Otherwise, adjust the target densities (sStep 610), and go to step 606; and

1 (7) Otherwise, stop (step 612).

2  
3 ~~For~~ In one example, the disk surface capacity is described by the  
4 ~~equation:~~  $\text{TPI} \times \text{BPI} \times (1 + \text{ECC}) / \text{FE}$ , wherein TPI is the track density, BPI is the  
5 linear bit density, ECC is the fractional level of error correcting code used which  
6 is typically about 0.1, and FE is the format efficiency which is typically about 0.57.

7  
8 The above process completes the format generation process.

9  
10 As another example ~~scenario of the results generated by an embodiment~~  
11 ~~of vertical zoning according to the present invention~~, a set of thirty-two<sup>32</sup>  
12 matured disk drives are selected and ~~wherein~~ each disk drive includes twelve<sup>12</sup>  
13 heads. The 1D, 2D and 3D ~~joint-BPI empirical~~ distributions are extracted at an  
14 ~~given specified target on-track~~ symbol error rate from the ~~three pre-specified~~  
15 ~~radial zones, i.e.,~~ outer, middle and inner zones. Next, the BPI extracted  
16 distributions are fed into the format optimizer 66, and high or low or high  
17 frequency per zone format designs are obtained at the three specified zones.  
18 This is performed once by individual optimization, ~~all~~ based on 1D BPI  
19 distributions at each of the three zones, and once by joint optimization based on  
20 the measurements obtained from the three zones and their extracted 1D, 2D and  
21 3D BPI distributions. The head format allocation search process (~~VZ test~~) is  
22 performed ~~by~~ in a simulation, and ~~wherein~~ for each zone the one-format designs  
23 (~~i.e., before the application of vertical zoning~~) are a special case of the two-format  
24 variable BPI designs by forcing the high and low and high formats to be ~~the same~~  
25 ~~and~~ equal to the nominal BPI format at that zone. Furthermore, the pass/fail of  
26 the disk drives is ~~decided based on the criterion that each head at every zone~~  
27 passing a target given on-track symbol target error rate as well as off-track  
28 squeeze and un-squeeze offset margins. Then, the drive yield is calculated  
29 by (~~i.e., in~~ simulation by interpolation/extrapolation of the measurement data)  
30 before and after the application of vertical zoning (VZ). ~~The following Table 2~~  
31 summarizes the results:

|                               | <u>Using Joint Optimization</u> | <u>Using Individual Optimization</u> |
|-------------------------------|---------------------------------|--------------------------------------|
| Drive Yield (Yd)              | 93.75                           | 90.625                               |
| Drives failed after VZ        | 4 & 29                          | 4, 6 & 29                            |
| Drives recovered              | 2, 3, 13, 19, 21 & 25           | 2, 3, 13, 19, 21 & 25                |
| Passed drives failed after VZ | None                            | 6                                    |
| Drives failed before VZ       | 2, 3, 4, 12, 19, 21 & 29        | 2, 3, 4, 12, 19, 21 & 29             |
|                               | i.e., drive yield before VZ     | i.e., dDrive yield after VZ          |
|                               | Yd=75%                          | Yd = 75%                             |

Table 2

~~In addition to disk drives, the present invention is useful with other storage devices such as e.g. tape drives, optical drives, etc. Although a manufacturing test case for a two format design is illustrated described, the search algorithm can be easily be generalized to a higher number of formats. The design of two formats based on 1D, 2D and 3D joint storage density-BPI distributions can easily be generalized to higher order or dimensions by considering more zones than three zones. The design of format designs can be generalized from two to a higher number of formats. The measurement procedure can be generalized to consider more zones as well as off-track measurements such as 747 curves or quality metrics versus error rate measurements to perform a correlation study for the choice of best metric with the least potential test time.~~

Further, the ~~above methods for a per zone variable BPI design can be easily extended to a variable BPI/TPI design as described below. The measurement process is extended to further include 747 measurements of all the heads from a pre-selected number of disk drives. To speed up the measurements of raw data, instead of 747 measurements, off-track and adjacency margin (squeeze measurements) of the all heads can be performed. Once the 747 raw data of the all heads at a pre-selected number of zone locations is determined, for every zone, (joint) BPI/TPI distributions can be extracted at the given desired target(s) by post-measurement data processing of data. The choice of a target is an integral part of the amount of performance gain, such as disk drive yield, due to the per zone variable BPI/TPI designs. Some example choices of target(s) are off-track symbol error rate, the variance~~



1 of-position error signal variance, and ~~or even a~~ combination of both. After the  
 2 joint BPI/TPI distributions are extracted and available for the all zones, a per zone  
 3 variable BPI/TPI design can be obtained by solving two -constrained (joint)  
 4 optimization problems: one that maximizes the ~~drive~~-yield while keeping the  
 5 same disk drive areal density, and another that maximizes the disk drive areal  
 6 density while keeping the same ~~drive~~-yield. Once the per zone variable BPI/TPI  
 7 designs are obtained, ~~a head BPI/TPI allocation and selection criterion, similar to~~  
 8 ~~that described herein, can be used such that a~~ pre-selected number of heads are  
 9 allocated to high and low density BPI and TPI formats, for example, for ~~the case~~  
 10 of a two variable BPI/TPI per zone design performed as part of the test process.

11  
 12 The present invention improves storage capacity ~~drive yield and drive~~  
 13 ~~capacity (and or consequently areal density at a fixed target BPI) and yield,~~ and  
 14 ~~allows reducing~~ the target TPI by increasing the average BPI across the stroke  
 15 per head (depending on the number of formats considered) to meet a desire  
 16 storage target drive capacity. In particular, ~~due to a maximum deliverable data~~  
 17 ~~rate of the ASIC components (e.g., channel, controller and preamp) the BPI at~~  
 18 the outer diameter may be limited by the maximum ~~minimum~~ deliverable data rate  
 19 of the ~~mentioned~~ ASIC components. -For example, if the controller 57 ~~has~~  
 20 ~~capable of a~~ maximum deliverable data rate of 650 MHz, the preamplifier 21  
 21 ~~has capable a~~ maximum deliverable data rate of 700 MHz and the read/write  
 22 ~~channel 51 has capable a~~ maximum deliverable data rate of 750 MHz, then the  
 23 BPI at the outer diameter is limited by the controller 57 at a maximum deliverable  
 24 data rate of 650 MHz. Thus, a conventional one format BPI profile across the  
 25 stroke does not achieve the desired storage drive capacity and ~~the desired~~  
 26 ~~manufacturing drive yield. The target BPI is increased and the BPI profile across~~  
 27 ~~the stroke is relaxed, wherein according to~~ whereas the present invention, ~~the~~  
 28 per zone variable BPI ~~design can be used to design (variable BPI) target formats~~  
 29 ~~that meet the desired~~ storage drive capacity at a fixed target TPI while improving  
 30 the ~~overall drive yield~~.

Referring back to FIG. 2A and FIGs. 3-6, in one embodiment of the present invention, the steps of the example method of the present invention: (1) The data collection/measurement process block 62, can be implemented by on a general purpose computing equipment 61, known in the art, and the drive electronics of the disk drive 100. The general purpose computer 61 can be a high end PC, a PC server or a workstation and include programmable simulation software. The drive electronics can include including the special-purpose electronic circuit (e.g., logic circuit) 49 and the controller on-board microprocessor 57. The logic (FIG. 1B), configured according to the present invention, wherein the special-purpose electronic circuit 49 is configured to performs the measurements and, the controller on-board microprocessor 57 directs the logic special-purpose circuit 49, and transfers the data to the general purpose computer 61. T, (2) the head assignments process can be implemented by on the controller on-board microprocessor 57 with within the disk drive 100 configured according to the present invention, the wherein a data collection sub-task is related to the head assignment task such that the data collection sub-task is performed by the logicspecial-purpose electronic circuit 49 within the disk drive 100. The, (3) the steps in each of the post-measurement data processing block 64, the format optimizer block 66 and the format generator block 68 can be implemented by on the general purpose computing equipment 61 (e.g., high end PC, PC server or workstation, etc., including programmable simulation software) configured according to the present invention.

The present invention has been described in considerable detail with reference to certain preferred versions thereof; however, other versions are possible. Therefore, the spirit and scope of the appended claims should not be limited to the description of the preferred versions contained herein.

**Abstract**

A method of defining ~~such a~~ storage format in ~~multiple~~ data storage devices, - each data storage device having ~~multiple~~ a plurality of storage media and a plurality of corresponding data transducer heads, each transducer head for recording on and playback of information from a corresponding storage media ~~um~~ in at least one zone, ~~wherein and~~ each zone including ~~es~~ a plurality of concentric tracks for recording on and playback of information. The method includes the ~~steps of:~~ selecting a sample of the a plurality of said data storage devices,; for each selected data storage device, measuring a record/playback performance capability of each head at one or more read/write frequencies per zone,; ~~based on said performance capability measurements,~~ generating storage density distributions corresponding to ~~at least a number of the heads in the~~ said selected data storage devices based on the performance capability measurements,; selecting a group of read/write frequencies for ~~the~~ said ~~multiple~~ data storage devices with, two or more frequencies for each zone, based on ~~the~~ said storage density distributions,; and assigning one of ~~the~~ said read/write frequencies to each head based on the performance capability of that head.



**SUBSTITUTE SPECIFICATION UNDER 37 C.F.R. 1.125**

**Per Zone Variable BPI for Improving Storage Device Capacity and Yield**

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**Field of the Invention**

The present invention relates to information storage on a storage media such as a disk in a disk drive.

**Background of the Invention**

Data storage devices such as disk drives are used in many data processing systems. Typically a disk drive includes a magnetic data disk having disk surfaces with concentric data tracks, and a transducer head paired with each disk surface for reading data from and writing data to the data tracks.

Disk drive storage capacity increases by increasing the data density (or areal density) of the data stored on the disk surfaces. Data density is the linear bit density on the tracks multiplied by the track density across the disk surface. Data density is measured in bits per square inch (BPSI), linear bit density is measured in bits per inch (BPI) and track density is measured in tracks per inch (TPI). As data density increases, the head performance distribution also increases which diminishes disk drive storage capacity and yield.

Conventional disk drives fail to account for the different capabilities of the head and disk surface pairs. Conventionally, each disk surface is formatted to store the same amount of data as every other disk surface. However, each head and disk surface pair has unique data recording capability, such as sensitivity

1 and accuracy, which depends on the fly height of the head over the disk surface,  
2 the magnetic properties of the head and the quality/distribution of the magnetic  
3 media for the disk surface. Thus, in conventional disk drives a head and disk  
4 surface pair that has a low error rate is formatted to the same BPI and TPI as a  
5 head and disk surface pair that has a high error rate.

6  
7 Conventional disk drive manufacturing applies a single error rate and a  
8 single data storage level for the head and disk surface pairs, and scraps disk  
9 drives that include a low performing head and disk surface pair that fails to meet  
10 the qualifying requirements. This lowers storage capacity due to inefficient use  
11 of high performing head and disk surface pairs that can store more data, and  
12 lowers yield due to disk drives being scrapped if they include a low performing  
13 head and disk surface pair even if they also include a high performing head and  
14 disk surface pair.

15  
16 U.S. Patent Nos. 6,091,559 and 5,596,458 provide different BPI on  
17 different disk surfaces, however these approaches do not take into consideration  
18 multiple constraints, including head performance across the stroke per disk  
19 surface, performance requirements such as throughput and manufacturing  
20 requirements such as test time. Instead, disk surface zone frequencies are  
21 selected based on a single metric for one head.

22  
23 There is, therefore, a need for storing data in a disk drive which improves  
24 disk drive storage capacity and yield and accounts for head performance  
25 variation.

### 26 27 **Summary of the Invention**

28 The present invention satisfies this need.  
29

1 In an embodiment, a variable BPI storage format is a function of zones in  
2 data storage devices, such as disk drives, based on head performance variation  
3 between different heads in a set of data storage devices.

4  
5 In another embodiment, a population of disk drives is selected, and head  
6 performance measurements are taken for disk surface locations at different  
7 frequencies. Head performance distributions obtained from the head  
8 performance measurements provide storage formats for the disks by determining  
9 different read/write frequencies for the zones, and the heads in each disk drive  
10 are assigned to the frequencies.

11  
12 The head allocations and assignments are per head per zone, taking into  
13 consideration head performance variation across the zones. For instance, if a  
14 first head performs well at the inner diameter (ID) of the disk but poorly at the  
15 outer diameter (OD) of the disk, and a second head has reverse performance,  
16 then the first head is assigned a high BPI at the ID and a low BPI at the OD, and  
17 the second head is assigned in the opposite fashion. The per zone variable BPI  
18 storage format improves storage capacity by taking several manufacturing and  
19 customer constraints into consideration. Performance of each head across the  
20 stroke of the disk surface, as well as performance variation from one head to  
21 another, determines the storage format and the head assignments.

22  
23 In another embodiment, the head performance and the storage format are  
24 determined off-line at development/design time, and then the heads are assigned  
25 to the different frequencies at manufacturing time. For example, the storage  
26 format for each zone and the number of heads allocated to each data density are  
27 preselected at design time, and then the heads are assigned to high/low data  
28 density storage formats at manufacturing time.

29  
30 In another embodiment, a method defines the storage format in data  
31 storage devices, with each data storage device having multiple storage media

1 and corresponding heads, each head for recording on and playback of  
2 information from a corresponding storage media in multiple zones, and each  
3 zone including concentric tracks for recording on and playback of information.  
4 The method includes (1) selecting a sample of the data storage devices, (2) for  
5 each selected data storage device, measuring a record/playback performance of  
6 each head at one or more read/write frequencies per zone, (3) generating head  
7 performance distributions based on the head performance measurements, (4)  
8 selecting a group of read/write frequencies for the data storage devices, two or  
9 more frequencies for each zone, based on the head performance distributions,  
10 and thereafter, during manufacturing, (5) assigning one of the read/write  
11 frequencies to each head based on the performance of that head.

12  
13 Advantageously, the present invention provides consistent performance  
14 (both sequential and random throughput) across a population of disk drives,  
15 improves storage capacity and yield and reduces test time.

#### 16 17 **Brief Description of the Drawings**

18 These and other features, aspects and advantages of the present  
19 invention will become understood with reference to the following description,  
20 appended claims and accompanying figures where:

21 FIG. 1A shows a disk drive with a data storage format;

22 FIG. 1B shows drive electronics for the disk drive;

23 FIG. 1C shows servo tracks and data tracks on a disk surface;

24 FIG. 1D shows a zone format in the disk drive with N disks, 2N heads and  
25 different heads in a zone on different disk surfaces;

26 FIG. 1E shows another zone format on a disk surface;

27 FIG. 1F shows zones on a disk surface that each include virtual cylinders;

28 FIG. 1G shows a data track format for the virtual cylinders in a zone on  
29 different disk surfaces with corresponding heads;

30 FIG. 1H shows a servo track and data track format for a zone on different  
31 disk surfaces with corresponding heads in which the number of servo tracks and

1 data tracks in different virtual cylinders of a zone on different disk surfaces are  
2 the same;

3 FIG. 1I shows another servo and data track format that varies from zone  
4 to zone on a disk surface;

5 FIG. 2A shows a function and flow diagram for generating the format of  
6 FIG. 1A;

7 FIG. 2B shows a graph of playback error measurement for a head at a  
8 zone at different recording frequencies;

9 FIG. 2C shows a histogram of the frequency capabilities of the heads in a  
10 set of disk drives at a zone at a fixed target error rate;

11 FIG. 2D shows a joint BPI distribution;

12 FIG. 3 shows a flowchart of vertical zoning data collection in FIG. 2A;

13 FIG. 4 shows a flowchart of vertical zoning and per zone joint BPI  
14 distribution extraction in FIG. 2A;

15 FIG. 5 shows a flowchart of head assignments in FIG. 2A; and

16 FIG. 6 shows a flowchart of format generation and optimization in FIG. 2A.

### 17 18 **Detailed Description of the Invention**

19 Data storage devices used to store data for computer systems include, for  
20 example, disk drives, floppy drives, tape drives, optical and magneto-optical  
21 drives and compact drives. Although the present invention is illustrated by way  
22 of a disk drive, the present invention can be used in other data storage devices  
23 and other storage media, including non-magnetic storage media, is as apparent  
24 to those of ordinary skill in the art and without deviating from the scope of the  
25 present invention.

26  
27 FIGs. 1A-1C show a hard disk drive 100 diagrammatically depicted for  
28 storing user data and/or operating instructions for a host computer 54. The disk  
29 drive 100 includes an electro-mechanical head-disk assembly 10 that includes  
30 one or more rotating data storage disks 12 mounted in a stacked, spaced-apart



1 relationship upon a spindle 13 rotated by a spindle motor 14 at a predetermined  
2 angular velocity.

3  
4 Each disk 12 includes at least one disk surface 23, and usually two disk  
5 surfaces 23 on opposing sides. Each disk surface 23 has associated magnetic  
6 media for recording data. The spindle motor 14 rotates the spindle 13 to move  
7 the disks 12 past the magnetic transducer heads 16 suspended by the  
8 suspension arms 17 over each disk surface 23. Generally, each head 16 is  
9 attached to a suspension arm 17 by a head gimbal assembly (not shown) that  
10 enables the head 16 to swivel to conform to a disk surface 23. The suspension  
11 arms 17 extend radially from a rotary voice coil motor 20. The voice coil motor  
12 20 rotates the suspension arms 17 and thereby positions the heads 16 over the  
13 appropriate areas of the disk surfaces 23 in order to read from or write to the disk  
14 surfaces 23. Because the disks 12 rotate at relatively high speed, the heads 16  
15 ride over the disk surfaces 23 on a cushion of air (air bearing).

16  
17 Each head 16 includes a read element (not shown) for reading data from a  
18 disk surface 23 and a write element (not shown) for writing data to a disk surface  
19 23. Most preferably, the read element is a magneto-resistive or giant magneto-  
20 resistive sensor and the write element is inductive and has a write width which is  
21 wider than a read width of the read element.

22  
23 Each disk surface 23 is divided into concentric circular data tracks 30 that  
24 each have individually addressable data sectors 35 in which user data is stored  
25 in the form of magnetic bits. The data sectors 35 are separated by narrow  
26 embedded servo sectors 25 arranged in radially extending servo spokes. The  
27 servo sectors 25 include a series of phase-coherent digital fields followed by a  
28 series of constant frequency servo bursts. The servo bursts are radially offset  
29 and circumferentially sequential, and are provided in sufficient numbers that  
30 fractional amplitude read signals generated by the head 16 from portions of at  
31 least two servo bursts passing under the head 16 enable the controller 57 to

1 determine and maintain proper position of the head 16 relative to a data track 30.  
2 A servo burst pattern for use with a head that includes a magneto-resistive read  
3 element and an inductive write element is described by commonly assigned U.S.  
4 Patent No. 5,587,850 entitled "Data Track Pattern Including Embedded Servo  
5 Sectors for Magneto-Resistive Read/Inductive Write Head Structure for a Disk  
6 Drive" which is incorporated herein by reference.

7  
8 The controller 57 controls the heads 16 to read from and write to the disk  
9 surfaces 23. The controller 57 preferably is an application specific integrated  
10 circuit chip (ASIC) which is connected by a printed circuit board 50 to other  
11 ASICs, such as a read/write channel 51, a motor driver 53 and a cache buffer 55.  
12 The controller 57 preferably includes an interface 59 which connects to the host  
13 computer 54 via a known bus 52 such as an ATA or SCSI bus.

14  
15 The controller 57 executes embedded or system software including  
16 programming code that monitors and operates the disk drive 100. During a read  
17 or write operation, the host computer 54 determines the address where the data  
18 is located in the disk drive 100. The address specifies the head 16, the data  
19 track 30 and the data sector 35. This data is transferred to the controller 57  
20 which maps the address to the physical location in the disk drive 100, and in  
21 response to reading the servo information in the servo sectors 25, operates the  
22 voice coil motor 20 to position the head 16 over the corresponding data track 30.  
23 As the disk surface 23 rotates, the head 16 reads the servo information  
24 embedded in each servo sector 25 and also reads an address of each data  
25 sector 35 in the data track 30.

26  
27 During a read operation, when the identified data sector 35 appears under  
28 the head 16, the entire contents of the data sector 35 containing the desired data  
29 is read. In reading data from the disk surface 23, the head 16 senses a variation  
30 in an electrical current flowing through the read element when it passes over an  
31 area of flux reversals on the disk surface 23. The flux reversals are transformed

1 into recovered data by the read/write channel 51 in accordance with a channel  
2 algorithm such as partial response, maximum likelihood (PRML). The recovered  
3 data is then read into the cache buffer 55 where it is transferred to the host  
4 computer 54. The read/write channel 51 most preferably includes a quality  
5 monitor which measures the quality of recovered data and provides an indication  
6 of the data error rate. One channel implementation which employs channel error  
7 metrics is described in commonly assigned U.S. Patent No. 5,521,945 entitled  
8 "Reduced Complexity EPR4 Post-Processor for Sampled Data Detection" which  
9 is incorporated herein by reference. The present invention uses the indication of  
10 recovered data error to select linear bit density, track density and/or error  
11 correction codes.

12  
13 During a write operation, the host computer 54 remembers the address for  
14 each file on the disk surface 23 and which data sectors 35 are available for new  
15 data. The controller 57 operates the voice coil motor 20 in response to the servo  
16 information read back from the servo sectors 25 to position the head 16, settles  
17 the head 16 into a writing position, and waits for the appropriate data sector 35 to  
18 rotate under the head 16 to write the data. To write data on the disk surface 23,  
19 an electrical current is passed through a write coil in the inductive write element  
20 of the head 16 to create a magnetic field across a magnetic gap in a pair of write  
21 poles that magnetizes the disk surface 23 under the head 16. When the data  
22 track 30 is full, the controller 57 moves the head 16 to the next available data  
23 track 30 with sufficient contiguous space for writing data. If still more track  
24 capacity is required, another head 16 is used to write data to a data sector 35 of  
25 another data track 30 on another disk surface 23.

26  
27 The present invention increases the storage capacity and yield of data  
28 storage devices, such as the disk drive 100, having magnetic media surfaces,  
29 such as the disk surfaces 23.

## 1    Vertical Zoning

2            In every disk drive, there is a distribution associated with the head and  
3    disk surface pair performance. The present invention takes advantage of that  
4    distribution to determine different linear bit density (BPI) recording frequency  
5    assignments for the heads, and optionally track allocation.

6  
7    A set of disk drives is selected, and head performance measurements are taken  
8    for each selected disk surface location in the disk drives at different frequencies.  
9    Empirical frequency capability histograms are extracted at a target performance  
10   metric from the measurement data. Head performance distributions (such as  
11   joint BPI distributions) are estimated from the histograms and fed into a format  
12   optimizer to obtain and design vertically zoned frequency format profiles across  
13   the stroke and the disk surface as well as the optimal number of head allocations  
14   to the frequencies. Once the frequency format profiles and the optimal number  
15   of head allocations are determined, during a test process, every head at every  
16   zone is assigned to one of the frequencies based on the head's performance.

17  
18           FIG. 1A shows a storage format for the disk drive 100. Each disk surface  
19   23 includes zones 60 that extend from one radius of the disk 12 to another radius  
20   of the disk 12, and the format of the zones 60 on each disk surface 23 is the  
21   same. The variable BPI storage format is a function of the zones 60 on each  
22   disk surface 23 based two data recording formats -- high data density and low  
23   data density -- that use (1) head performance variation from one head 16 to the  
24   next head 16 in the disk drive 100, and (2) the performance variation of a given  
25   head 16 across the stroke of a disk surface 23.

26  
27           The disk drive 100 includes the disks 12 depicted as disks 1 to N, the  
28   heads 16 depicted as heads 1 to 2N, and the disk surfaces 23 depicted as disk  
29   surfaces 1 to 2N. Each disk 12 includes two opposing disk surfaces 23, and  
30   each head 16 is associated with one of the disk surfaces 23. For instance, head  
31   1 is associated with disk surface 1 of disk 1, head 2 is associated with disk

surface 2 of disk 1, head 3 is associated with disk surface 3 of disk 2, and head 2N is associated with disk surface 2N of disk N.

Each disk surface 23 includes the zones 60 depicted as zones 1 to M across its stroke, with zone 1 at the ID and zone M at the OD. The radial boundaries on zone 1 of disk surface 1 of disk 1 are the same as the radial boundaries of zone 1 on disk surface 2 of disk 1, and so on. Similarly, the radial boundaries of zone M on disk surface 1 of disk 1 are the same as the radial boundaries of zone M on disk surface 2 of disk 1, and so on. However, different zones 60 across the stroke on each disk surface 23 need not necessarily have the same number of data tracks 30 or TPI. For example, zone 1 on disk surface 1 of disk 1 has the same number of data tracks 30 and the same radial boundaries as zone 1 on disk surface 1 of disk N, and zone M on disk surface 1 of disk 1 has the same number of data tracks 30 and the same radial boundaries as zone M on disk surface 1 of disk N. However, the number of data tracks 30 in zones 1 and M can be different.

Each disk surface 23 also includes virtual cylinders 39 depicted as virtual cylinders 1 to n. Each zone 60 includes multiple virtual cylinders 39, and each virtual cylinder 39 includes multiple data tracks 30 on each disk surface 23. Further, within a virtual cylinder 39, different heads 16 may read and write at different frequencies (variable BPI) to provide vertical zoning.

FIG. 1C shows the data tracks 30 and the servo tracks 37 on the disk surface 23. The data tracks 30 include the data sectors 35, and the servo tracks 37 include the servo sectors 25. Five servo tracks 37 depicted as servo tracks Sa, Sb, Sc, Sd and Se are shown in relation to three data tracks 30 depicted as data tracks Tk1, Tk2 and Tk3.

The servo tracks 37 are written on the disk surface 23 during manufacturing at a servo track density that is about 150% of the maximum data

1 track density. The servo track density is determined by the maximum read width  
2 and the minimum write width of a population of the heads 16. After writing the  
3 servo tracks 37 at the servo track pitch, the data tracks 30 can be written at any  
4 radial position between the servo tracks 37. The data track density (TPI) can be  
5 selected from predetermined levels or can be based on the location of a data  
6 sector 35. Additional tests can be performed to determine the optimum data  
7 track density of the disk surface 23. Each servo track 37 comprises radially  
8 similarly situated servo sectors 25 in the servo spokes. For example, the servo  
9 track Se contains servo sectors 25 at essentially the same radial distance from  
10 the center of the disk 12, the servo track Sd contains servo sectors 25 at  
11 essentially the same radial distance from the center of the disk 12, etc.

12  
13 FIGs. 1D to 1I show vertical zone formats in which different heads 16 on  
14 different disk surfaces 23 may read/write at different linear frequencies (variable  
15 BPI) on the data tracks 30 within a virtual cylinder 39.

16  
17 FIG. 1D shows a zone 60 format of the disk drive 100 with N disks 12, 2N  
18 heads 16 and different heads 16 in zone 1 on different disks 12. FIG. 1E shows  
19 another zone 60 format on the disk surface 23. FIG. 1F shows each zone 60 on  
20 the disk surface 23 includes multiple virtual cylinders 39. Zone 1 includes virtual  
21 cylinders 1 to j, and zone M includes virtual cylinders 1 to i. The radial  
22 boundaries of the zones 60 are shown as dark circles, and the radial boundaries  
23 of the virtual cylinders 39 are shown as light circles. FIG. 1G shows a data track  
24 30 format for the virtual cylinders 39 in a zone 60 on different disk surfaces 23  
25 with corresponding heads 16. FIG. 1H shows a data track 30 and servo track 37  
26 format for a zone 60 on different disk surfaces 23 with corresponding heads 16 in  
27 which the number of data tracks 30 and servo tracks 37 in different virtual  
28 cylinders 39 of a zone 60 on different disk surfaces 23 is the same. FIG. 1I  
29 shows a data track 30 and servo track 37 format for zones 60 on the disk surface  
30 23 with a corresponding head 16 in which the data track 30 and servo track 37  
31 format varies from zone 1 to zone M.

1

2 Format Optimization

3       The vertical zoning includes designing, optimizing and selecting two or  
4 more recording frequency profiles per zone for a sample number of disk drives  
5 off-line during the disk drive development/design phase. Then, for a population  
6 of disk drives, in each disk drive, each head is assigned to one of the  
7 predetermined frequencies for a given zone during the disk drive manufacturing  
8 phase. A predetermined read/write frequency (BPI) is assigned to each head  
9 based on a known number of head allocations and the head's performance. A  
10 head assigned to a high frequency records more bits on a track, and a head  
11 assigned to a low frequency records less bits on a track.

12

13       Performance testing of the head and disk surface pairs occurs after full  
14 read/write and servo calibration and optimization of the disk drive. If the tested  
15 performance of head 1 at zone 1 on disk surface 1 of disk 1 at a given frequency  
16 is better than a target performance metric, then head 1 is considered strong  
17 since it is capable of storing more information than originally accounted for.  
18 Thus, the recording frequency can be increased at zone 1 on disk surface 1 of  
19 disk 1 for head 1 yet the performance does not fall below the target performance  
20 metric. If the tested performance of head 2 at zone 1 on disk surface 2 of disk 1  
21 at the same frequency is worse than a target performance metric, then head 2 is  
22 considered weak but can be compensated for by relaxing the frequency at which  
23 head 2 operates to ensure the target performance metric is met. Performing the  
24 above trade-off between the heads for all the zones provides frequency profiles  
25 across the stroke that are vertically zoned frequency format profiles without loss  
26 of storage capacity.

27

28       Advantageously, by compensating for head 2, rather than failing the disk  
29 drive due to head 2, the vertical zoning improves yield. Furthermore, the format  
30 optimizer uses the head performance (read/write frequency capability)  
31 distributions at every zone and a target performance metric to design a group of

1 read/write frequency format profiles for strong and weak heads within a given  
2 disk drive. The format optimizer also determines the optimal number of strong  
3 versus weak heads.

4  
5 The format optimizer does not determine which specific head is at the high  
6 or low frequency, but does provide a breakdown of the number of heads at the  
7 high frequency and the number of heads at the low frequency. The breakdown is  
8 fixed, performed off-line, and used during the head assignments. Then, in the  
9 head assignments during a manufacturing test, out of  $2N$  heads in a disk drive  
10 with  $N$  disks, the number of heads assigned to each predetermined frequency is  
11 determined.

12  
13 The heads within a set of disk drives are allocated to the predetermined  
14 group of read/write frequencies-as part of the optimization process to meet the  
15 storage capacity and yield requirements for the disk drives. The allocation  
16 process allocates a number of the heads in a disk drive to the predetermined  
17 frequencies, however the specific assignment of a particular head to a particular  
18 frequency is performed later during the assignment process. For example, in a  
19 two read/write frequency design (high frequency and low frequency) for a set of  
20 disk drives each with eight heads, in each disk drive for zone 1 on all the disk  
21 surfaces, any five of the eight heads are allocated to the high frequency and any  
22 three of the eight heads are allocated to the low frequency based on the  
23 performance measurements of the heads in the set of the disk drives.  
24 Thereafter, the specific assignment of each particular head to a particular  
25 predetermined frequency is performed. For example, in a first disk drive heads  
26 2, 5, 6, 7, 8 are assigned to the high frequency and heads 1, 3, 4 are assigned to  
27 the low frequency, whereas in a second disk drive heads 1, 4, 5, 6, 7 are  
28 assigned to the high frequency and heads 2, 3, 8 are assigned to the low  
29 frequency. The specific head assignments depend on the specific capability of  
30 the heads in each disk drive.



1           The optimal number of heads per frequency is determined at the same  
2 time that the group of read/write frequencies are selected by the format optimizer  
3 by solving a joint constrained optimization problem. For example, in a disk drive  
4 with eight heads and a high frequency and a low frequency that are each a  
5 different ratio of a reference frequency, in each vertical zone, allocating two  
6 heads to the high frequency and six heads to the low frequency provides a  
7 specific storage capacity. Changing the frequency ratios and the number of  
8 heads allocated to each frequency provides a different storage capacity. Thus,  
9 the disk drive storage capacity is a function of the number of heads multiplied by  
10 the frequency allocated to each head per zone. For example, if a nominal disk  
11 surface data storage is 1 unit, and if the high frequency =  $4/3 \times$  the reference  
12 frequency and the low frequency =  $2/3 \times$  the reference frequency, then one head  
13 can be at the high frequency for every one head at the low frequency to maintain  
14 the average disk surface data storage at 1 unit.

15  
16           The head performance distributions represent percentages of the heads in  
17 the disk drives that can operate at different frequencies. For example, the head  
18 performance distribution is a BPI distribution that represents the head frequency  
19 capability at a target performance metric. Using the head performance  
20 distributions (the head read/write frequency capability distributions at the target  
21 performance metric for every zone), the number of heads, the format of the  
22 virtual cylinders and the desired storage capacity, the format optimizer  
23 determines the frequency for each virtual cylinder in each zone and the number  
24 of heads in each disk drive allocated to each frequency to achieve the desired  
25 storage capacity. Thereafter, in the assignment process as part of testing each  
26 disk drive, each head in a population of disk drives is assigned to one of the  
27 predetermined frequencies based on the allocation criteria and the specific head  
28 performance. For example, in a disk drive with four heads, the format optimizer  
29 considers three heads at the high frequency and one head at the low frequency,  
30 then two heads at the high frequency and two heads at the low frequency, and  
31 then one head at the high frequency and three heads at the low frequency.

1 Thus, the format optimizer uses the head performance distributions to determine  
2 the storage capacity and yield.

3  
4 In one version of the optimization process, the yield is maximized while  
5 meeting a constraint on storage capacity. In another version, the storage  
6 capacity is maximized while meeting a constraint on yield. In the former case,  
7 the format optimizer uses a format where the maximum number of disk drives  
8 qualify and the fewest number of disk drives fail to reach the required storage  
9 capacity. For example, in a disk drive with four heads and a nominal disk surface  
10 data storage of 1 unit, allocating two heads to the high frequency and two heads  
11 to the low frequency provides a nominal data storage of 4 units. In the later  
12 case, the format optimizer uses a format where the maximum number of disk  
13 drives reach the required storage capacity and the fewest number of disk drives  
14 fail to qualify. For example, in a disk drive with four heads and a nominal disk  
15 surface data storage of 1 unit, allocating three heads to the high frequency and  
16 one head to the low frequency provides a high data storage of 4.66 units.

17  
18 Thus, the vertical zoning for variable BPI includes an off-line  
19 predetermined per zone format design based on disk drive data collection and  
20 head performance distribution extraction. In one version, a fixed predetermined  
21 zone boundary format is used to design multiple frequency BPI formats based on  
22 representative or actual joint BPI distributions at one or more desired target  
23 performance metrics (such as off-track symbol error rate) and the joint BPI  
24 distributions are extracted from a finite preselected set of disk drives.

25  
26 The collected data is used to extract the joint BPI distributions for the  
27 heads at every preselected zone, and the per zone design of high and low data  
28 density formats for the heads is performed off-line. The format optimizer solves a  
29 constrained joint optimization off-line to obtain the format designs using well-  
30 known constrained optimization routines. Using joint BPI distributions allows  
31 consideration of potential correlation of BPI capability of the heads across the

1 stroke as well as the individual contribution of each head to the storage capacity  
2 and yield.

3  
4 The off-line format design allows the format optimizer to consider  
5 additional constraints. For example, as more information is obtained in  
6 quantifying the thermal stability constraints of the disks (which in turn places an  
7 upper bound on linear bit density for the heads) the off-line format design does  
8 not exceed these constraints. Likewise, if there are data rate constraints in either  
9 the write process or the ASICs, such constraints may be cast within the joint  
10 constrained format optimizer to ensure the constraints are not exceeded.

#### 11 12 Data Measurement

13 A measurement procedure is used to collect data from which one-  
14 dimensional (1D), two-dimensional (2D) and three-dimensional (3D) BPI  
15 distributions at a desired read/write target error rate (or any other metric) can be  
16 extracted. Data is collected based on head capability measurements taken at  
17 different radial positions on the disk. The distributions represent the capability of  
18 each head at different radial positions. For example, several disk drives which  
19 collectively include 1000 heads are selected for measurement, and  
20 record/playback error rate measurements of the 1000 heads from zone 1 to zone  
21 24 of the disk surfaces at different frequencies are obtained. Thereafter, in post-  
22 measurement data processing (a) the BPI capability of each head at a fixed  
23 target performance metric at zone 1 is determined to obtain a 1D BPI distribution,  
24 (b) the BPI capability of each head at a fixed target performance metric at zones  
25 1 and 5 is determined to obtain a 2D BPI distribution, and (c) the BPI capability of  
26 each head at a fixed target performance metric at zones 1, 5 and 20 is  
27 determined to obtain a 3D BPI distribution.

28  
29 The BPI distributions are then passed to the format optimizer to solve  
30 three constrained optimization problems to provide head frequency per zone  
31 allocations. The three constrained optimization problems (1) maximize the yield

1 while preserving the storage capacity, (2) maximize the storage capacity while  
2 preserving the yield, and (3) maximize the yield while ensuring a target storage  
3 capacity is met at a fixed target TPI. Customer related or ASIC data rate  
4 constraints are also considered. The format optimizer can solve any of these  
5 three problems, and one problem can take priority over another depending on the  
6 process phase. For example, at an early development phase where the disk  
7 drive components are not mature, meeting the storage capacity may be a  
8 challenge. In that phase, the format optimizer can design the variable BPI format  
9 profiles by solving the second problem. Then, as the disk drive components  
10 mature, meeting the storage capacity becomes easier and meeting the yield  
11 becomes more important, the first problem may be solved. Thereafter, as part of  
12 a test process, an assignment algorithm ensures the appropriate head  
13 assignments to the predetermined high and low data density formats per head  
14 and per zone or across the stroke based on the head allocation breakdown of the  
15 format optimizer.

16  
17 The yield is improved while meeting the target storage capacity by  
18 allowing a frequency format with high and low frequencies and a predetermined  
19 number of high and low performing head allocations. Using realistic constraints  
20 such as ASIC data rate limitations, the same fixed target TPI is maintained by  
21 increasing the average target BPI across the stroke to achieve the target storage  
22 capacity. As such, head performance variation from one head to the next head  
23 in the disk drive and for the head across the stroke of the disk surface is used to  
24 increase the storage capacity while preserving the yield. For example, the  
25 vertical zoning format uses several design constraints to improve yield using a  
26 variable high and low BPI design with a fixed predetermined number of head  
27 allocations as a function of the zones while meeting the target storage capacity at  
28 a fixed target TPI. The head performance variation or correlation across the  
29 stroke is also used.

1 Further, the difference in data storage of two or more zones on a disk  
2 surface is considered as it affects storage capacity. The storage capacity is  
3 defined as a weighted combination of the zone capacities across the stroke on  
4 each disk surface in the disk drive. A correlation in the head performance  
5 statistics is extracted from one head to another head, and for every head  
6 considered in a set of disk drives across the stroke on each disk surface.

7  
8 The joint constrained optimization determines a per zone target high and  
9 low data density format. The optimization takes into account constraints  
10 including customer related requirements such as minimum logical block count,  
11 monotonic data rate, and maximum data rate at the outer zones which can be  
12 formulated into additional constraints.

#### 13 14 Example Implementation

15 FIG. 2A shows a function and flow diagram for generating the optimal data  
16 density format shown in FIG. 1A. The function and flow diagram includes a data  
17 measurer 62, a post-measurement data processor 64, a format optimizer 66 and  
18 a format generator 68.

#### 19 20 Data Measurer

21 The data measurer 62 takes data measurements for every zone at a finite  
22 number of frequency samples.

23  
24 The data measurer 62 implements a measurement procedure that  
25 includes the steps of:

26 (1) Create several different predetermined linear bit density format  
27 profiles including a profile of different frequencies per zone across the stroke,  
28 such as a first profile including high frequency 1 for zone 1, high frequency 2 for  
29 zone 2 . . . high frequency M for zone M, and a second profile including low  
30 frequency 1 for zone 1, low frequency 2 for zone 2 . . . low frequency M for zone  
31 M to be loaded on a representative number of disk drives selected for the

1 measurement process (or if possible on all the available disk drives for that  
2 build);  
3 (2) Load a frequency format profile;  
4 (3) Perform read/write and servo optimization and calibration;  
5 (4) Take head performance measurements including off-track mean  
6 square error or quality metric and/or symbol error rate at preselected frequencies  
7 for preferably all available zones and save the data; and  
8 (5) Repeat steps 2-4 for the remaining frequency format profiles.  
9

10 The above steps are performed for the selected disk drives in the  
11 measurement process.  
12

13 Thus, in the disk drive 100, the data is recorded on a data sector 35 of the  
14 disk surface 23 at the selected data density by positioning the head 16 abutting  
15 the data sector 35 and sending the appropriate write signals to the head 16.  
16 Typically, a sample of data is recorded on the disk surface 23 such that a  
17 significant number of errors are detected (such as ten errors per error rate  
18 measurement) to obtain a statistically representative sampling of the error rate  
19 for the data sector 35. Thereafter, the recorded data is read by the head 16 and  
20 stored by the host computer 54 for evaluation. An error rate of the recorded data  
21 is measured or compiled by comparing the written data with the read data,  
22 element-by-element. The error rate can be determined using a bit error  
23 measurement in which a bit of data read from the disk surface 23 is compared  
24 with the correct bit, a bit stream measurement in which a bit stream of data read  
25 from the disk surface 23 is compared with a correct bit stream, or a mean square  
26 error metric measurement in which a waveform read from the disk surface 23 is  
27 compared with an ideal waveform to provide an error signal that is squared and  
28 summed to form the error metric.  
29

30 In this description, a component distribution is defined as a random  
31 variation (tolerance) of a prespecified target nominal component parameter such

1 as a head write/read width, and a distribution is defined as a probability  
2 distribution function. During the early product development, when the head  
3 performance distributions are wide and unreliable, data from a mature set of disk  
4 drives is used for extracting reference joint BPI distributions at a target  
5 performance metric such as on-track symbol error rate, off-track symbol error  
6 rate, on-track mean square error or off-track mean square error. Later, when the  
7 head performance variation from one phase to the next in the distribution is  
8 expected to be minimal, new sets of measurement data are collected using a  
9 selected population of disk drives at their more mature stages.

10  
11 Thus, a number of BPI formats including the nominal target format are  
12 selected. Then, on-track or off-track symbol error rate or mean square error  
13 measurements are taken at different preselected locations of the disk surfaces,  
14 such as the outer, middle and inner zones. The performance measurements can  
15 be limited to these three zones to reduce the measurement time. However,  
16 preferably the performance measurements over multiple zones and other  
17 measurements such as off-track 747 can be performed. The nominal formats are  
18 generated from the data.

19  
20 Two or more different linear bit density format profiles can be loaded at a  
21 time. In one example, two variable BPI format per zone design (high and low  
22 data density format profiles) can be created for measurement data collection  
23 during every build. In this way, more statistical data can be collected from more  
24 disk drives, however there will be only two frequency samples per zone available  
25 for post-measurement data processing.

#### 26 27 Post-Measurement Data Processor

28 Post-measurement data processor 64 uses the available performance  
29 metric measurements to calculate each head's frequency performance, for  
30 instance as kilo flux per inch (kFCI) or kilo bits per inch (kBPI), at a target

1 performance metric. The performance of every head at every zone is determined  
2 as a function of the read/write frequency profiles used for the measurements.

3  
4 For example, if six different frequency profiles are used, then for every  
5 head per zone, the data measurer 62 provides measured data as a function of  
6 six frequency samples at a target performance metric. In the post-measurement  
7 data processor 64, the measured data is sorted and the performance of every  
8 head at every zone at the six frequency samples is extracted to generate  
9 frequency capability histograms at a target performance metric.

10  
11 FIG. 2B shows a graph of playback error measurement for a head at a  
12 zone at different recording frequencies. The curve shows head performance as  
13 a function of frequency (BPI). The x-axis is the read/write frequency in kBPI at  
14 the outer diameter, and the y-axis is the on-track symbol error rate on a log  
15 scale. Each frequency sample 70 is depicted as "+", each curve fit point 72 is  
16 depicted as "o" and each projected frequency 74 is depicted as "◇".

17  
18 In the illustration, head 1 at zone 1 in disk drive 3 is measured at six  
19 frequency samples. The curve is generated using a least square polynomial fit to  
20 the six frequency samples. The projected frequency (BPI) for a target on-track  
21 symbol error rate is extracted from the curve by interpolation or extrapolation.  
22 For example, if the target on-track symbol error rate is  $10^{-8}$  then the projected  
23 frequency is determined by interpolation, whereas if the target on-track symbol  
24 error rate is  $10^{-6}$  then the projected frequency is determined by extrapolation.  
25 The on-track symbol error rate varies as a function of frequency and increases as  
26 the frequency increases.

27  
28 The nominal kBPI (before vertical zoning) and the kBPI gain relative to the  
29 nominal kBPI are also shown. Head 1 can be classified as a strong head  
30 because there is reasonably significant margin before its on-track symbol error  
31 rate of  $-9.1$  (log) at a nominal frequency/kBPI of  $\sim 188$  can be changed to a



1 projected on-track symbol error rate of  $-6.22$  at a frequency/kBPI of  $\sim 217$ .  
2 Hence, there is a total kBPI gain of  $\sim 29$ , allowing the nominal frequency to  
3 increase by 15% while meeting the target on-track symbol error rate performance  
4 metric of  $6 \times 10^{-7}$ . Thus, head 1 of disk drive 3 has a frequency capability of about  
5 217 at the target on-track symbol error rate of  $6 \times 10^{-7}$ , which provides a sample  
6 for the generation of a histogram.

7  
8 FIG. 2C shows a histogram of the frequency capabilities of the heads in a  
9 set of disk drives at a zone at a target performance metric. The histogram 76 is  
10 constructed using the projected frequencies determined in FIG. 2B for the heads  
11 in the selected disk drives reading from zone 1 at the target on-track symbol error  
12 rate of  $6 \times 10^{-7}$ . The x-axis is the projected frequency capability at the outer  
13 diameter, and the y-axis is the number of heads. The histogram is extracted and  
14 empirical, has a normal distribution fit and has a width that corresponds to the  
15 head performance variation.

16  
17 Additional histograms are constructed for the remaining zones based on  
18 the frequency capabilities determined from the graphs based on the performance  
19 measurements taken at the remaining zones so that every available head  
20 considered in the disk drives under measurement has BPI histograms at a target  
21 performance metric per zone.

22  
23 Thus, performance measurements are provided for each head at each  
24 zone in the selected disk drives, the graphs are generated for each head at each  
25 zone, the frequency capabilities for each head at each zone are determined for a  
26 target performance metric, and the histograms are constructed for each head at  
27 each zone for the target performance metric. Likewise, if a histogram of head  
28 BPI capability at a target performance metric of a zone (such as an intermediate  
29 zone) is not available then the histogram for that zone can be constructed by  
30 interpolation or extrapolation. The histograms can be used to estimate a BPI  
31 distribution.

1

2           FIG. 2D shows a joint BPI distribution calculated from the histograms of  
3 the heads in the measured disk drives at a target performance metric. The joint  
4 BPI distribution is a 2D distribution based on the histograms in FIG. 2C at the  
5 target on-track symbol error rate of  $6 \times 10^{-7}$ . The x-axis is the BPI capability of the  
6 heads at the middle diameter (MD) of the disks, the y-axis is the BPI capability of  
7 the heads at the outer diameter (OD) of the disks, and the z-axis is the calculated  
8 number of heads divided by the total number of heads. The joint BPI distribution  
9 provides an estimate of the probability that the heads meet the target  
10 performance metric at the MD and the OD.

11

12           The joint BPI distribution may predict, for example, that 10% of the heads  
13 in the measured disk drives can operate at a high frequency of 1.5 x the  
14 reference frequency, 50% of the heads can operate at a high frequency of 1.25 x  
15 the reference frequency, 90% of the heads can operate at the reference  
16 frequency, and 99.9% of the heads can operate at a low frequency of 0.75 x the  
17 reference frequency.

18

19           For example, the linear bit density sensitivity of every head at zone K  
20 (where K ranges from 1 to M) at the six frequency samples is determined. If  
21 frequency 1K, frequency 2K . . . frequency 6K are the frequency samples at zone  
22 K, every head is positioned on the same track in zone K and the record/playback  
23 performance of each head is measured at every frequency sample using a target  
24 performance metric.

25

26           The BPI distributions can be calculated at the target performance metric  
27 as 1D, 2D or 3D distributions that are marginal, individual or per zone  
28 distributions, respectively. The format optimizer uses the estimated frequency  
29 capability BPI distributions for every zone at the target performance metric to  
30 determine the storage capacity and yield.

31

1    Format Optimizer

2           The format optimizer 66 provides variable BPI optimization. The format  
3 optimizer 66 solves three constrained optimization problems in response to  
4 various inputs. The first problem maximizes the yield while preserving the  
5 storage capacity, the second problem maximizes the storage capacity while  
6 preserving the yield, and the third problem maximizes the yield while reducing  
7 the track density and meeting the storage capacity. The inputs include the  
8 number of different read/write frequencies (frequency profiles or formats), the  
9 number of heads in each disk drive, the BPI distributions, and the nominal  
10 storage capacity. The BPI distributions indicate the frequency capability  
11 distribution of the heads at a target performance metric.

12  
13       The format optimizer 66 simultaneously searches through a continuous range of  
14 all possible frequency capabilities to maximize the yield such that the nominal  
15 storage capacity is met. The format optimizer 66 can also perform the same  
16 operation with the storage capacity and the yield interchanged.

17  
18       The format optimizer 66 can optimize high and low data density as a  
19 function of the zones. For example, in a disk drive with eight heads, the  
20 possibilities are one head at high data density and seven heads at low data  
21 density, two heads at high data density and six heads at low data density, three  
22 heads at high data density and five heads at low data density, four heads at high  
23 data density and four heads at low data density, one head at low data density  
24 and seven heads at high data density, two heads at low data density and six  
25 heads at high data density, and three heads at low data density and five heads at  
26 high data density. The format optimizer 66 considers all the combinatorial  
27 possibilities, in each case solves a constrained optimization problem and  
28 chooses the optimal solution among the possibilities. Alternatively, the format  
29 optimizer 66 can reach the optimal solution more directly by non-linear mixed-  
30 integer programming.

1           Therefore, once the 1D, 2D and 3D BPI distributions at a target  
2 performance metric are passed to the format optimizer 66, the format optimizer  
3 66 solves two problems, (1) maximizing or improving the yield due to the target  
4 performance metric while meeting the desired nominal storage capacity, and (2)  
5 maximizing the storage capacity while meeting the desired nominal yield.

6  
7           The format optimizer 66 mathematically casts these two problems as  
8 constrained optimization problems and solves them using well-known  
9 optimization techniques such as a line search algorithm. The constrained  
10 optimization problems can also be cast as non-linear mixed-integer programming  
11 and solved using existing optimization methods. Example constraints to be  
12 considered, and cast mathematically within the format optimizer 66, include not  
13 exceeding a certain frequency at the outer diameter due to ASIC data rate  
14 limitations or at the inner diameter due to head/disk limitations. Furthermore,  
15 closed form equations are derived and used in the format optimizer 66 to  
16 estimate the storage capacity and yield. The format generator 66 also considers  
17 possible overhead such as adding redundant bits due to error correction coding  
18 or gray coding.

19  
20           The format optimizer 66 also uses information from the format generator  
21 68 such as the calculated format efficiency per zone (defined in percentages as  
22 the amount of user data in blocks that can fit in all tracks in a zone), or the  
23 number of tracks per zone, to achieve a very close estimate of the storage  
24 capacity determined by the format generator 68. Then, the format optimizer 66  
25 calculates optimal linear bit density format profiles as well as the optimal number  
26 of heads allocated to each vertically zoned format profile.

27  
28           For example, histograms are extracted and the corresponding BPI  
29 distributions are estimated for different zones at the target on-track symbol error  
30 rate of  $6 \times 10^{-7}$ . A format design is provided for a disk drive with four heads and  
31 two frequencies to optimize yield while meeting storage capacity.

1

2           For example, the format optimizer 66 uses the 1D, 2D and 3D BPI  
3 distributions at the target performance metric to jointly optimize for vertically  
4 zoned frequency format profiles and the corresponding number of head  
5 allocations three zones at a time. An advantage of considering three zones  
6 instead of one zone, and thus joint optimization instead of individual optimization,  
7 is that the joint optimization allows the frequency profiles to be optimized across  
8 the stroke on each disk surface. Therefore, joint optimization exploits the  
9 potential correlation in performance from one zone to another zone as well as  
10 their individual and weighted contribution to the storage capacity. Joint  
11 optimization is preferable for a high/low data density format across the stroke for  
12 either improving the yield while keeping the same storage capacity or improving  
13 the storage capacity while preserving the yield.

14

15           The format optimizer 66 generates the target high/low BPI formats per  
16 zone, the optimal number of head allocations per format, and an estimate of the  
17 storage capacity and yield. The accuracy of the estimates can be sensitive to the  
18 underlying BPI distributions at the target performance metric. Further, the target  
19 high/low BPI formats can be sensitive to the variance of the BPI distributions.  
20 And, the variance of the BPI distributions can be sensitive to the absolute value  
21 of the target performance metric and the type of target performance metric. In  
22 addition, the target high/low BPI formats are designed three zones at a time and  
23 the yield improvement while preserving the storage capacity is based on the  
24 profile of the target nominal formats. The format optimizer 66 also allows for  
25 smoothing the target variable BPI format designs. The format generator 68  
26 determines the number of tracks per zone, the number of blocks per track, the  
27 radius at each zone, as well as block and track format efficiency. This  
28 information is saved in output files for use with the format optimizer 66. The  
29 format optimizer 66 then saves the target high/low BPI formats per zone that it  
30 generates in two separate files that can be loaded into the format generator 68.

31

1           Once the target format profiles are calculated, if they are non-smooth  
2 across the stroke, optionally a smoothing process is applied. The format profiles  
3 are then loaded into the format generator 68 to create vertically zoned formats  
4 and configuration pages. The formats and configuration pages are used by the  
5 disk drive firmware to create binary files to be loaded into the reserve image of  
6 the disk drives as part of the file system. In this fashion, the design and  
7 implementation of the format profiles as well as the number of optimal head  
8 allocations are performed off-line and are predetermined for every disk drive  
9 configuration.

10  
11           For example, in a disk drive with four heads and four disk surfaces on two  
12 disks, the format optimizer 66 designs vertically zoned high and low frequency  
13 profiles. Every disk surface is uniformly partitioned into three zones across the  
14 stroke, at a track density with a fixed number of tracks per zone, vertically aligned  
15 from one disk surface to another. The nominal disk surface data storage before  
16 the vertical zoning can be approximated by the sum over all the zones of the  
17 nominal tracks per zone multiplied by the nominal BPI per track multiplied by the  
18 format efficiency per zone. Format efficiency per zone is the percentage of the  
19 user data that is effectively stored per zone. The nominal storage capacity is the  
20 nominal disk surface data storage multiplied by the total number of disk surfaces  
21 (or heads). The nominal number of tracks per zone and the format efficiency per  
22 zone can be generated by the format generator 68.

23  
24           Performing vertical zoning to improve the yield without losing storage  
25 capacity finds the best frequency per zone and per head such that the disk drive  
26 meets performance and storage capacity requirements. If a disk drive with four  
27 heads fails due to the performance of head 1 at zone 1, but the performance of  
28 another head/zone pair, such as head 1 at zone 2 or head 3 at zone 1, is  
29 significantly better, passing the tests with reasonable margins, then a higher than  
30 nominal frequency at zone 1 or zone 2 is designed for the strong heads and the  
31 frequency at zone 1 for the weak head is lowered. This trade-off obtains a

1 vertically zoned design of variable frequencies per zone such that the storage  
2 capacity is preserved. In addition, the number of heads per zone allocated to  
3 high or low data density is determined. Thus, the storage capacity can be  
4 approximated by the sum over all the zones of the number of strong heads  
5 multiplied by the high frequency data storage per zone multiplied by the format  
6 efficiency per zone plus the sum over all the zones of the number of weak heads  
7 multiplied by the low frequency data storage per zone multiplied by the format  
8 efficiency per zone.

9  
10 For example, the format optimizer 66 is provided with joint BPI  
11 distributions at the target performance metric. Then, for every combinatorial  
12 possibility of head allocation to high or low frequency, the format optimizer 66  
13 searches through a continuous range of possible frequencies by considering  
14 every zone independently using the marginal distributions and by the  
15 combination of zones using the joint BPI distributions to maximize the yield  
16 calculated using a closed form equation, such that the storage capacity after the  
17 vertical zoning is applied is essentially the same as the nominal storage capacity.  
18 Further, the optimal high and low frequency profiles for every combination of  
19 head allocations is compared and the one that results in the highest yield is  
20 chosen and passed to the format generator 68 for the generation of vertically  
21 zoned configuration pages to be used by the disk drive firmware.

22  
23 The disk surfaces can be partitioned into more than three zones. To  
24 reduce computational complexity and time, if the selected/designed number of  
25 zones per disk surface is more than three, the format optimizer 66 can generate  
26 high and low frequency profiles three zones at a time and smooth the profile after  
27 post-processing. Another approach includes embedding the smoothing operator  
28 in the design and extending the joint optimization to all the zones to consider the  
29 impact of smoothing to yield calculation as part of the design rather than the later  
30 stages.

1           In the disk drive with four heads, the yield is maximized while preserving  
2   the nominal storage capacity. To determine the number of head allocations, the  
3   format optimizer 66 begins with one weak head and three strong heads per zone.  
4   The format optimizer 66 searches through a continuous range of possible  
5   frequency capabilities per zone, as well as two and three zones at a time, by  
6   considering the 1D, 2D and 3D BPI distributions that result in the best calculated  
7   yield such that a minimum nominal storage capacity can be obtained. Next, the  
8   format optimizer 66 uses two weak heads and two strong heads and repeats  
9   solving the constrained optimization problem. This process is continued until all  
10   the combinatorial possibilities are considered. Finally, the format optimizer 66  
11   chooses the solution that results in the best yield and provides the target high  
12   and low optimal data density format profiles and the associated number of high  
13   and low head allocations to the format generator 68. The format generator 68  
14   then generates vertically zoned format files and configuration pages to be used  
15   by the disk drive firmware.

#### 16 17   Format Generator

18           The format generator 68 generally performs three functions. First, the  
19   format generator 68 uses target formats/frequencies (or linear densities/BPI) for  
20   each zone and calculates the data storage of each zone and thus the storage  
21   capacity of the disk drive. Second, the format generator 68 calculates the format  
22   efficiency (the percent of the disk surface that is occupied by user data) for each  
23   zone. Third, the format generator 68 generates configuration pages. The  
24   configuration pages contain per-drive, per-zone, and per-head-per-zone  
25   parameters that are programmed into the disk drive electronics such as the  
26   preamplifier 21, the read/write channel 51 and the controller 57. The parameters  
27   are ordered such that the disk drive firmware selects the correct set of  
28   parameters to be programmed into each of the components for the particular  
29   head and zone that is being written to or read from at the time.



1           The format generator 68 calculates the frequency and the data storage of  
2 each zone taking into consideration limitations in the programmability and the  
3 capability of the disk drive components. For example, the heads 16 have varying  
4 down-track separation between the read and write elements, the preamplifier 21  
5 has a minimum and maximum delay in turning on the write current, the read/write  
6 channel 51 synthesizer frequencies are limited to discrete frequencies, the motor  
7 driver 53 can keep the spindle motor 14 within a finite precision of the nominal  
8 rotational speed, the controller 57 has specific latencies in generating commands  
9 to the preamplifier 21 and the read/write channel 51 often with a finite uncertainty  
10 as to the exact timing of these commands, and a reference crystal (not shown)  
11 has finite accuracy and stability over temperature.

12  
13           The format generator 68 can be fully automated, or can be directed by a  
14 human operator. In the absence of input from the format optimizer 66, the target  
15 per-zone BPI/frequency profiles, in particular, must be generated by a human  
16 operator. In general, the human operator modifies the target frequency profiles  
17 until the desired storage capacity is reached.

18  
19           The format generator 68 includes a format efficiency process that uses the  
20 format optimizer 66 target high/low variable BPI format designs as well as the  
21 optimal predetermined number of high/low performing head allocations to modify  
22 and generate the appropriate configuration pages as part of the file system. For  
23 each zone, the format generator 68 selects the nearest frequency to the target  
24 frequency for that zone, given the component limitations mentioned above. The  
25 nearest frequency provides the target formats.

26  
27           The optimal predetermined number of high/low performing head  
28 allocations comprises the number of heads allocated to each of the multiple  
29 frequencies in each zone. The format optimizer 66 determines the head  
30 allocation, which is input to the format generator 68. The capacity of a zone

1 depends on the target frequencies and the number of heads allocated to each  
2 frequency.

3  
4 The format optimizer 66 uses the nominal average BPI or frequency  
5 (nominal BPI format target designs) (e.g., one read/write frequency) in each zone  
6 from the format generator 68 to estimate the yield before applying the variable  
7 BPI designs. For a design with multiple frequencies per zone, this is the  
8 weighted average by the number of allocated heads of the multiple frequencies.  
9 The nominal format is created by a human operator working with the format  
10 generator 68 in an interactive manner.

11  
12 The format generator 68 calculates the number of tracks per zone,  
13 number of blocks per track, radius at each zone as well as block and track format  
14 efficiency to calculate the zone data storage. The format optimizer 66 estimates  
15 the zone data storage using the tracks per zone, radii, and format efficiency.  
16 Thus, the format optimizer 66 and the format generator 68 interact as shown in  
17 FIG. 2A. For example, in a disk drive with four heads, and two data density  
18 format frequency profiles (high and low frequency profiles) with three zones  
19 across the disk surface, after the measurement and optimization processes, the  
20 format generator 68 is provided with two optimal frequency profiles and the  
21 optimal allocation of the heads. The format generator 68 then calculates the  
22 storage capacity, and if the disk drive meets the minimum required storage  
23 capacity, the format generator 68 generates the configuration pages for the disk  
24 drive firmware. The configuration pages are used by the disk drive firmware to  
25 command the head to write at an assigned frequency to a zone. If the calculated  
26 storage capacity does not meet the minimum required storage capacity, the  
27 format optimization is performed again with new format efficiency values and the  
28 process is repeated.

1    Head Assignments

2           Allocating the number of heads to the predetermined multiple frequencies  
3   in a zone, and assigning a particular head in a particular disk drive to a particular  
4   frequency, are distinct. The allocation is performed by the format optimizer 66  
5   and applies to the disk drives of a particular design. The head assignments are  
6   then performed during manufacturing as part of a test process undergone by  
7   each disk drive to be produced.

8  
9           Once the configuration pages are generated and converted to binary files  
10   as part of the file system, they can be loaded into a reserved image of the disk  
11   drive for use after power cycling. Then, for every disk drive, the assignments are  
12   performed per head and per zone to assign a predetermined number of heads to  
13   high BPI formats and the remaining heads to low BPI formats in a two frequency  
14   design, to satisfy the allocation of heads to the formats by the format optimizer  
15   66.

16  
17           The head assignments for the two frequency format where high and low  
18   frequencies are used includes the steps of:

19           (1)   Load default parameters from the configuration pages, and  
20   calibrate selected parameters on a per head, per zone basis (e.g., load high BPI  
21   format profile for all the zones across the stroke);

22           (2)   Take measurements from the heads at the disk surfaces at  
23   preselected zones with respect to a target performance metric;

24           (3)   For each head in every measured zone, sort/rank the heads by the  
25   target performance metric from best to worst, select a prespecified (by the  
26   allocation process in the format optimizer 66) number of heads with the best  
27   performance, and assign those heads to the high frequency for a particular zone;

28           (4)   Optionally interpolate between the measurements obtained from  
29   the preselected number of zones to find the results for the other zones, and do  
30   the same for the interpolated zones. The interpolation reduces the test time.

31   Head performances are measured, sorted and assigned to a frequency for a

subset of the total number of zones. For the remaining zones, the heads are assigned by interpolating the head assignments from the measurements;

(5) For every zone, save the worst prespecified number of weak heads with respect to the target performance metric; and

(6) For every zone, load and calibrate the weak heads with the low BPI format.

The above process can improve storage capacity, improve yield and tradeoff between storage capacity and yield. In a test, the heads can pass or fail with respect to a target performance metric to determine if the test target limits are met.

The disk drive firmware is extended to load more than one format profile. A head can be assigned a different read/write frequency per zone across a disk surface, and radially similarly situated zones on different disk surfaces can have different read/write frequencies assigned to the corresponding heads whereby one head is assigned a different frequency/format profile than another head.

The head assignments apply to a format design with two recording frequencies per zone, but can be easily extended to more than two frequencies per zone and can be iterated to assign heads to more than two frequencies per zone. For example, in a design with  $H$  heads and  $F$  frequencies per zone, steps 1 and 2 are completed for the high frequency. The first selection of heads in step 3 assigns the highest  $h_1$  heads, where  $h_1$  is the prespecified number of heads allocated to the highest frequency for that zone. The remaining  $(H - h_1)$  heads are then loaded and calibrated with the second highest frequency (step 1 again), measurements are taken (step 2 again), the heads are ordered relative to the metric and the best  $h_2$  heads are assigned to the second highest frequency (step 3 again). Here  $h_2$  is the prespecified number of heads allocated to the second highest frequency in the zone. Steps 1-3 are then iterated for the  $(H - h_1 - h_2)$  heads, followed by the  $(H - h_1 - h_2 - h_3)$  heads, and so on, until  $h_F$  heads

remain to be assigned to the lowest frequency. The set of  $\{h_1 \dots h_F\}$  heads receive the head allocation made by the format optimizer 66.

Table 1 illustrates the vertical zoning head assignments on a disk drive with six heads and five zones across the stroke on each disk surface. Each head is assigned to either a high or low data density format based on record/playback performance of that head, and the number of heads assigned to high data density and the number of heads assigned to low data density is according to the head allocation determined by the format optimizer 66.

| HEAD | ZONE 1 | ZONE 2 | ZONE 3 | ZONE 4 | ZONE 5 |
|------|--------|--------|--------|--------|--------|
| 0    | Low    | High   | Low    | High   | Low    |
| 1    | High   | Low    | High   | High   | Low    |
| 2    | High   | Low    | High   | Low    | High   |
| 3    | High   | High   | Low    | High   | High   |
| 4    | Low    | High   | High   | High   | High   |
| 5    | High   | High   | High   | Low    | High   |

Table 1 – Example format assignment of a disk drive after test using vertical zoning with variable BPI across zones.

FIG. 3 shows a flowchart of vertical zoning data collection that includes the steps of:

(1) Select a number of disk drives for data measurement/collection (step 300);

(2) Create a nominal linear bit density profile  $\overline{kFCI}$  (nominal  $\overline{kFCI}$ ):  $\overline{kFCI}(R)$ , where  $R$  is the disk radius (step 302);

(3) Create more linear bit density profiles by multiplying the nominal  $\overline{kFCI}$  by the scaling factor  $x_i$  (step 304):

$$(1 \pm x_i) * \overline{kFCI}(R)$$

1           (4)     Create a binary file system for every generated profile (step 306):

$$i \in \{1, \dots, N\}$$

2

3           where N is the total number of frequency format profiles, for  
4     example, for  $N = 2$ , having  $X_1$ , and  $X_2$ , if  $X_1 = 0.05$  and  $X_2 = 0.1$ , then including  
5     the nominal frequency format there are five different frequency profiles in step  
6     304 as follows: (a) nominal KFCI, (b) 1.05 x nominal KFCI, (c) 0.95 x nominal  
7     KFCI, (d) 1.1 x nominal KFCI, and (e) 0.90 x nominal KFCI;

8           (5)     Select the first head by setting  $i$  to 1 (step 308);

9           (6)     Load the file system  $i$  into the reserved image of the disk drives  
10    (step 310);

11          (7)     Take the head performance measurements (step 312);

12          (8)     Unload and save the results in the data base (step 314);

13          (9)     Increment  $i$  by one (step 316);

14          (10)    Determine if  $i = N$  (step 318);

15          (11)    If not, go to step 310; and

16          (12)    Otherwise, stop (step 320).

17

18          The above process collects performance data for all the heads at all the  
19    zones.

20

21          FIG. 4 shows a flowchart of vertical zoning post-measurement and per  
22    zone BPI distribution extraction that includes the steps of:

23          (1)     Organize the head performance data for every head  $i \in \{1, \dots, M_1\}$

24    and every zone  $j \in \{1, \dots, M_2\}$  as a function of the linear bit density samples,

25    where  $M_1$  is the total number of heads in the disk drives selected for  
26    measurement and  $M_2$  is the total number of zones, to generate head  
27    performance histograms (step 400);

28          (2)     Choose a target performance metric (step 402);

29          (3)     Set  $j = 1$  and  $i = 1$  (step 404);

- 1           (4)     Interpolate/extrapolate BPI at the target performance metric for
- 2     head  $i$  at zone  $j$  (step 406);
- 3           (5)     Select the next head by incrementing  $i$  by one (step 408);
- 4           (6)     Determine if all the heads have been processed by determining if
- 5      $i = M_1$  (step 410);
- 6           (7)     If not, go to step 406 to process the next head, otherwise generate
- 7     a frequency capability histogram at zone  $j$  for all the heads (step 412);
- 8           (8)     Determine if all the zones have been processed by determining if
- 9      $j = M_2$  (step 414);
- 10          (9)     If not, move to the next zone and start with the first head again, set
- 11      $j = j + 1$  and  $i = 1$  (step 416) and go to step 406; and
- 12          (10)    Otherwise, stop (step 418).

13

14           The above process generates 1D frequency capability histograms at a

15     target performance metric for every zone by considering all the heads from the

16     sample disk drives selected for measurement. Using the 1D frequency capability

17     histograms at a target performance metric, probability theory known to those

18     skilled in the art can be adopted to estimate the 1D frequency capability

19     distributions. Further, the above process is extended by using 2D and 3D

20     interpolation/extrapolation routines to extract and estimate the 2D and 3D joint

21     frequency capability histograms and their associated distributions.

22

23           FIG. 5 shows a flowchart of head assignments for  $N$  heads with a two

24     frequency format (high/low data density) that includes the steps of:

- 25          (1)     Assign all the heads in a disk drive to the high data density format
- 26     (step 500);
- 27          (2)     Calibrate all the heads at the high data density format for selected
- 28     zones (step 502);
- 29          (3)     Measure the head performance metric at the selected zones for all
- 30     the heads (step 504);

1           (4)    For each selected zone, rank the heads by the head performance  
2    metric (step 506);

3           (5)    For each selected zone, assign the highest K heads to the high  
4    data density format, and assign the other N-K heads to the low data density  
5    format (step 508);

6           (6)    Optionally interpolate the head assignments for the remaining  
7    zones (step 510); and

8           (7)    Complete the calibration of all the heads and all the zones at the  
9    assigned formats (step 512).

10  
11           The above process completes the assignment of each head in each disk  
12    drive to a predetermined frequency.

13  
14           The format generator 68 passes the track formats to the format optimizer  
15    66 to have a more accurate way of calculating the storage capacity (nominal  
16    format). Such information and constraints are provided to the format optimizer  
17    66 to solve the joint optimization problems. The format optimizer 66 performs a  
18    coarse calculation of the storage capacity, whereas the format generator 68  
19    performs an exact calculation of the storage capacity. The format generator 68  
20    provides format information (such as number of tracks per zone, and the zone  
21    format) to the format optimizer 66, and calculates the exact storage capacity.  
22    Such information is passed once from the format generator 68 to the format  
23    optimizer 66 for a head design with a given number of heads. The format  
24    generator 68 initially provides nominal information to the format optimizer 66, and  
25    the format optimizer 66 performs its calculation of target densities (zone  
26    frequencies and number of heads allocated to each frequency) and provides that  
27    information to the format generator 68. The format generator 68 then determines  
28    if required storage capacity has been reached. Adjusting the target densities to  
29    meet storage capacity and/or yield requirements includes adjusting the selected  
30    zone density or zone frequencies.



FIG. 6 shows a flowchart of format generation and optimization in which an iterative process for a minimum storage capacity (C) and a user specified storage overcapacity ( $\Delta$ ) includes the steps of:

(1) Determine the disk geometry, track density and servo spoke details, and provide the inner diameter (ID) and outer diameter (OD) radii, the track density (TPI), the number of servo spokes, and the servo spoke length (step 600);

(2) The format generator 68 generates the initial format at the storage capacity using the ID and OD radii, the TPI, the number of servo spokes and the servo spoke length, and provides the radius of each zone per disk surface, the number of tracks per zone, the number of blocks per track, and the format efficiency by zone (step 602);

(3) The format optimizer 66 generates optimal target densities at all the zones using the radius of each zone per disk surface, the number of tracks per zone, the number of blocks per track, and the format efficiency by zone and provides the high and low BPI targets by zone and the number of high and low BPI head allocations by zone (step 604);

(4) The format generator 68 generates new formats with a storage capacity (the number of logical blocks per disk drive) (step 606);

(5) Determine if the storage capacity  $> C$  and the storage capacity  $< (C + \Delta)$  (step 608);

(6) If not, adjust the target densities (step 610) and go to step 606; and

(7) Otherwise, stop (step 612).

For example, the disk surface capacity is  $TPI \times BPI \times (1 + ECC) / FE$ , where TPI is the track density, BPI is the linear bit density, ECC is the fractional level of error correcting code which is typically about 0.1, and FE is the format efficiency which is typically about 0.57.

The above process completes the format generation.

As another example, a set of thirty-two mature disk drives are selected and each disk drive includes twelve heads. The 1D, 2D and 3D BPI distributions are extracted at an on-track symbol error rate from the outer, middle and inner zones. Next, the BPI distributions are fed to the format optimizer 66, and high or low frequency per zone format designs are obtained at the three zones. This is performed once by individual optimization based on 1D BPI distributions at each of the three zones, and once by joint optimization based on the measurements obtained from the three zones and their extracted 1D, 2D and 3D BPI distributions. The head format allocation search is performed by simulation, and for each zone the one-format designs before the application of vertical zoning are a special case of the two-format variable BPI designs by forcing the high and low formats to be equal to the nominal BPI format at that zone. Furthermore, the pass/fail of the disk drives is based on each head at every zone passing a target on-track symbol error rate as well as off-track squeeze and unsqueeze offset margins. Then, the yield is calculated by simulation by interpolation/extrapolation of the measurement data before and after the application of vertical zoning (VZ). Table 2 summarizes the results:

|                               | <u>Using Joint Optimization</u> | <u>Using Individual Optimization</u> |
|-------------------------------|---------------------------------|--------------------------------------|
| Drive Yield (Yd)              | 93.75                           | 90.625                               |
| Drives failed after VZ        | 4 & 29                          | 4, 6 & 29                            |
| Drives recovered              | 2, 3, 13, 19, 21 & 25           | 2, 3, 13, 19, 21 & 25                |
| Passed drives failed after VZ | None                            | 6                                    |
| Drives failed before VZ       | 2, 3, 4, 12, 19, 21 & 29        | 2, 3, 4, 12, 19, 21 & 29             |
|                               | i.e., drive yield before VZ     | i.e., drive yield after VZ           |
|                               | Yd=75%                          | Yd = 75%                             |

Table 2

Although a manufacturing test case for a two format design is illustrated, the search algorithm can be easily generalized to a higher number of formats. The design of two formats based on 1D, 2D and 3D BPI distributions can easily be generalized to higher order or dimensions by considering more than three zones. The format design can be generalized from two to a higher number of formats. The measurement procedure can be generalized to consider more zones as well as off-track measurements such as 747 curves or quality metrics

versus error rate measurements to perform a correlation study for the best metric with the least test time.

Further, the per zone variable BPI design can be easily extended to a variable BPI/TPI design. The measurement process is extended to include 747 measurements of all the heads from a preselected number of disk drives. To speed up the measurements, instead of 747 measurements, off-track and adjacency margin squeeze measurements of the heads can be performed. Once the 747 data of the heads at a preselected number of zones is determined, for every zone, joint BPI/TPI distributions can be extracted at the target(s) by post-measurement data processing. The choice of a target is an integral part of the performance gain, such as yield, due to the per zone variable BPI/TPI designs. Some example targets are off-track symbol error rate, position error signal variance, and a combination of both. After the joint BPI/TPI distributions are extracted and available for the zones, a per zone variable BPI/TPI design can be obtained by solving two constrained (joint) optimization problems: one that maximizes the yield while keeping the same disk drive areal density, and another that maximizes the disk drive areal density while keeping the same yield. Once the per zone variable BPI/TPI designs are obtained, a preselected number of heads are allocated to high and low density BPI and TPI formats, for example, for a two variable BPI/TPI per zone design performed as part of the test process.

The present invention improves storage capacity (and consequently areal density at a fixed target BPI) and yield and reduces the target TPI by increasing the average BPI across the stroke per head (depending on the number of formats considered) to meet a desire storage capacity. In particular, the BPI at the outer diameter may be limited by the maximum deliverable data rate of the ASIC components. For example, if the controller 57 has a maximum deliverable data rate of 650 MHz, the preamplifier 21 has a maximum deliverable data rate of 700 MHz and the read/write channel 51 has a maximum deliverable data rate of 750 MHz, then the BPI at the outer diameter is limited by the controller 57 at a

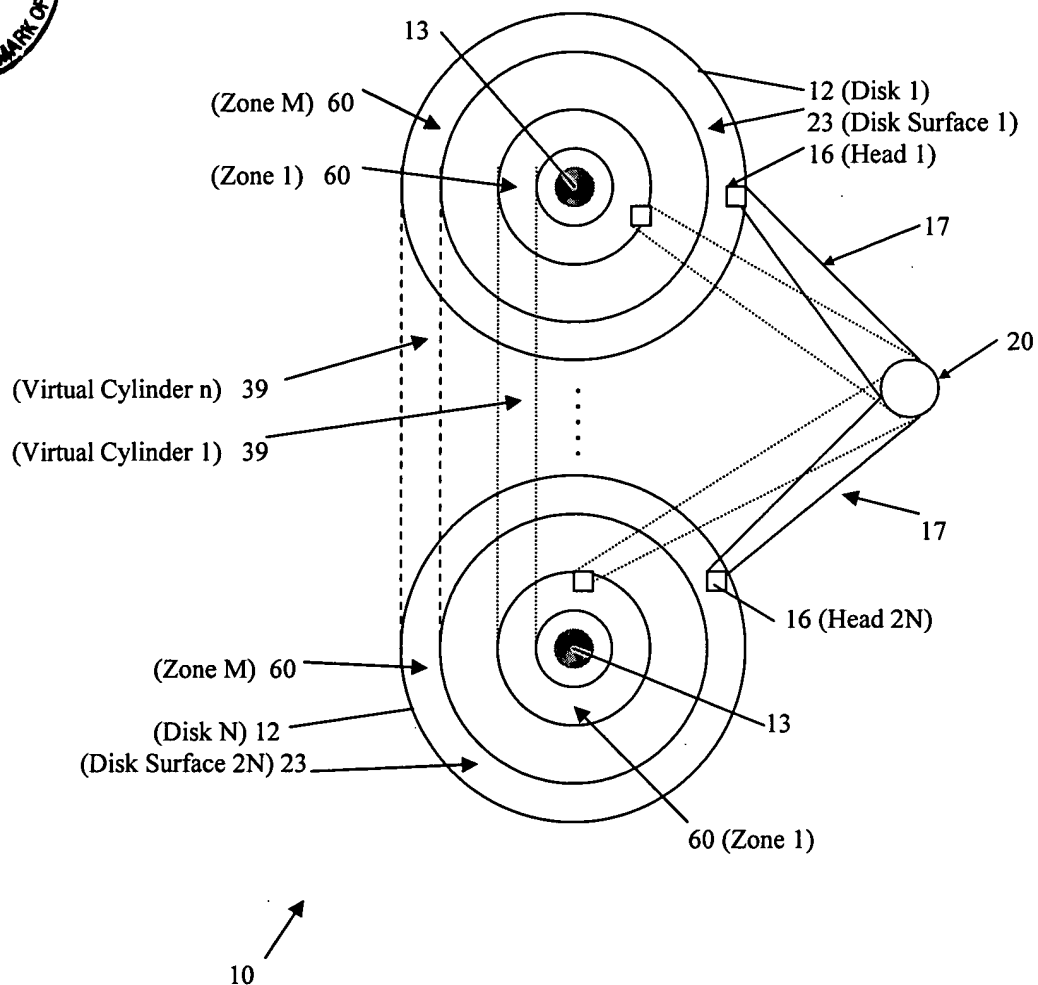
1 maximum deliverable data rate of 650 MHz. Thus, a conventional one format  
2 BPI profile across the stroke does not achieve the desired storage capacity and  
3 yield, whereas the present invention per zone variable BPI target formats meet  
4 the desired storage capacity at a fixed target TPI while improving the yield.  
5

6 The data measurer 62 can be implemented by a general purpose  
7 computer 61 and the drive electronics of the disk drive 100. The general purpose  
8 computer 61 can be a high end PC, a PC server or a workstation and include  
9 programmable simulation software. The drive electronics can include the logic  
10 circuit 49 and the controller 57. The logic circuit 49 performs the measurements  
11 and the controller 57 directs the logic circuit 49 and transfers the data to the  
12 general purpose computer 61. The head assignments can be implemented by  
13 the controller 57 with the data collection sub-task performed by the logic circuit  
14 49. The post-measurement data processor 64, the format optimizer 66 and the  
15 format generator 68 can be implemented by the general purpose computer 61.  
16

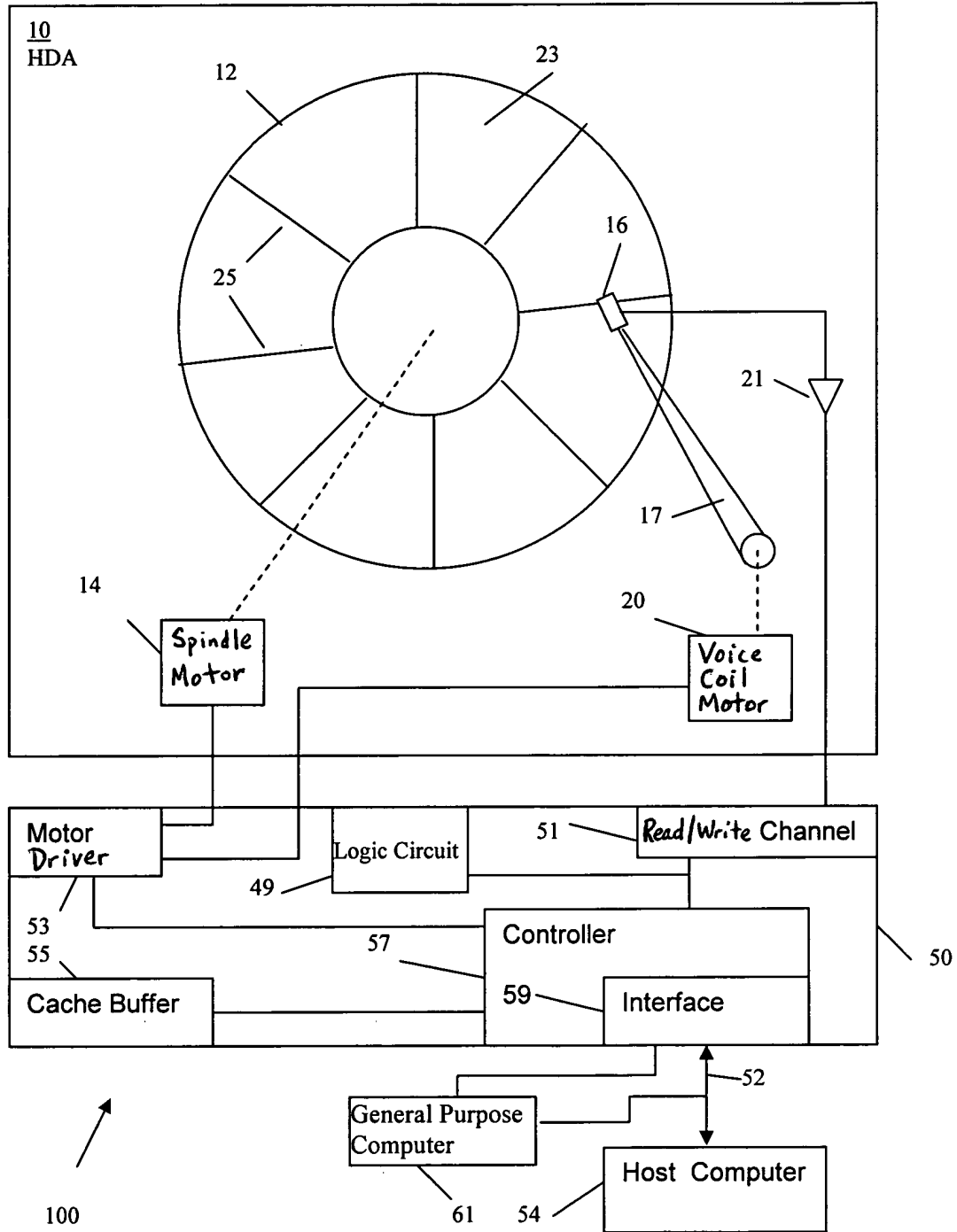
17 The present invention has been described in considerable detail with  
18 reference to certain preferred versions thereof; however, other versions are  
19 possible. Therefore, the spirit and scope of the appended claims should not be  
20 limited to the description of the preferred versions contained herein.

**Abstract**

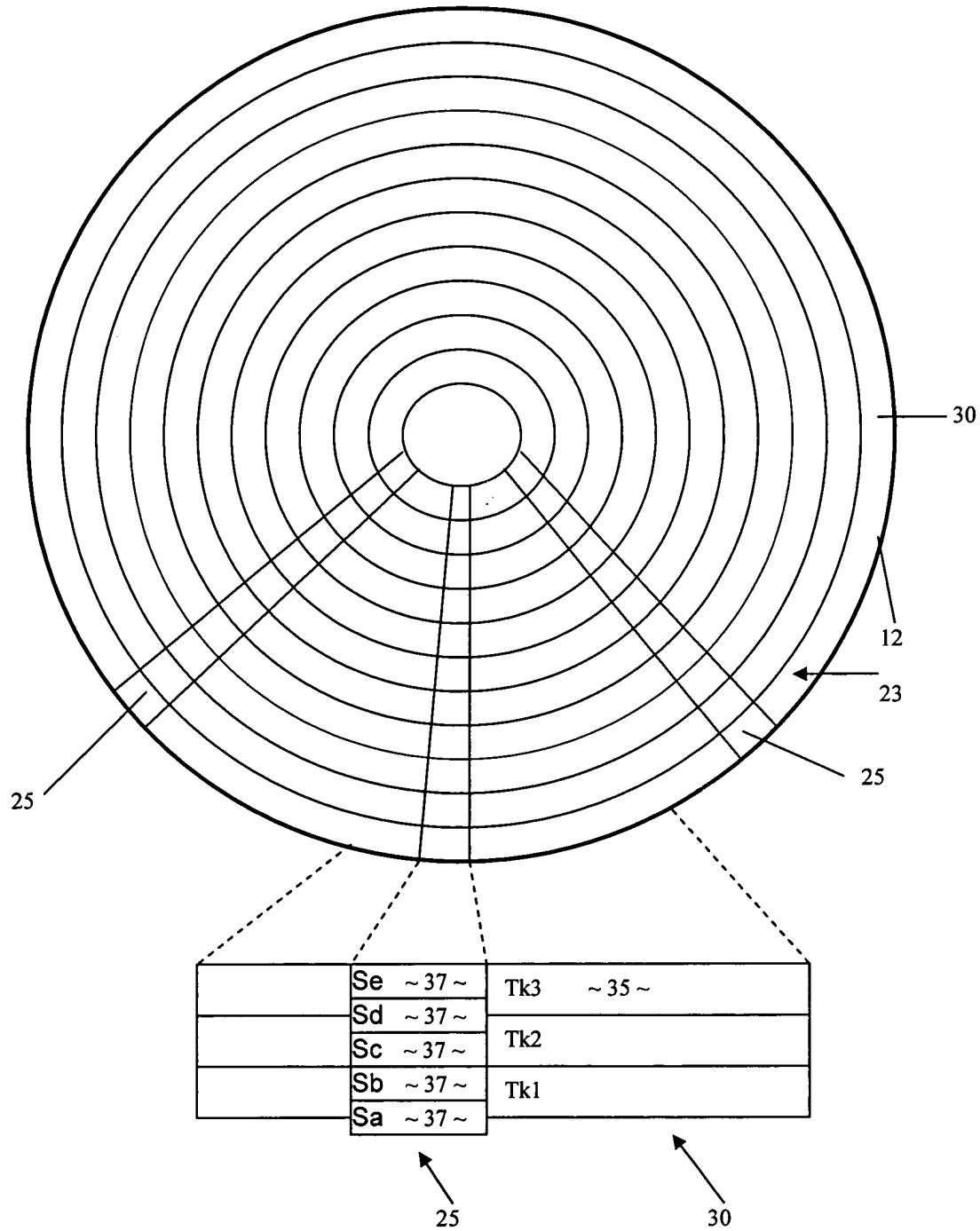
A method of defining a storage format in data storage devices, each data storage device having multiple storage media and corresponding heads, each head for recording on and playback of information from a corresponding storage media in at least one zone, and each zone including concentric tracks for recording on and playback of information. The method includes selecting a sample of the data storage devices, for each selected data storage device measuring a record/playback performance capability of each head at one or more read/write frequencies per zone, generating storage density distributions corresponding to the heads in the selected data storage devices based on the performance capability measurements, selecting a group of read/write frequencies for the data storage devices with two or more frequencies for each zone based on the storage density distributions, and assigning one of the read/write frequencies to each head based on the performance capability of that head.



**FIG. 1A**



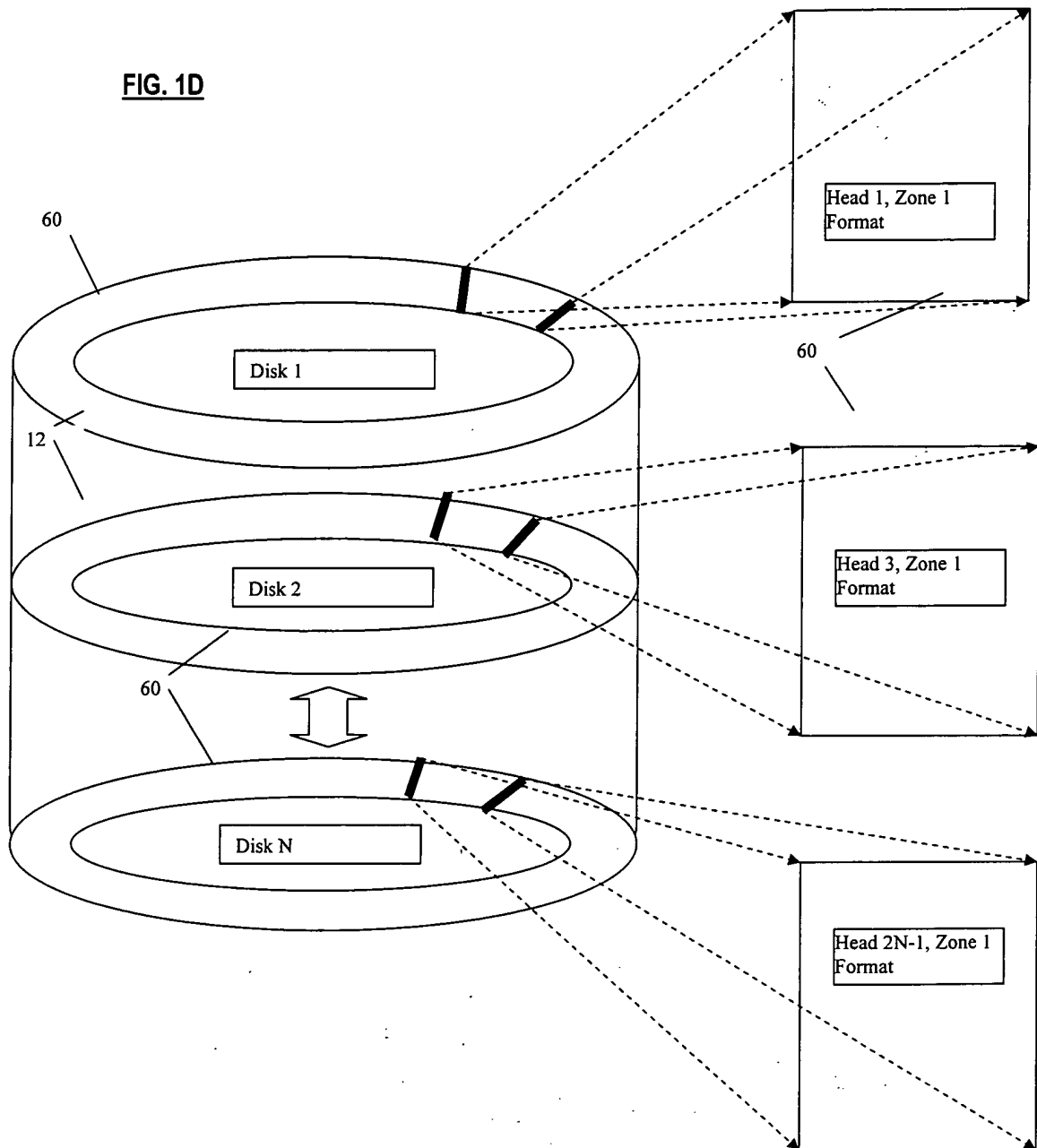
**FIG. 1B**



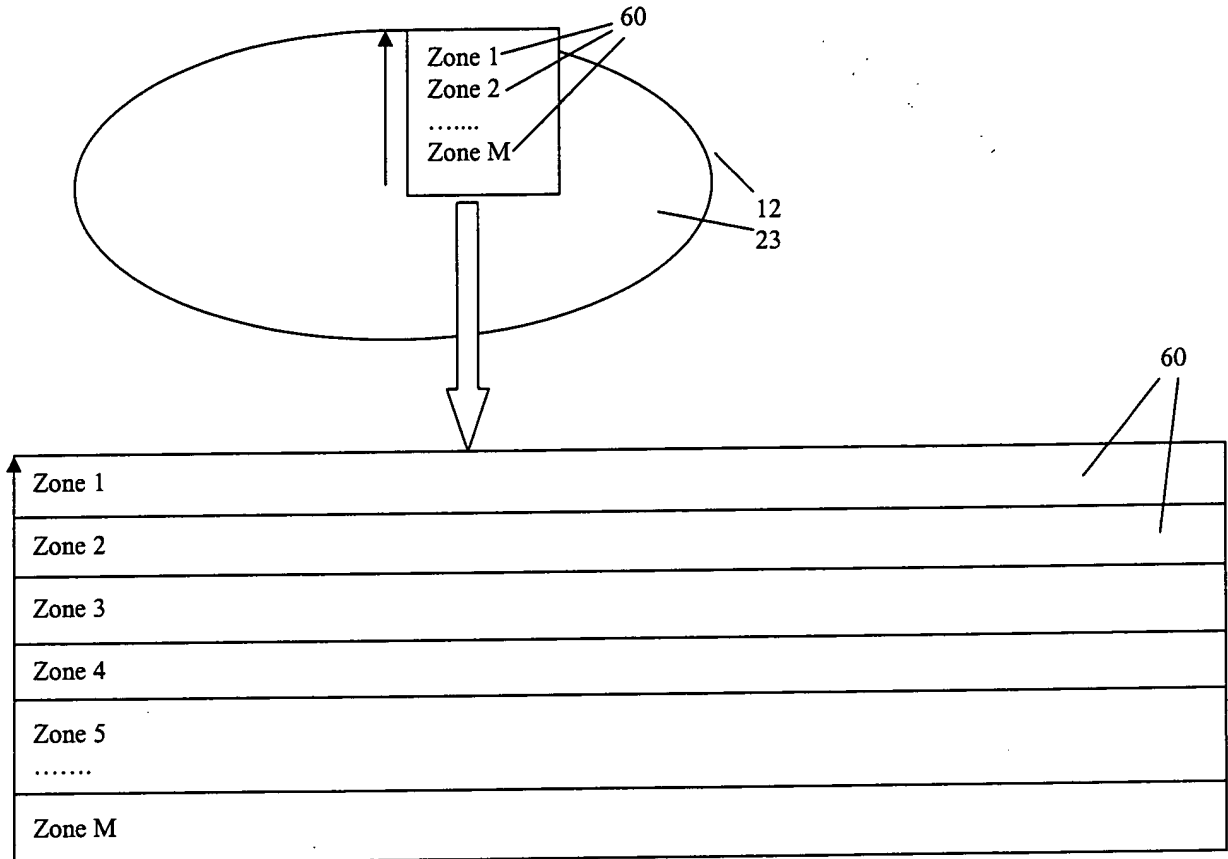
**FIG. 1C**

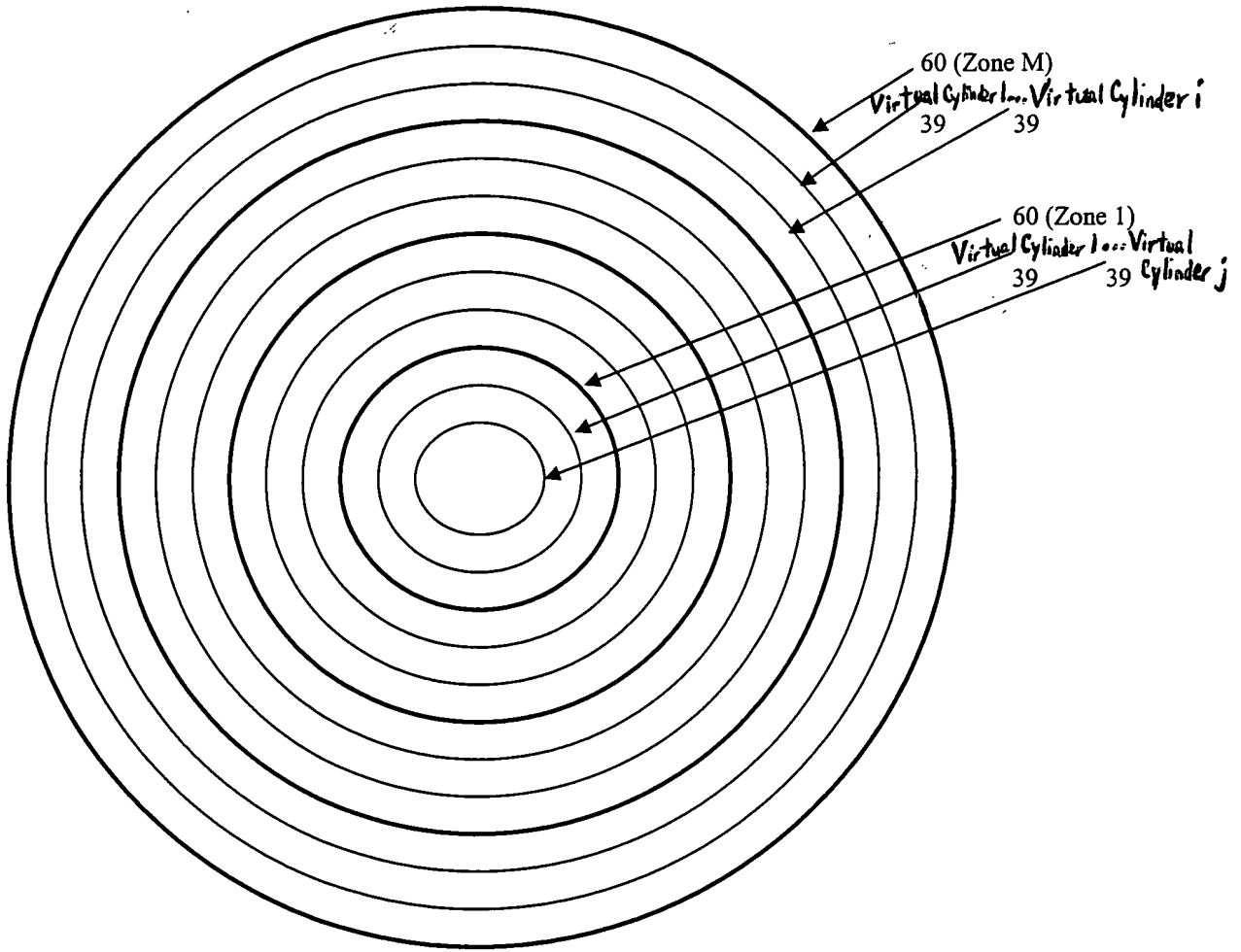


**FIG. 1D**



**FIG. 1E**





**FIG. 1F**

**FIG. 1G**

Head 1

Virtual Cylinder 1 Track 0  
Virtual Cylinder 1 Track 1  
Virtual Cylinder 1 Track 2  
Virtual Cylinder 1 Track 3  
Virtual Cylinder 1 Track 4  
Virtual Cylinder 2 Track 0  
Virtual Cylinder 2 Track 1  
Virtual Cylinder 2 Track 2  
Virtual Cylinder 2 Track 3  
Virtual Cylinder 2 Track 4  
Virtual Cylinder 3 Track 0  
Virtual Cylinder 3 Track 1  
Virtual Cylinder 3 Track 2  
Virtual Cylinder 3 Track 3  
Virtual Cylinder 3 Track 4

Head 2

Virtual Cylinder 1 Track 0  
Virtual Cylinder 1 Track 1  
Virtual Cylinder 1 Track 2  
Virtual Cylinder 1 Track 3  
Virtual Cylinder 1 Track 4  
Virtual Cylinder 2 Track 0  
Virtual Cylinder 2 Track 1  
Virtual Cylinder 2 Track 2  
Virtual Cylinder 2 Track 3  
Virtual Cylinder 2 Track 4  
Virtual Cylinder 3 Track 0  
Virtual Cylinder 3 Track 1  
Virtual Cylinder 3 Track 2  
Virtual Cylinder 3 Track 3  
Virtual Cylinder 3 Track 4

Head N

Virtual Cylinder 1 Track 0  
Virtual Cylinder 1 Track 1  
Virtual Cylinder 1 Track 2  
Virtual Cylinder 1 Track 3  
Virtual Cylinder 1 Track 4  
Virtual Cylinder 2 Track 0  
Virtual Cylinder 2 Track 1  
Virtual Cylinder 2 Track 2  
Virtual Cylinder 2 Track 3  
Virtual Cylinder 2 Track 4  
Virtual Cylinder 3 Track 0  
Virtual Cylinder 3 Track 1  
Virtual Cylinder 3 Track 2  
Virtual Cylinder 3 Track 3  
Virtual Cylinder 3 Track 4

Replacement Sheet 8 of 17 sheets

**FIG. 1H**

37 30

Head 1

Head 2

V  
I  
R  
T  
U  
A  
L  
  
C  
Y  
L  
I  
N  
D  
E  
R  
  
1

Servo Track 0

Data Track 0

Data Track 0

Servo Track 1

Data Track 1

Data Track 1

Servo Track 2

Data Track 2

Data Track 2

Servo Track 3

Servo Track 4

Data Track 3

Data Track 3

Servo Track 5

Servo Track 6

Data Track 4

Data Track 4

Servo Track 7

Data Track 5

Data Track 5

Servo Track 8

Servo Track 9

Data Track 6

Data Track 6

Servo Track 10

Data Track 7

Data Track 7

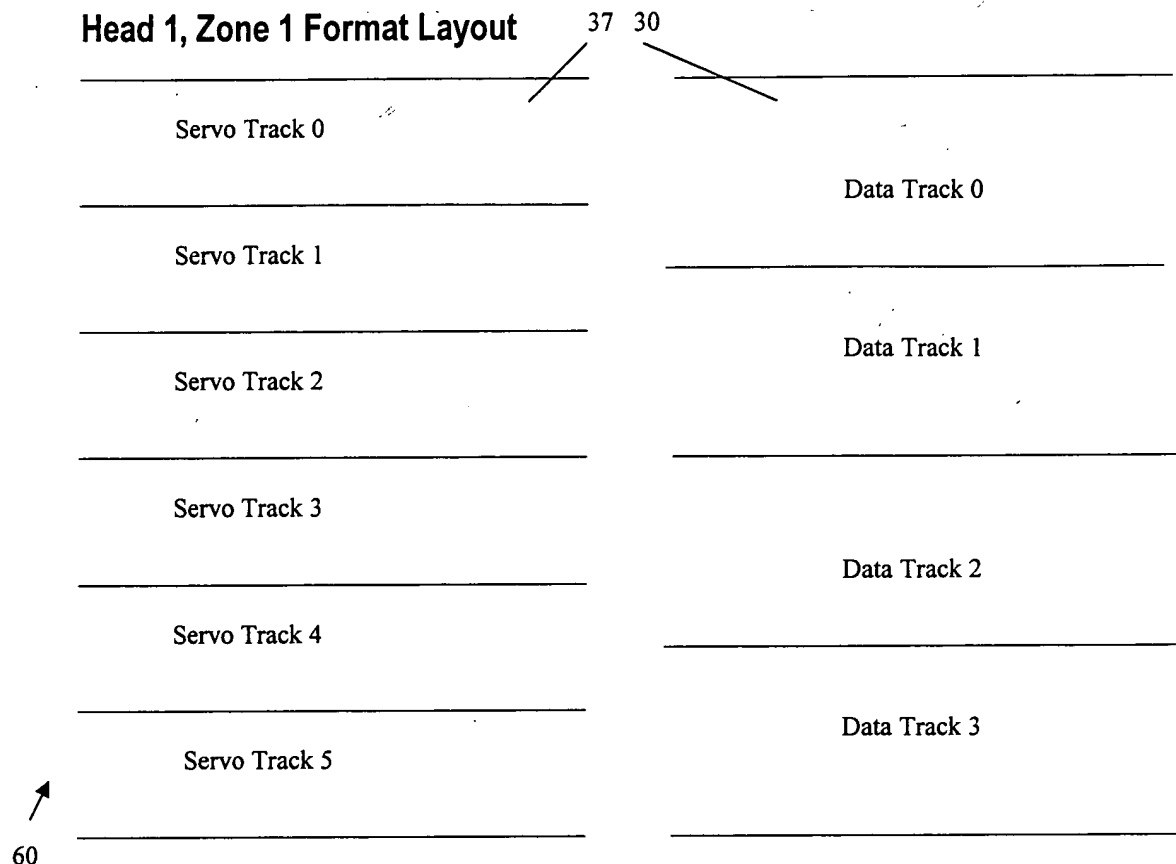
Servo Track 11

39

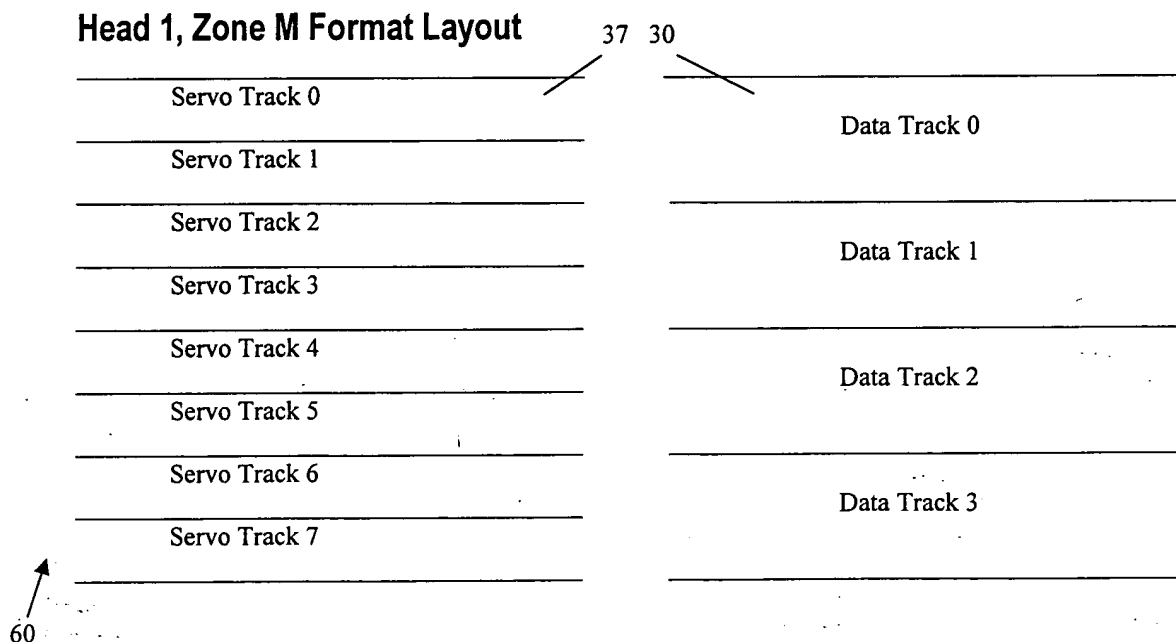
V  
I  
R  
T  
U  
A  
L  
  
C  
Y  
L  
I  
N  
D  
E  
R  
  
2

Replacement Sheet 9 of 17 sheets

## Head 1, Zone 1 Format Layout

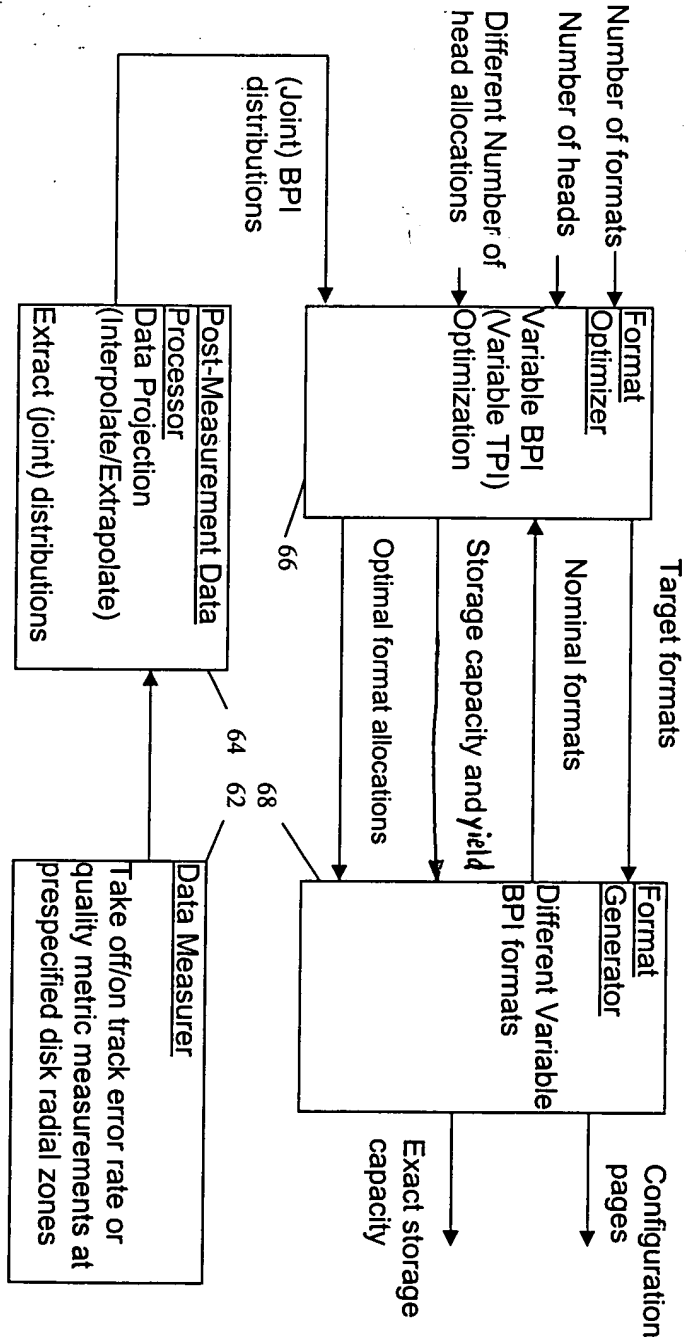


## Head 1, Zone M Format Layout



**FIG. 11**

Replacement Sheet 10 of 17 sheets



**FIG. 2A**

- + - Frequency sample
- - Least square polynomial fit
- ◇ - Projected frequency

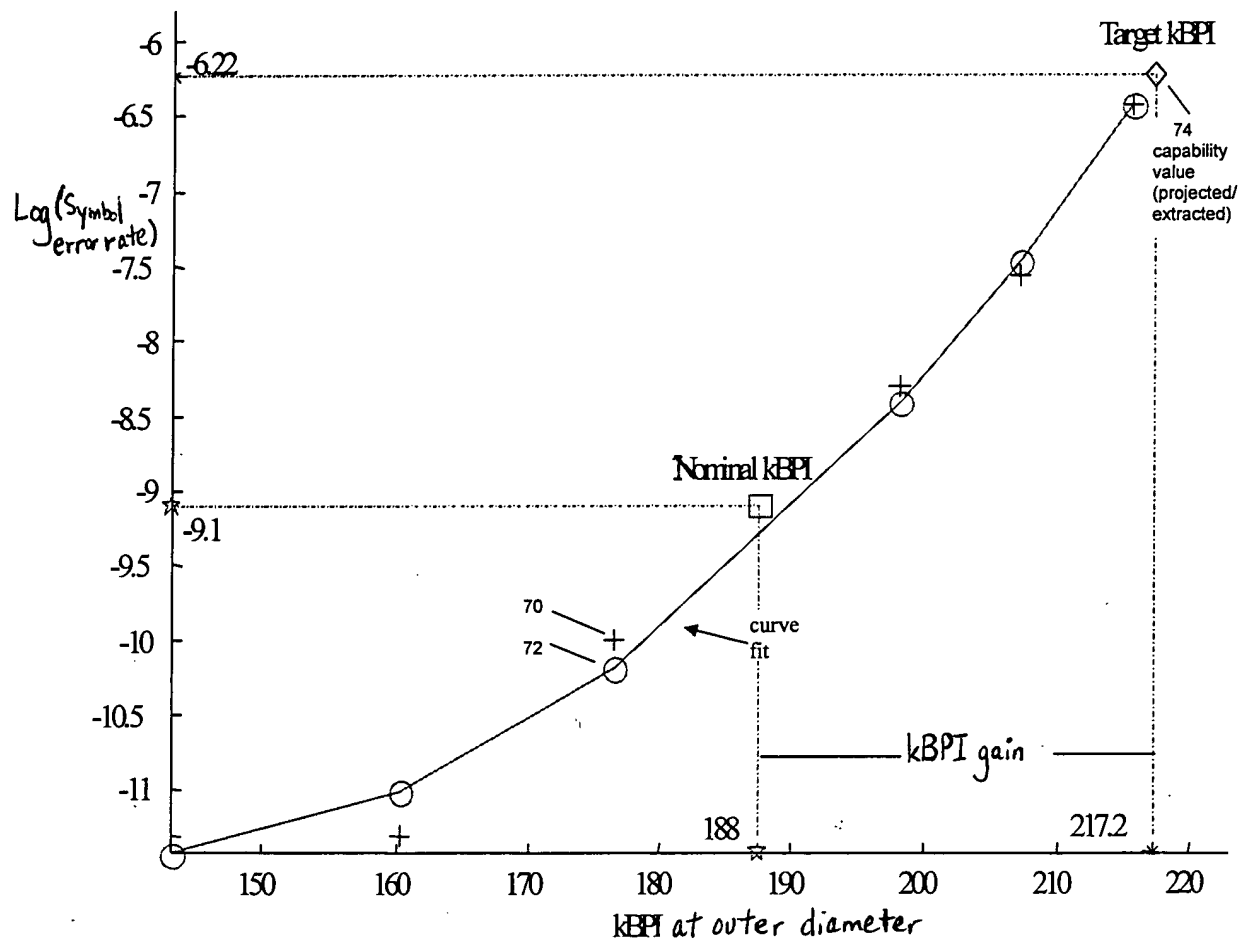
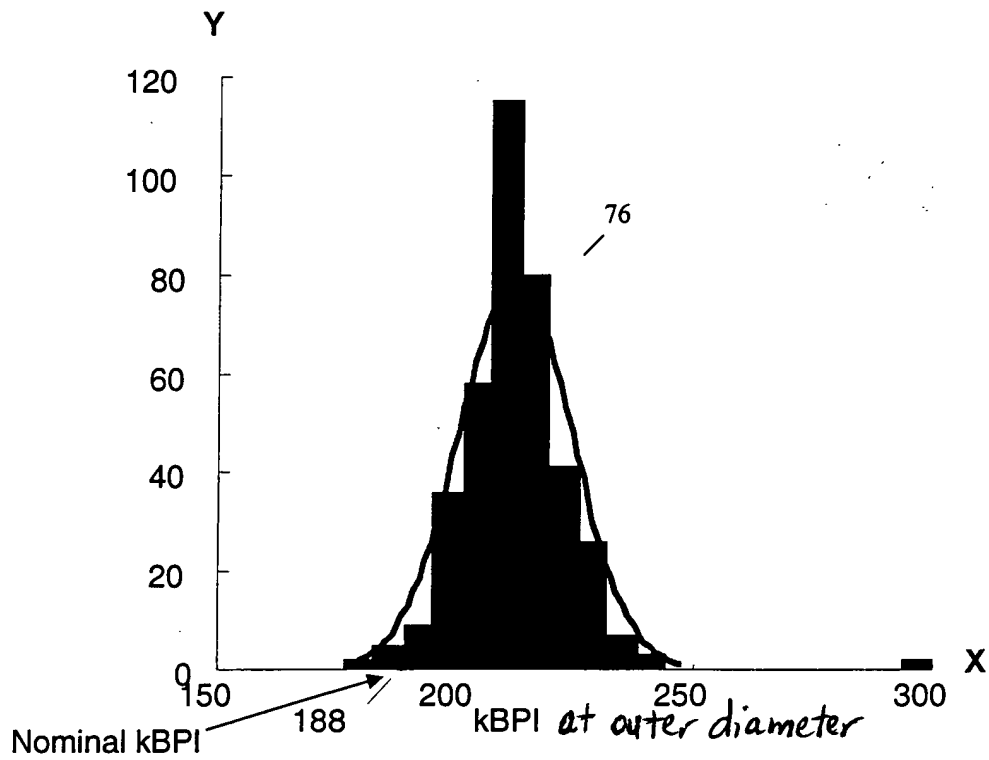
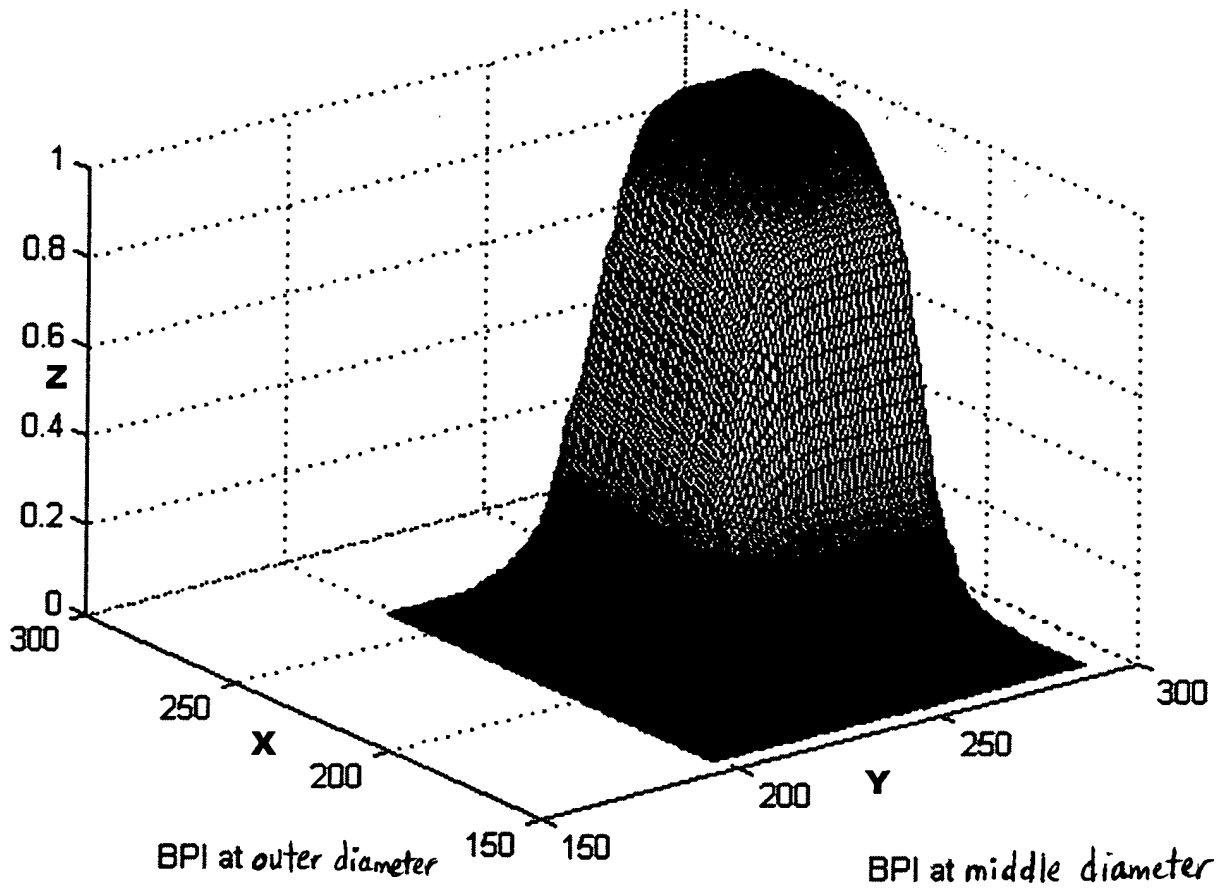


FIG. 2B

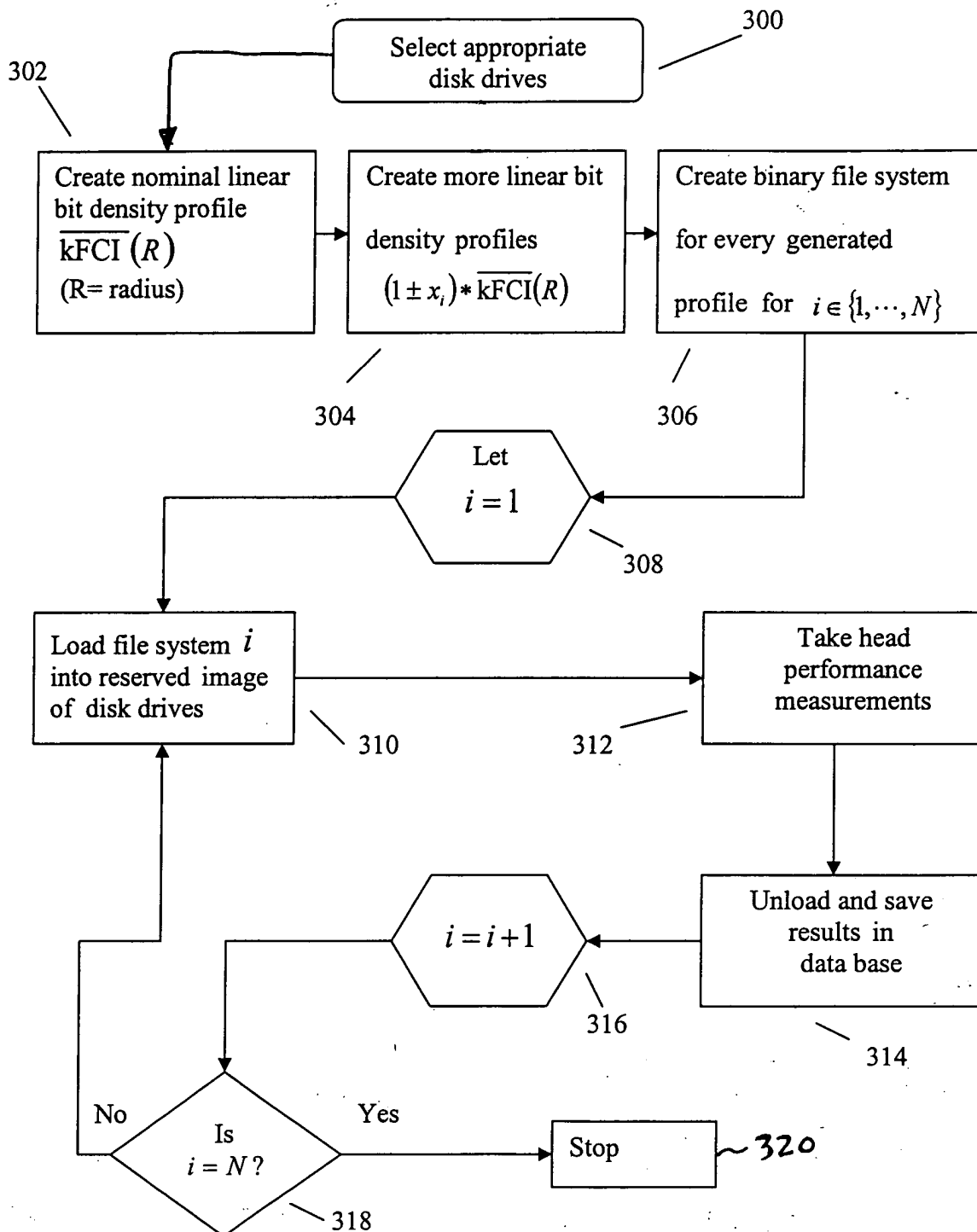




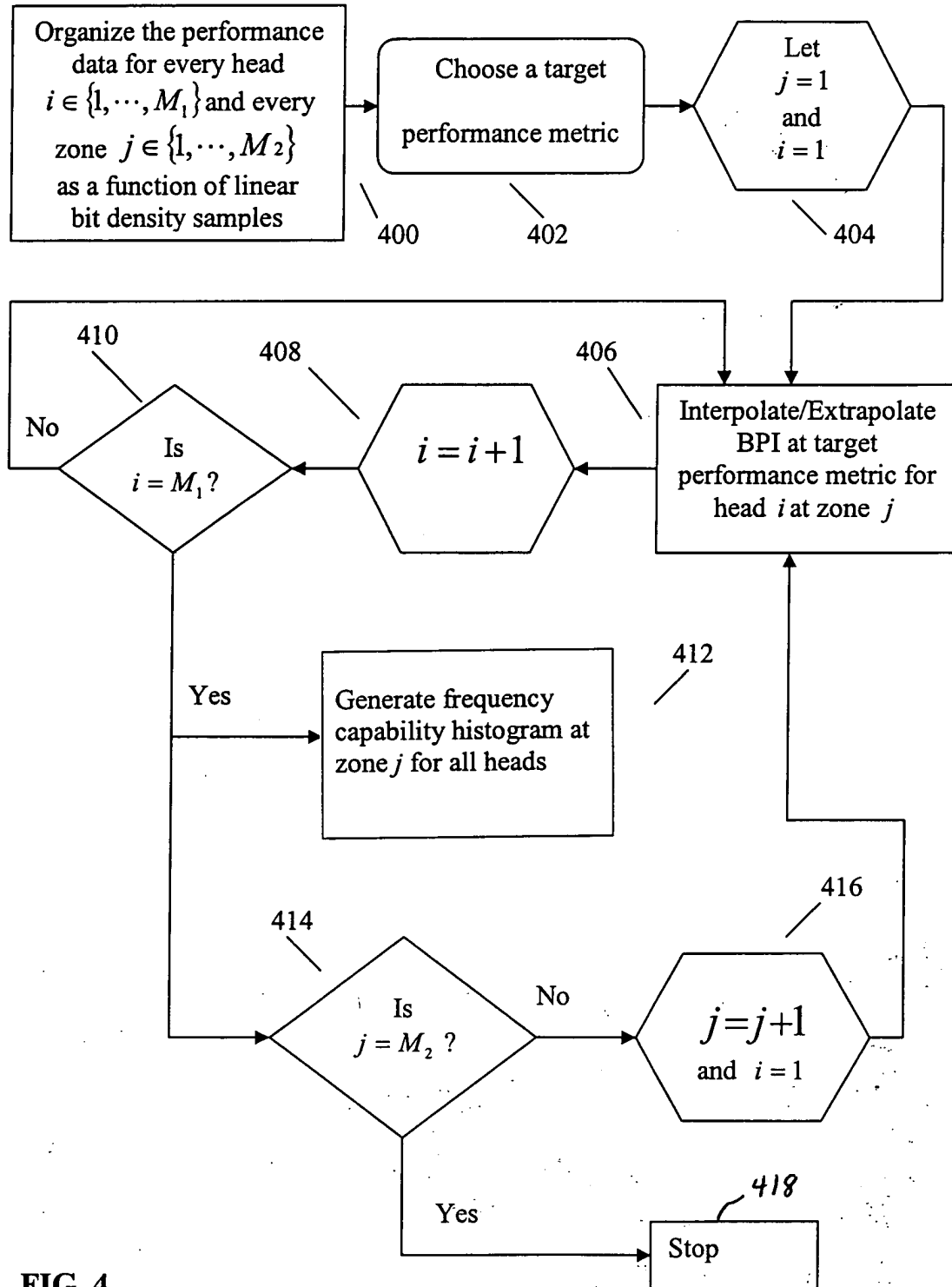
**FIG. 2C**



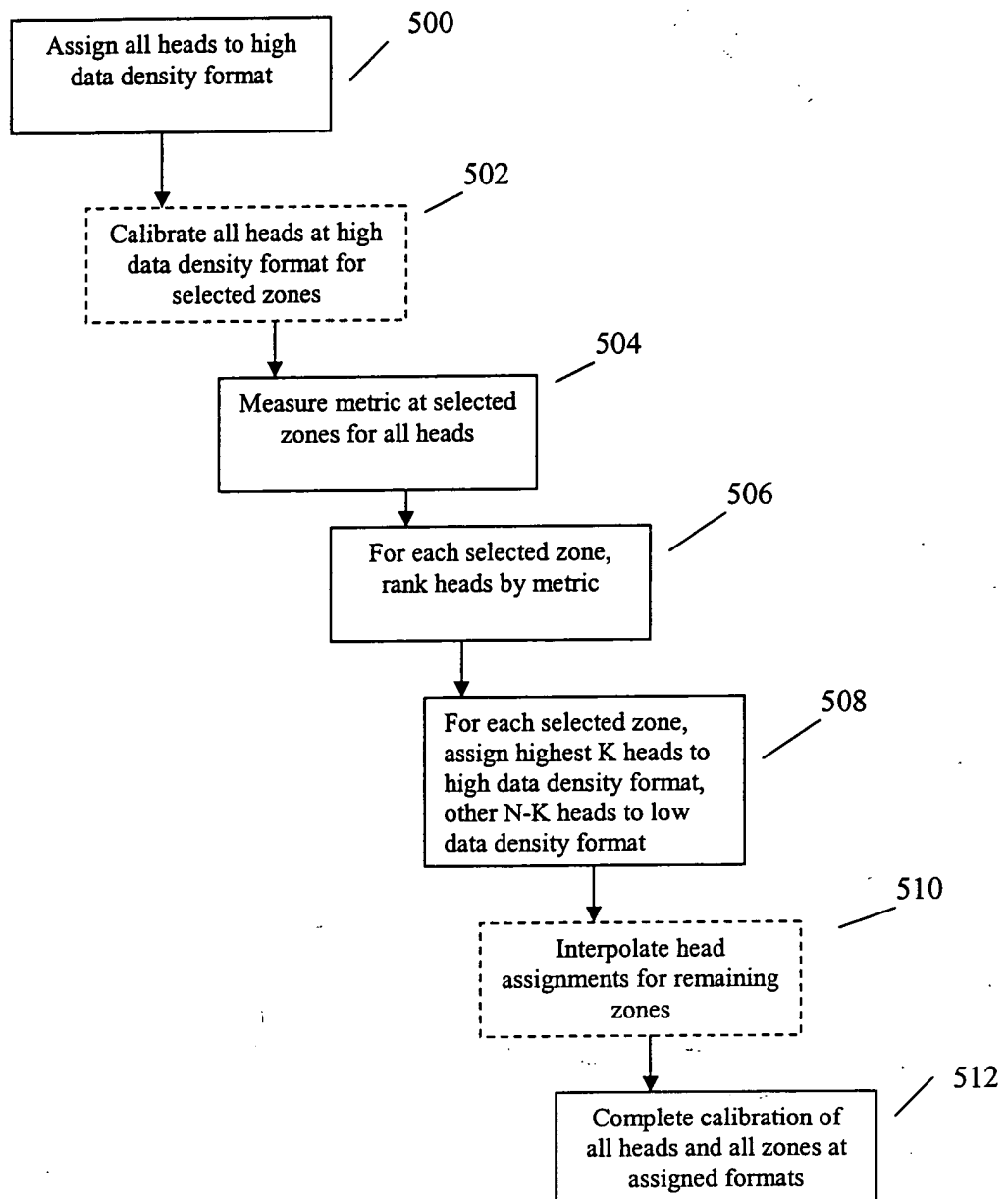
**FIG. 2D**



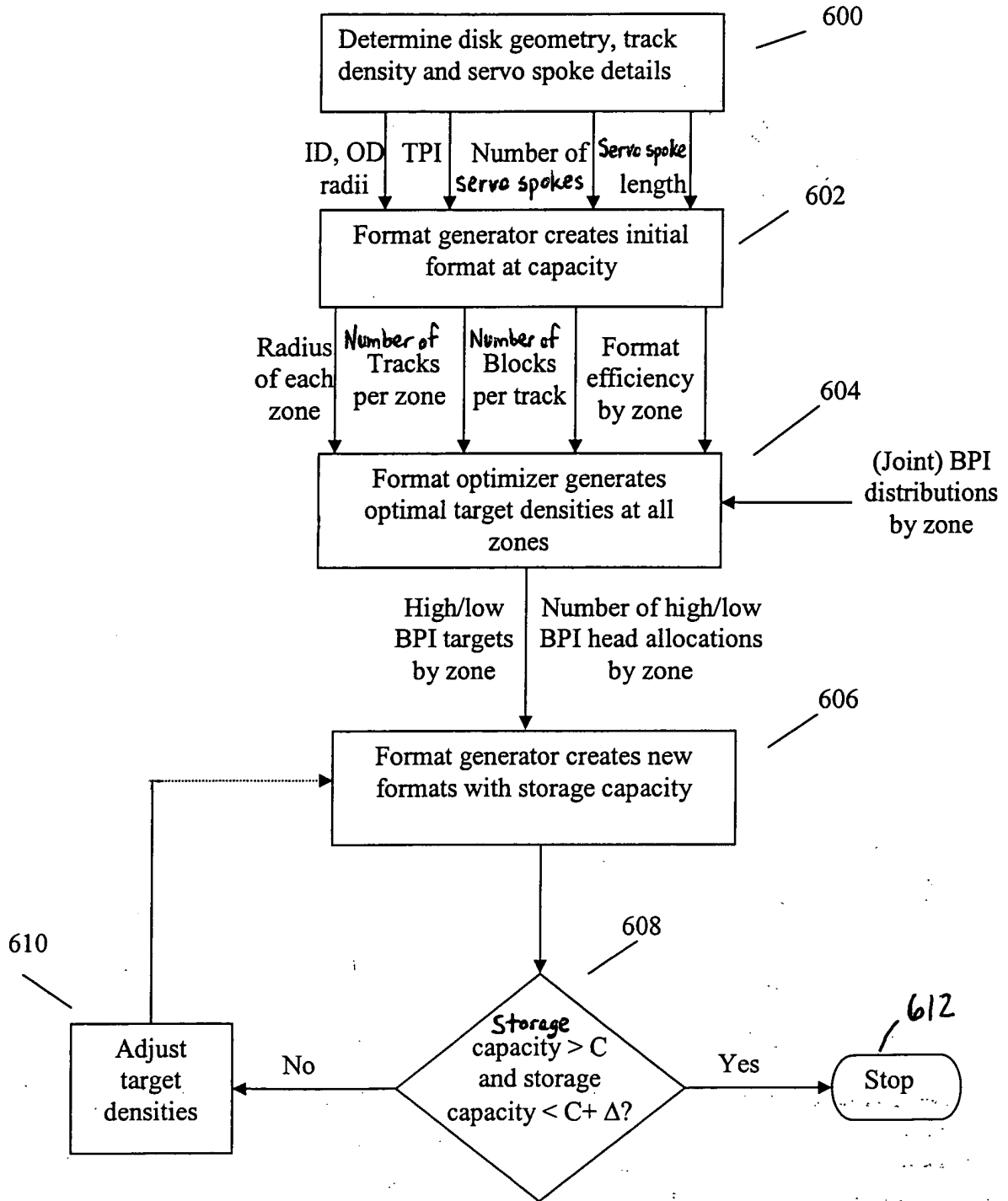
**FIG. 3**



**FIG. 4**



**FIG. 5**



**FIG. 6**